AD A 0 9 0 5 5 3

SONIC FATIGUE DESIGN TECHNIQUES FOR ADVANCED COMPOSITE AIRCRAFT STRUCTURES

FINAL REPORT

lan Holehouse

Rohr Industries
P.O. Box 878
Chula Vista, California 92012

April 1980

Technical Report AFFDL-TR-80-3019

Final Report August 1977 - December 1979



Approved for public release; distribution unlimited.

Flight Dynamics Laboratory Air Force Wright Aeronautical Laboratories Air Force Systems Command Wright-Patterson Air Force Base, Ohio 45433 00T 1 4 1980

A

Reproduced From Best Available Copy

80 10 14 197

NOTICE

When Government drawings, specifications, or other data are used for any purpose other than in connection with a definitely related Government procurement operation, the United States. Government thereby incurs no responsibility nor any obligation whatsoever; and the fact that the government may have formulated, furnished, or in any way supplied the said drawings. specifications, or other data, is not to be regarded by implication or otherwise as in any manner licensing the holder or any other person or corporation, or conveying any rights or permission to manufacture, use, or sell any patented invention that may in any way be related thereto.

This report has been reviewed by the Office of Public Affairs (ASD/PA) and is releasable to the National Technical Information Service (NTIS) At NTIS, it will be available to the general public, including foreign nations.

This technical report has been reviewed and is approved for publication.

KENNETH R. WENTZ

PROJECT ENGINEER

FRANK D. ADAMS, Acting Chief Structural Integrity Branch Structures and Dynamics Division

FOR THE CCMMANDER

RALPH L. KUSTER, JR., COL, USAF

Chief, Structures & Dynamics Division

"If your address has changed, if you wish to be removed from our mailing list, or if the addressee is no longer employed by your organization please notify _AFWAL/FIBED W-PAFB, OH 45433 to help us maintain a current mailing list."

Copies of this report should not be returned unless return is required by security considerations, contractual obligations, or notice on a specific document.

AIR FORCE/56780/26 August 1980 - 300

Unclassified SIFICATION OF THIS PAGE (When Date Entered) READ INSTRUCTIONS REPORT DOCUMENTATION PAGE BEFORE COMPLETING FORM 2. GOVT ACCESSION NO AFWAL **-**¶TR−8Ø−3019 Final Technical Report Sonic Fatigue Design Techniques August 1977-Dece for Advanced Composite Aircraft Structures AUTHOR(*) Ian Holehouse F33615-77-C-3Ø33/ PERFORMING ORGANIZATION NAME AND ADDRESS Rohr Industries P. O. Box 878 Chula Vista, California 92012 11. CONTROLLING OFFICE NAME AND ADDRESS Air Force Wright Aeronautical Laboratory Apr**a** 1980 Air Force Systems Command Wright-Patterson Air Force Base, Ohio 45433 14. MONITORING AGENCY NAME & ADDRESS(II ALL 15. SECURITY CLASS, (of this report) Unclassified DECLASSIFICATION/DOWNGRADING 16. DISTRIBUTION STATEMENT (of this Report) Approved for public release; distribution unlimited. 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, If different from Report) 18. SUPPLEMENTARY NOTES 19. KEY WORDS (Continue on reverse side if necessary and identify by block number) Acoustic Fatique Sonic Patigue Composites Graphite ABSTRACT (Continue on reverse side if necessary and identify by block number) A combined analytical and experimental program was conducted in order to develop a semi-empirical sonic fatigue design method for curved and flat graphite-epoxy skin-stringer panels. A range of multi-bay panels was subjected to high intensity noise environments in a progressive-wave tube. Shaker tests were also performed in order to provide additional random

DD FORM 1473

EDITION OF 1 NOV 65 IS OBSOLETE

Unclassified

SECURITY CLASSIFICATION OF THIS PAGE (When Date Entered)

(Continued)

407654



SECURITY CLASSIFICATION OF THIS PAGE(When Date Entered)

fatigue data. Finite-element analyses were carried out on the test panel designs, generating static strains and frequencies. Multiple stepwise regression analysis was used to develop the sonic fatigue design method. Design equations and a nomograph are presented. Comparisons of sonic fatigue resistance between graphite and aluminum panels were also carried out. The design method developed is presented as a self-contained section in this report and is suitable for practical design use

SECURITY CLASSIFICATION OF THE PAGE(When Date Enter of

FOREWORD

This report was prepared by Rohr Industries, Chula Vista, California, for the Structural Integrity Branch, Structures and Dynamics Division, Flight Dynamics Laboratory, Air Force Wright Aeronautical Laboratory, Wright-Patterson Air Force Base, Ohio, under contract number F33615-77-C-3033. The work described herein was conducted as part of the Air Force System Command's exploratory development program to establish design criteria for sonic fatigue prevention for flight vehicles.

Mr. H.F. Wolfe and Mr. K.R. Wentz were the project engineers.

This report concludes the work on contract F33615-77-C-3033, which covered a period from August 1977 to December 1979.

The author wishes to gratefully acknowledge the encouragement and assistance from Mr. H.F. Wolfe and Mr. K.R. Wentz, the AFWAL project engineers; and to Mr. J.A. Mekus of Rohr Industries for his assistance as test engineer throughout the experimental phase of the program.



TABLE OF CONTENTS

SECTION		PAGE
I	INTRODUCTION	1
II	ANALYTICAL	5
	1. Introduction	5
	2. General Sonic Fatigue Theory	7
	3. Composite Laminate Analysis	10
	4. Preliminary Sonic Fatigue Analysis	18
	5. Finite Element Solutions	18
	6. Additional Frequency Analysis	46
III	EXPERIMENTAL	4 9
	1. Introduction	4 9
	2. Test Specimen and Fixture Design	4 9
	3. Test Specimen Fabrication	54
	4. Shaker Tests	72
	5. Progressive-Wave Tube Tests	75
IV	DEVELOPMENT OF DESIGN METHOD	140
	1. Introduction	140
	2. Summary of Analytical and Experimental Results	142
	3. Regression Analysis	142
	4. Design Equations .'	173
	5. Design Method	177
	6. Design Method Comparisons	185
V	CONCLUSIONS	187
	REFERENCES	190
APPENDIX A	- FINITE ELEMENT MODELS AND RESULTS	A-1
APPENDIX B	- ENGINEERING DRAWINGS OF FEST STRUCTURES	B-1
APPENDIX C	- TEST DATA USED IN THE DEVELOPMENT OF	C_1

LIST OF ILLUSTRATIONS

FIGURE		PAGE
1	Program Phase/Task Flow Diagram	4
2	Flow Chart of Analytical Work	7
3	Location of Finite Element Models Relative to Entire Panel	22
4	Comparison of Bending Moment Distributions Using Different Size Elements and Flate Solution Take from Timoshenko (13)	23
5	Location of Points Used in Table 10	31
6	Comparison of Test and Analytical Static Strain (y) Distributions for Panel d (Z Type Stiffeners)	35
7	Comparison of Static Stress Results Between J and Z Type Stiffeners for Panel b	38
8	Finite Element Model for Shaker Specimens	44
9	Mode Shapes of Shaker Specimen No. 2	45
10	Honeycomb Beam Stiffened Panel (e)	53
11	Bond Jig for Z Layup	57
12	Bond Jig With Hat Section in Pla	58
13	Bond Jig With Bag in Place	59
14	Cured Hat Sections	60
15	Locating Tool for Zee Stiffeners	61
16	Locating Tool for Honeycomb Stiffeners	62
17	Layup of Graphite Epoxy Skin	63
18	Shaker Test Set-Up	74
19	Shaker Test Fatigue Curve: Strain v Cycles to Failure	76

FIGURE		PAGE
20	Shaker Test Fatigue Curve: Stress vs Cycles to Failure	76
21	Rockwell Facility and Rohr Mobile Laboratory	77
22	Progressive Wave Tube with Panels Installed	78
23	PWT Microphone Amplitude Distribution	80
24	Closeup of Panel Installation in the PWT	83
25	Panel 1 - Linear Response of Aluminum Skin-Stringer Panel	89
26	Panel 5 - Linear Response of Graphite Skin- Stringer Panel	90
27	Rohr Panel No. 5 After Sonic Fatigue Failure	91
28	Sections of Failed Honeycomb Stiffener from Panel No. 5	92
29	Panel al after Sonic Fatigue Testing	95
30	Panel n after Sonic Fatigue Testing	96
31	Panel p after Sonic Fatigue Testing Back Face	97
32	Panel p after Sonic Fatigue Testing Front Face	98
33	Sonic Fatigue Test Fatigue Curve: Strain vs. Cycles to Failure	102
34	Sine Sweep - Panel r, Gauge 4	104
35	Random Response - Panel r, Gauge 4-1	104
36	Random Response - Panel r, Gauge 4	105
37	Phase and Cross Spectral Density - Panel r, Gauges 4 and 4-1	106
38	Random Response - Panel s, Gauge 4-1	107

FIGURE		PAGE
39	Random Response - Panel s, Gauge 4-2	108
40	Phase and Cross Spectral Density - Panel s, Gauges 4-1 and 4-2	109
41	Center Strain - Panel b, Z Stiffener	112
42	Center Strain - Panel b, J Stiffener	113
43	Center Strain - Panel c, Z Stiffener	114
44	Center Strain - Panel c, J Stiffener	115
45	Edge Strain - Panel b, Z Stiffener	116
46	Edge Strain - Panel b, J Stiffener	117
47	Edge Strain, Panel c, Z Stiffener	118
48	Edge Strain - Panel c, J Stiffener	119
49	Phase and Cross Spectral Density for Panel b, J Stiffener, Gauges 4 and 28	120
50	Comparison of Strain Spectrum for Bonded and Riveted Panels	123
51	Strain Spectrum for Panel g-Stiffener Clips Not Attached, Gauge 4	125
52	Comparison of Strain Spectrum for Aluminum and Steel Fixtures	126
53	Response Spectrum for Panel d - Free Edges, Gauge 10	128
54	Response Spectrum for Panel d - Fixed Edge., Gauge 10	129
55	Response Spectrum for Panel d Regular Test Fixture, Gauge 10	130
56	Load Cell Spectrum	131
57	Comparison of Strain Spectrum at 160 dB and 165 dB (Panel b)	135

FIGURE		PAGE
58	Integrated Power Spectral Density for Strain Response, for Panel b, Gauge 4	. 136
59	Integrated Power Spectral Density for Panel k, Gauge 4-1	138
60	Graphic Illustration of Regression Error	160
61	Response Comparisons for Different Stringer Spacings	161
62	Response Comparisons for Different Skin Thicknesses	162
63	Response Comparisons for Different Radii of Curvature	163
64	RMS Strain Nomograph	178
65	Natural Frequency Nomograph for Panel With Fixed Edges (Reference 5)	180
66	Random Fatigue Curve for Bonded Skin- Stiffener Joint RMS Strain vs. Cycles to Failure	181
A-1	Finite Element Model of 3 x 3 Center Panel - Flat	A-2
A-2	Finite Element Model of 4 x 3 Center Panel - Flat	A-2
A-3	Finite Element Model of 6 x 3 Center Panel - Flat	A-3
A-4	Finite Element Model of 3 x 3 Center Panel (Radius of Curvature = 30 In.)	A-3
A-5	Finite Element Model of 6 x 3 Center Panel (Radius of Curvature = 60 In.)	A-4
A-6	Finite Element Model of 4 x 3 Center Panel (Radius of Curvature = 90 In.)	A-4
A-7	Static Deformation for Configuration b	A-5

FIGURE		PAGE
8-A	Z-Displacement for Configuration b	A-5
A-9	Normal Stress (y) for Configuration b	A-6
A-10	Normal Stress (x) for Configuration b	A-7
A-11	Static Deformation for Configuration d	A-8
A-12	Z-Displacement for Configuration d	A-8
A-13	Normal Stress (y) for Configuration d \dots	A-9
A-14	Normal Stress (x) for Configuration d	A-10
A-15	Static Deformation for Configuration f	A-11
A-16	Z-Displacement for Configuration f	A-11
A-17	Normal Stress (y) for Configuration f \dots	A-12
A-18	Normal Stress (x) for Configuration f	A-13
A-19	Flat 3 x 3 Finite Element Model for Dynamic Analysis	A-14
A-20	Flat 4 x 3 Finite Element Model for Dynamic Analysis	A14
A-21	Flat 6 x 3 Finite Element Model for Dynamic Analysis	A-15
A-22	Curved (R=30) 3 x 3 Finite Element Model for Dynamic Analysis	A-15
A-23	Curved (R=30) 4 x 3 Finite Element Model for Dynamic Analysis	A-16
A-24	Curved (R=60) 6 x 3 Finite Element Model for Dynamic Analysis	A-16
A-25	First (Fundamental) Harmonic for Panel b (f ₁ = 171 Hz)	A-17
A-26	Second Harmonic for Panel b (f ₂ = 177 Hz)	A17

FIGURE		PAGE
A-27	Third Harmonic for Panel b $(f_3 = 189 \text{ Hz}) \dots$	A-18
A-28	Fourth Harmonic for Panel b $(f_4 = 213 \text{ Hz}) \dots$	A-18
A-29	First (Fundamental) Harmonic for Panel f (f ₁ = 343 Hz)	A-19
A-30	Second Harmonic for Panel f $(f_2 = 463 \text{ Hz}) \dots$	A-19
A-31	Third Harmonic for Panel f ($f_3 = 483 \text{ Hz}$)	A-20
A-32	Fourth Harmonic for Panel f $(f_4 = 536 \text{ Hz}) \dots$	A-20
B~1	Fatigue Test Panels	B-2
B2	Existing Rohr Test Panel Configurations	8-8
B-3	Shaker Test Specimens	B-9
C-1	Microphone Spectrum - Sine	C-2
C-2	Microphone Spectrum - 140 dB Random	C - 3
C-3	Microphone Spectrum - 145 dB Random	C- 4
C-4	Microphone Spectrum - 150 dB Random	C-5
C-5	Microphone Spectrum - 155 dB Random	C-6
C-6	Microphone Spectrum - 160 dB Random	C-7
C-7	Microphone Spectrum - 165 dB Random	C-8
C-8	Strain Spectrum for Panel al	C-9
C-9	Strain Spectrum for Panel al	C-10
C-10	Strain Spectrum for Panel al	C-11
C-11	Strain Spectrum for Panel al	C-12
C-12	Strain Spectrum for Panel al	C-13
C-13	Strain Spectrum for Panel b2	C-14

FIGURE																		PAGE
C-14	Strain	Spectrum	for	Panel	b2													C-15
C-15	Strain	Spectrum	for	Panel	b2													C-16
C-16	Strain	Spectrum	for	Panel	b2			•										C-17
C-17	Strain	Spectrum	for	Panel	b2									•				C-18
C-18	Strain	Spectrum	for	Pane1	d				•				•	•				C-19
C-19	Strain	Spectrum	for	Panel	d								•					C-20
C-20	Strain	Spectrum	for	Panel	d	•			•		•							C-21
C-21	Strain	Spectrum	for	Panel	d	•												C-22
C-22	Strain	Spectrum	for	Pane:	d	•					•							C-23
C-23	Strain	Spectrum	for	Panel	d	•	•	•			•						•	C-24
C-24	Strain	Spectrum	for	Panel	f2		•								•	•	•	C-25
C-25	Strain	Spectrum	for	Pane1	f2	•	•		•				•	•	•			C-26
C-26	Strain	Spectrum	for	Panel	f2		•										•	C-27
C-27	Strain	Spectrum	for	Panel	f2						٠	•		•		•	•	C-28
C-28	Strain	Spectrum	for	Panel	f2		•	•								•	•	C-29
C-29	Strain	Spectrum	for	Panel	f2		•	•						•	٠	•		C-30
C-30	Strain	Spectrum	for	Panel	f2			•	•						•	•		C-31
C-31	Strain	Spectrum	for	Panel	g2	•		•		•	•		•	•	•	•		C-32
C-32	Strain	Spectrum	for	Panel	g2	٠	٠	-		•	-			•	•	•		C-33
C-33	Strain	Spectrum	for	Panel	g2	٠	•	•		•	•							C-34
C-34	Strain	Spectrum	for	Panel	g2	•	•	•		•	•	•	•	•				C-35
C-35	Strain	Spectrum	for	Panel	g2	•	•	•			•	•		•				C-36
C-36	Strain	Spectrum	for	Panel	g2													C-37

F.	IGURE																		PAGE
	C-37	Strain	Spectrum	for	Panel	g2					•	1						•	C-38
	L-38	Strain	Spectrum	for	Panel	h			•		•						•		C-39
	C-39	Strain	Spectrum	for	Panel	h			•						•		•		C-40
	C-40	Strain	Spectrum	for	Pane1	h	•	•						•					C-41
	C-41	Strain	Spectrum	for	Panel	h	•			•		•							C-42
	C-42	Strain	Spectrum	for	Panel	h				•								•	C-43
	C-43	Strain	Spectrum	for	Panel	h							•	•	•	•	•		C44
	C-44	Strain	Spectrum	for	Panel	h		•	•				•		•	•	•		C-45
	C-45	Strain	Spectrum	for	Panel	i										•		•	C-46
	C-46	Strain	Spectrum	for	Pane1	i		•		•	•								C-47
	C-47	Strain	Spectrum	for	Panel	i			•		•				•	•		•	C-48
	C-48	Strain	Spectrum	for	Panel	i	•		•								•		C-49
	C-49	Strain	Spectrum	for	Panel	i			s	•	•				•	•			C-50
	C-50	Strain	Spectrum	for	Panel	i						•		•					C-51
	C-51	Strain	Spectrum	for	Panel	ĭ				•		•							C-52
	C-52	Strain	Spectrum	for	Pane1	j										•			C-53
	C-53	Strain	Spectrum	for	Panel	j				•	•	•			•		•		C-54
	C-54	Strain	Spectrum	for	Panel	j		•	•				•		•	•	•		C-55
	C-55	Strain	Spectrum	for	Panel	j							•		•	•		•	C-56
	C-56	Strain	Spectrum	for	Pane1	j	•		•		•	•		•			•		C-57
	C-57	Strain	Spectrum	for	Pane1	j	•			•						•			C-58
	C-58	Strain	Spectrum	for	Pane1	j	•				•	•	•	•		•			C-59
	C-59	Strain	Spectrum	for	Panel	k1												•	C-60

FIGURE	Pi	AGE
C-60	Strain Spectrum for Panel k1	C-61
C-61	Strain Spectrum for Panel kl	C-62
C-62	Strain Spectrum for Panel kl	C-63
C-63	Strain Spectrum for Panel kl	C-64
C-64	Strain Spectrum for Panel kl	C-65
C-65	Strain Spectrum for Panel 1	C-66
C-66	Strain Spectrum for Panel 1	C-67
C-67	Strain Spectrum for Panel 7	C-68
C-68	Strain Spectrum for Panel 1	C-69
C-69	Strain Spectrum for Panel 1	C-70
C-70	Strain Spectrum for Panel 1	C-71
C-71	Strain Spectrum for Panel 1	C-72
C-72	Strain Spectrum for Panel n	C-73
C-73	Strain Spectrum for Panel n	C-74
C-74	Strain Spectrum for Panel n	C-75
C-75	Strain Spectrum for Panel n	C-76
C-76	Strain Spectrum for Panel n	C-77
C-77	Strain Spectrum for Panel n	C-78
C-78	Strain Spectrum for Panel p	C-79
C-79	Strain Spectrum for Panel p	C-80
C-80	Strain Spectrum for Panel p	C-81
C-81	Strain Spectrum for Panel p	C-82
C-82	Strain Spectrum for Panel p	C-83

FIGURE																			PAGE
C-83	Strain	Spectrum	for	Pane1	q						•	•						•	C-84
C-84	Strain	Spectrum	for	Pane1	q							•					•		C-85
C-85	Strain	Spectrum	for	Panel	q	•					•	•							C-86
C-86	Strain	Spectrum	for	Pane1	q										•	•	•		C-87
C-87	Strain	Spectrum	for	Panel	q						•					•			C-88
C-88	Strain	Spectrum	for	Panel	q			•											C-89
C-89	Strain	Spectrum	for	Panel	r	•													C-90
C-90	Strain	Spectrum	for	Pane1	r			•											C-91
C-91	Strain	Spectrum	for	Pane1	r				•						•		•		C-92
C-92	Strain	Spectrum	for	Panel	r										•	•			C-93
C-93	Strain	Spectrum	for	Pane1	r		•	•							•				C-94
C-94	Strain	Spectrum	for	Panel	r			•			•		•	•					C-95
C-95	Strain	Spectrum	for	Pane1	r			•	•		•		•			•			C-96
C-96	Strain	Spectrum	for	Panel	S		•				•		•			•	•		C-97
C-97	Strain	Spectrum	for	Panel	s						•						•		C-98
C-98	Strain	Spectrum	for	Panel	Ş					•	•	•		•		•	•		C-99
C-99	Strain	Spectrum	for	Pane1	s														C-160
C-100	Strain	Spectrum	for	Panel	s										•	•			C-101
C-101	Strain	Spectrum	for	Panel	S					_						_	_		C-102

LIST OF TABLES

TABLE		PAGE
1	Test Panel Configurations	6
2	Laminate Properties for Shaker Specimen 1 and Panels a, j and r	12
3	Laminate Properties for Shaker Specimens 2, 5 and 6 and Panels b, e, f, g, h, i, k, and m	. 12
4	Laminate Properties for Shaker Specimen 3 and Panel c	13
5	Laminate Properties for Shaker Specimen 4 and Panels d and 1	13
6	Laminate Properties for Shaker Specimen 7 and Panels n, p, q and s	14
7	Effects of Stacking Order and Ply Orientation on Bending Stiffness Matrix	16
8	Effects of Stacking Order on Natural Frequency Factors	17
9	Preliminary Sonic Fatigue Analysis Results	19
10	Static Stress Levels for Zee Stiffened Panels (ksi)	. 32
11	Static Stresses and Bending Strains for Regression	. 34
12	Tabulated Results of Natural Frequency Solutions	42
13	Natural Frequencies of Shaker Test Specimens	44
14	Comparison of Measured and Calculated Frequencies for Shaker Specimen Type 2	. 46
15	Computed and Measured Natural Frequencies	48
16	Shaker Test Results for Adhesive Evaluation	. 66
17	Void and Resin Contents of Skin Laminates	. 66
18	Flatwise Tensile Test Results on Skin Laminates	68

LIST OF TABLES - Continued

TABLE		PAGE
19	Comparative Adhesive Evaluation - Static Results	69
20	Comparative Adhesive Evaluation - Shaker Test Results	69
21	AF-147 Adhesive Processing Evaluation	70
22	Overall RMS Stress Levels for Existing Panels 1, 5 and 4	86
23	Overall RMS Stress Levels for Existing Panel 3, Flat and Curved	87
24	Overall RMS Strains (Microinches/Inch) used in the Development of the Design Method	99
25	Response Strain Comparisons Between Z and J Stiffeners and Between $(0, \pm 45, 90)_S$ and $(0_2, \pm 45)_S$ Ply Orientations	111
26	Comparison of Overall RMS Strain Levels for Bonded and Riveted Panels	12.2
27	Overall RMS Strain Levels (Microinches/Inch) for Panel "d" With Different Edge Conditions	131
28	Comparison of Overall RMS Strains (Microinches/Inch) for Honeycomb and Z Stiffened Panels	133
29	Summary of Analytical and Experimental Results	143
30	Regression Input Data	151
31	Regression Results for Linear Equation	152
32	Table of Residuals for Linear Regression Equation	153
33	Cross-Correlation Matrix for Variables Used in Final Regression Equation	155
34	Regression Analysis Results for Final Regression Equation	156

LIST OF TABLES - Concluded

TABLE		PAGE
35	Table of Residuals for Final Regression Equation	157
36	Table of Residuals for Regression of Miles' Equation	167
37	Table of Residuals for Regression Using Calculated Frequencies and Static Strains	168
3 8	Table of Residuals for Nonlinear Regression	171
39	Regression Analysis Results for	172

SECTION I

Sonic fatique has become a recognizable and persistent structural design problem over the past twenty-five years. Although not usually a catastrophic problem in terms of human lives, it has resulted in structural failures adversely affecting maintenance costs, mission effectivity and often requiring major structural redesigns. Sonic fatique problems have been characterized by a significant degree of inherent unpredictability that has so far denied the structural designer the precise analytical tools that are available in other areas of structural analysis. These limitations have been accompanied by the need for minimum weight designs in increasingly severe and varied acoustic environments. This situation has led to the development and application of semiempirical design techniques based on Miles⁽¹⁾ single degree-of-freedom approach in combination with experimental data from full-scale airplane tests and laboratory sonic fatigue tests. References 2, 3 and 4 have used such techniques to develop design nomographs for various types of structures. References 5 and 6 present much of this work as part of overall sonic fatique design guides.

These existing design methods have been developed for metal structures. However, recent advanced composite materials development has led to a wide-spread aerospace application of nonmetallic structures, in the interests of cost and/or weight savings. The most notable of these materials to date is graphite-epoxy. Although there have been

investigations into the sonic fatigue resistance of graphite structures⁽⁷⁾, there are no sonic fatigue design methods available for these materials that are comparable to those currently available for most metal structures. Consequently, it is difficult for the designer to translate the potential weight savings of graphite structures into a practical reality with the necessary level of assurance against sonic fatigue failures. The primary purpose of the program described in this report was to remedy this by developing a semi-empirical sonic fatigue design method for both flat and curved graphite-epoxy stiffened-skin panels.

The program comprised three phases: analytical, experimental and the development of a design method. The analytical approach consisted of incorporating composite laminate analyses into finite-element computer methods in order to determine the static and dynamic response characteristics of a range of graphite-epoxy stiffened-skin panels. These panels were 3 x 3, 4 x 3 and 6 x 3 arrays, with various laminate thicknesses, stiffener spacings, radii of curvature and ply orientations represented. The experimental phase consisted of fabricating and sonic fatigue testing a range of test panel configurations corresponding to those subjected to analysis. Sonic fatigue testing was carried out in a "progressive-wave tube" with the panels being subjected to random acoustic loading at grazing incidence. The panels were instrumented with strain gauges and flush-mounted microphones, and data taken over a wide range of sound pressure levels. The sonic fatigue test program was augmented by performing shaker tests, with random loading, on sections of skinlaminates in order to develop random fatigue curves.

The design method phase of the program attempts to relate the analytical results and the test data in order to provide a semi-empirical design method. Measured random strains are compared to those calculated from Miles' equation, using the analytically determined static strains and frequencies as inputs. The test results were also compared to values obtained from the AGARD nomographs (5), with density and elastic modulus

values modified to reflect the graphite-epoxy laminates. Finally, "multiple stepwise-regression" analysis techniques were used to develop empirical relationships between the measured strains and frequencies, and various combinations of panel configuration parameters and finite element analysis results. From these regression analyses, a set of design equations was developed and a design nomograph constructed. The design method is presented as a self-contained unit (Section IV.5), allowing it to be utilized independently of the remainder of this report. A worked example is also presented. Figure 1 shows the program phase/task flow diagram.

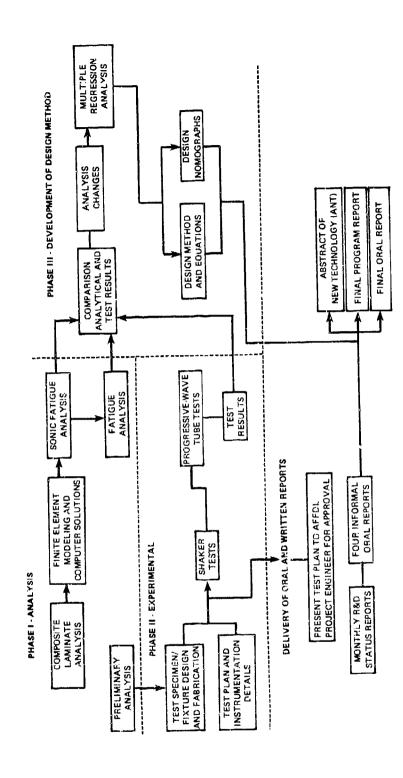


Figure 1. Program Phase/Task Flow Diagram

SECTION II ANALYTICAL

1. INTRODUCTION

This section describes the analytical work performed in support of the program. A description of general sonic fatigue theory is given in Section II.2. The analytical approach consisted of generating a complete set of elastic properties for each composite laminate used in the program; these properties were then used as inputs to both the preliminary analyses and the finite-element solutions. The preliminary analysis consisted of using Miles' equation and Reference 5 to calculate natural frequencies and dynamic stresses for each of the proposed test panel configurations. This was done in order to ensure that their expected response characteristics were compatible with the expected sonic fatigue test envelope. The finite-element analysis consisted of constructing a series of coarse and fine grid finite-element models, and using the NASTRAN computer program to generate a set of natural frequencies and static strains to be used as inputs in determining acoustically induced dynamic strains. An additional set of natural frequencies was generated using equations developed by Lin⁽⁸⁾.

Table 1 lists the panel configurations used in this program. An analytical comparison was also made between Z and J type stiffeners. Figure 2 presents a flow chart of the analytical work.

TABLE 1
TEST PANEL CONFIGURATIONS

Conf	iguration	Number	Skin Laminate		Stringer		Radius of
Numb	and er of Bays	of Panels	No.of Plies	Ply Orientation	Spacing (in.)	Stiffener Type	Curvature (in.)
a	(3 x 3)	2	6	(0, ±45) _s	8	Zee	Flat
b	(3×3)	2	8	(0, ±45,90) _s	8	Zee	Flat
bj	(3×3)	1	8	$(0, \pm 45,90)_{s}$	8	J	Flat
С	(3×3)	2	8	$(0_2, \pm 45)_s$	8	Zee	Flat
сj	(3×3)	1	8	$(0_2, \pm 45)_5$	8	J	Flat
d	(3×3)	1	12	(0, ±45) _{2s}	8	Zee	Flat
e	(3×3)	2	8	Same as (b)	8	Honeycomb	Flat
f	(3×3)	2	8	Same as (b)	8	Zee	30
g	(3×3)	2	8	Same as (b)	8	Zee	60
h	(3×3)	1	8	Same as (b)	8	Zee	90
i	(6 x 3)	1	8	Same as (b)	4	Zee	Flat
j	(6 x 3)	1	8	Same as (b)	4	Zee	90
k	(4×3)	2	8	Same as (b)	6	Zee	Flat
1	(4×3)	1	12	Same as (d)	6	Zee	90
m	(8 x 1)	1	8	Same as (b)	4.5	Zee	Flat
n	(3 x 3)	1	4	(0, 90) _s	8	Zee	Flat
p	(3×3)	1	4	Same as (n)	8	Zee	90
q	(6×3)	1	4	Same as (n)	4	Zee	Flat
r	(6×3)	1	6	Same as (a)	4	Zee	60
S	(4×3)	1	4	Same as (n)	6	Zee	30

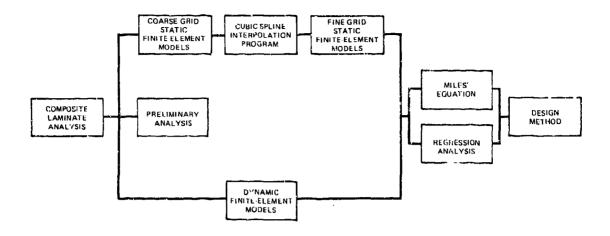


Figure 2. Flow Chart of Analytical Work

2. GENERAL SONIC FATIGUE THEORY

The central problem in sonic fatigue analysis is the calculation of the vibratory stress levels in structural panels subjected to the random acoustic excitation associated with jet engine noise, and then to predict the resulting fatigue life. Since the structural loading is random (Gaussian), the structural response is also random and multimodal in nature. It also follows that the amplitude distribution of the random response must be taken into account in order to determine corresponding fatigue lives.

The complete response of a complex structure to a random noise field can be fully described by an equation developed by Powell⁽⁹⁾. However, Powell's theory is too cumbersome to be used in everyday design and requires input data that is never available in the design stage of a vehicle. In order to simplify the theory to the level of practical use, the following assumptions are made:

- (1) Only one mode of vibration contributes to fatigue failure, and that this mode is the fundamental mode of the individual panel bays. This mode is usually assumed to be the fundamental fully-fixed mode or the fundamental in-phase mode, in which adjacent bays vibrate in-phase with each other, putting the panel stiffeners into bending. Full scale tests on aircraft have shown this assumption to be generally true.
- (2) The vibratory mode shape is identical with the static deflected shape of the panel when subjected to a uniform static pressure.
- (3) The acoustic pressure is exactly in-phase over the who: panel. This assumption is reasonable for jet noise excitation of typically sized aircraft panels. It may not be valid for boundary-layer excitation.
- (4) The power spectral density of the acoustic pressure is constant over the frequency range near the fundamental natural frequency of the panel. It is also assumed that the whole of the energy represented by the acoustic spectrum level at the frequency of the assumed mode of vibration is used to excite that mode.

These assumptions simplify the structural response equation to the form developed by Miles (1):

Mean square stress
$$\sigma^2(t) = \frac{\pi}{4c} - f_n \cdot G(f_n) \sigma_0^2$$
 (1)

where

- is the damping ratio of the fundamental mode,
 often assumed to be typically 0.017 (Reference 5).
- f_n is the natural frequency of the assumed fundamental mode in Hz.
- $G(f_n)$ is the spectral density of the acoustic pressure at the frequency f_n .



 σ_0 is the static pressure at the point of interest due to a unit uniform static pressure over the whole of the panel.

This equation forms the basis of most design oriented sonic fatigue work to date, including the nomographs presented in Reference 5. Many of the simplified sonic fatigue design methods assume fully-fixed panel edges in the calculation of f_n and σ_0 . In this program, these values were to be determined from the finite-element solutions, using actual boundary conditions.

The usual estimating procedure, using Miles' equation is as follows:

- a. Estimate the fundamental natural frequency of the panel, usually assuming fixed edges. Reference 5 provides an appropriate nomograph for this purpose.
 - b. Obtain the acoustic spectrum level at the estimated frequency. NOTE: The spectrum level, $L(f_n)$, is the square root of the spectral density $G(f_n)$. Since the acoustic spectrum level corresponds to the acoustic energy in a 1-Hz bandwidth, acoustic data expressed in other bandwidth form must be converted to the spectrum level using the following relationship

L = Sound Pressure Level - 10 Log₁₀ (
$$f_2$$
- f_1) (2)

where \mathbf{f}_2 and \mathbf{f}_1 are the upper and lower frequency limits, respectively, of the given bandwidth.

c. Calculate σ_0 . Reference 10 gives a simplified equation for the maximum static stress in a fully-fixed panel.

- d. Calculate $\sigma(t)$ using Equation 1, assuming $\zeta = 0.017$.
- e. Determine sonic fatigue life using specially generated random fatigue curves. Reference 6 contains examples of random S-N curves.

NOTE: Random fatigue curves can be developed from conventional cyclic fully-reversed flexural fatigue curves. This is accomplished by applying Miner's $^{(11)}$ cumulative damage law to the Rayleigh distribution function for peak amplitudes in a Gaussian process.

3. COMPOSITE LAMINATE ANALYSIS

Rohr has several computer programs available for analysis of composite laminates. These analytical techniques range from large general purpose programs down to simplified procedures used on the desk computers.

The primary general purpose program developed for laminate property analysis, called COMPOSITE, calculates the laminate elastic and strength properties for a specified laminate layup. The program may also analyze a laminate with up to five different materials in the layup, hence, is useful in determining the properties of hybrid laminates. Options for three failure criteria are also included within the program and can be used to assist in determining laminate failure modes. The laminate analysis can be performed for combinations of in-plane and bending loads.

The COMPOSITE program was developed with several additional features for the analysis of laminate properties. If the laminate fails under the specified load, one program feature will remove the failed plies from the layup and recalculate the laminate elastic and strength properties. This feature is useful in evaluating nonlinearities due to ply failure and determining to what degree the laminate with the failed plies removed can sustain the load. The laminate stiffness matrix, suitable for direct input into the NASTRAN finite-element program, is also computed and is part of the output.

The program can also calculate the buckling coefficients for flat laminate panels. By selecting the options and inputting panel size, the buckling coefficient can be determined and displayed either in tabular or graphical printout. A material data bank is also incorporated into the COMPOSITE program. Material laminate properties are stored within the program and may be called by identification number for a laminate analysis. This feature saves time in setting up the computer deck and provides consistent properties for use on a regular basis. The laminate properties in the data bank may be updated as necessary to reflect current data.

Material property data for all the skin and stiffener laminates were calculated and tabulated based on carpet plots in Reference 12. Rohr has used its "COMPOSITE" computer program and performed laminate property tests to confirm selected data points in Reference 12. Tables 2 through 6 list the laminate properties generated and used as inputs for the finite element analyses. Values shown in parentheses are computer generated values used to check those obtained from Reference 12. Elastic properties were computed for the skin, skin/stiffener attach flange, stiffener web, and the stiffener free flange with unidirectional reinforcement. Modulus values are times 10^6 (1b/in²).

Effect of Stacking Order

One of the advantages of composite materials is the capability to tailor structural properties by dictating the number and orientation of plies. The in-plane strength and elastic properties ($E_{\rm X}$, $E_{\rm y}$, $G_{\rm Xy}$) of the laminate can be readily determined for specified orientation patterns through the use of computer programs or "carpet plots." These procedures are documented in the Air Force Composite Design Guide⁽¹²⁾ and other sources.

The elastic properties are customarily used in the structural finiteelement programs, such as NASTRAN (see Section 11.5).

TABLE 2
LAMINATE PROPERTIES FOR SHAKER SPECIMEN 1 AND PANELS a, j AND r

Laminate	E _y	E _x	G _{yx}	[∨] yx	[∨] xy	G11 E _y 1-"xy 'yx	G22 E _y 1-v _{xy} v _{yx}	G21 = G12 v _{xy} E _y 1-v _{xy} v _{yx}	G33
Skin - (0, + 45) _s	7.5 (7.3)	3.3 (3.3)	3.4 (3.2)	.69 (.69)	.31	9.54	4.2	2.96	3.4 (3.2)
Skin + attached stiffener flange -	4.5	3.1	3.9	.73	.50	7.09	4.88	3.54	3.9
Stiffener, web -	2.4 (2.3)	2.4 (2.3)	4.5 (4.5)	.76 (.76)	.76	5.68	5.68	4.32	4.5 (4.5)
Stiffener, free-flange -	10.2	3.0	2.4	.61	.17	11.38	3. 35	1.93	2.4

NOTE: Modulus values are in units of 10^6 lb/in. 2 .

TABLE 3

LAMINATE PROPERTIES FOR SHAKER SPECIMENS 2, 5 AND 6

AND PANELS b, e, f, g, h, i, k AND m

						G11 E _v	G22 E _v	G21 = G12 v _{xy} E _y	G33
Laminate	Ey	Ex	G yx	v _{yx}	νху	1-v _{xy} v _{yx}	1-v _{xy} v _{yx}	T-V _{XY} V _{yX}	Gyx
Skin - (0, ± 45, 90) _s	6.7 (6.8)	6.7 (6.8)	2.6 (2.6)	.31 (.31)	.31	7.41	7.41	2.3	2.6 (2.6)
Skin + attached stiffener flange -	4.75	4.75	3.6	.49	.49	6.25	6.25	3.06	3.6
Stiffener, web -	2.4 (2.3)	2.4 (2.3)	4.5. (4.5)	.76 (.76)	.76	5.63	5.68	4.32	4.5 (4.5)
Stiffener, free-flange -	9.3	:.2	2.7	. 64	.21	10.74	3.7	2.26	2.7

NOTE: Modulus values are in units of 10⁶ lb/in.².

12

TABLE 4

LAMINATE PROPERTIES FOR SHAKER SPECIMEN 3 AND PANEL C

Laminate	Ey	Ex	G _{yx}	v _{yx}	ху	E _y	622 E _y 1-0 _{xy} 0 _{yx}	G21 = G12 Vxy Ey 1-Vxy Vyx	G33
Skin - (0 ₂ , ± 45) _s	9.7 (9.8)	3.2 (3.2)	2.6 (2.6)	.63 (.63)	.21	11.18	3.69	2.35	2.6 (2.6)
Skin + atwached stiffener flange -	6.0	3.3	3.6	.71	. 39	8.3	4.56	3.24	3.6
Stiffener, web -	2.4 (2.3)	2.4 (2.3)	4.5 (4.5)	.76 (.76)	.76	5.68	5.68	4.32	4.5 (4.5)
Stiffener, free-flange -	9.3	3.2	2.7	.64	. 21	10.74	3.7	2.26	2.7

NOTE: Modulus values are in units of 10^6 lb/in.².

TABLE 5

LAMINATE PROPERTIES FOR SHAKER SPECIMEN 4 AND PANELS d AND 1

Laminate	Ey	E _X	[©] yx	уyx	^v xy	611 E _y 1-v _{xy} v _{yx}	G22	$G21 = G12$ $v_{xy} = F_y$ $1 - v_{xy} = v_{yx}$	633 ^G yx
Skin - (0, <u>+</u> 45) _{2s}	7.5	3.3	3.4	.69	.31	9.54	4.2	2.96	3.4
Skin + attached stiffener flange -	4.5	3.1	3.9	. 73	.5	7.09	4.88	3.54	3.9
Stiffener, web -	2.4	2.4	4.5	.76	.76	5.68	5.68	4.32	4.5
Stiffener, free-flange -	6.2	3.3	3.5	.73	. 39	8.67	4.61	3.38	3.5

NOTE: Modulus values are in units of 10⁶ lb/in.².

TABLE 6 LAMINATE PROPERTIES FOR SHAKER SPECIMEN 7 AND PANELS $n,\,p,\,q$ AND α

						GT E _y	G22 E _y	G21 = G12 v _{xy} E _y	633
Laminate	Ey	E×	G yx	Vyx	^ν xy	1-ν _{xy} ν _{yx}	Y-Vxy Vyx	1-v _{xy} v _{yx}	G yx
Skin - (0, 90) _s	9.4 (9.4)	9.4	.65 (.65)	.05 (.04)	. 05	9.42	9.42	.47	.65 (.65)
Skin + attached stiffener flange -	4.8	4.8	3.25	.4	. 4	5.71	5.71	2.29	3,25
Stiffener, web -	2.4 (2.3)	2.4 (2.3)	4.5. (4.5)	.76 (.76)	. 76	5.68	5.68	4.32	4.5
Stiffener, free-flange -	10.2	3.0	2.4	. 61	.17	11.38	3.35	1.93	2.4

NOTE: Modulus values are in units of 10^6 ib/in.².

However, for this investigation where composite structures are exposed to a sonic environment, additional composite properties are desired. A laminated structure subjected to a bending load whether applied by a sonic or structural source requires the use of the inertia or bending stiffness properties. For laminates, the bending stiffness is defined by the "D $_{ij}$ " matrix. The D $_{ij}$ matrix is computed from the individual ply properties transformed from the specified orientation to the desired stiffness direction. The ply location from the center of the laminate is also taken into consideration. The D $_{ij}$ matrix is therefore written in short notation as:

$$D_{ij} = \frac{1}{3} \sum_{k=1}^{n} (\overline{Q}_{ij})_{k} (h_{k}^{3} - h_{k-1}^{3})$$
 (3)

The $\overline{\mathbb{Q}}_{i,j}$ matrix is the in-plane stiffness of each ply and h_K , h_{K-1} provides the geometric location. The summation provides the bending stiffness of

the laminate. The position of the ply in the laminate therefore will dictate the stiffness.

The effect of ply position or "stacking order" on the laminate stiffness, (D_{ij}) , can be determined by using the COMPOSITE computer program. The D_{ij} matrix results for different ply stacking orders are shown in Table 7. In the table, the D_{11} stiffness is in the laminate 0 degree direction, the d_{12} is the Poisson effect, D_{22} is the laminate 90° stiffness and D_{66} is the in-plane shear stiffness. Even the quasi-isotropic layup $(^{\pm}$ 45°/90°/0°)_{2s} has different values in the laminate orthogonal directions.

The variability of the D_{ij} factors indicates that stacking order has an effect upon the performance of composite panels subjected to an acoustic environment. As an example of the stacking order effect, the natural frequency of simply supported composite plate is of the form

$$W = \frac{\pi}{\rho_1} K \tag{4}$$

abana Dan andersea

where K =
$$D_{11} \left(\frac{m}{a}\right)^{2} + 2 \left(D_{12} + 2 D_{66}\right) \left(\frac{mn}{ab}\right)^{2} + D_{22} \left(\frac{n}{b}\right)^{4}$$
 and P_{1} = mass density.

Since the stacking order affects only the factor "K", its value was tabulated for various laminate layups in Table 8. For a sixteen ply laminate, the stiffness factor has a 12 percent variation depending upon the stacking order.

Complications arose in trying to quantify the effects of stacking order on panel response. This is discussed in Paragraph II.5.a.

TABLE 7

EFFECTS OF STACKING ORDER AND PLY ORIENTATION ON BENDING STIFFNESS MATRIX

LAMINATE "D_{ij}" MATRIX

GR/EP 3501/AS TYPE

 $E_1 = 17 \times 10^6$ $E_2 = 1.7 \times 10^6$ $G = .65 \times 10^6$

Orientation	No. Plies	ווס	D ₂₂	012	D ₆₆
(±45/90 ₂) _{2s}	16	246.01	518.74	171.32	187.87
(±45/0 ₂) _{2s}	16	518.74	246.01	171.32	187.87
(±45/90/0) _{2s}	16	351.7	413.06	171.32	187.87
(±45/0 ₂) ₄	16	549.49	235.85	161.03	177.58
(n/90/±45) _s	8	66.407	40.48	5.051	6.80
(0/90/±45) _{3s}	24	1793.1	1093.0	136.4	183.6
(±45) _{8s}	16	265.17	265.17	202.78	216.76
(0 ₂ /±45 ₈) _s	20	1046.3	343.28	219.18	246.5

$$D_{16} = D_{26} = 0$$

$$D_{ij} = \frac{1}{3} \sum_{K=1}^{n} (\overline{Q}_{ij})_{K} (h_{K}^{3} - h_{K-1}^{3})$$

Where $\overline{0}_{ij}$ is the transformed ply property and h_K , h_{K-1} is the distance of the ply surfaces from the reference.

TABLE 8
EFFECTS OF STACKING ORDER ON NATURAL FREQUENCY FACTORS

Layup	К	Number of Plies
(±45/90 ₂ ; _{2s}	.4514	16
(±45/0 ₂) _{2s}	.5072	16
(±45/90/0) _{2s}	.4738	16
(±45/0 ₂) ₄	.5075	16
(0/90/±45) _s	.149	8
(0/90/±45) _{3s}	.7745	24
(±45) _{8s}	.4643	16
(0 ₂ /±45 ₈) _s	.6531	20

(1) Where
$$\omega = \left(\frac{\pi}{\rho_1}\right)^2 K$$

4. PRELIMINARY SONIC FATIGUE ANALYSIS

Preliminary sonic fatigue analyses were performed in support of the design of the sonic fatigue test panels, given in Table 1. These analyses were made to ensure that the application of these panels in acoustic environments appropriately spanned the full rance of aircraft application. It was also necessary to ensure that the sonic fatigue resistance of the test pane's was within the available progressive-wave tube test envelope. It is important in a sonic fatique test program to obtain a good spread of response characteristics, and to obtain some sonic fatigue failures out in the 10^6 to 10^7 cycle range, without having too many panels fail either too quickly or not at all. The AGARD $^{(5)}$ sonic fatigue design nomographs were used in this analysis, with the results being modified to take account or the elastic modulus and density values for the appropriate skin laminates. The results are shown in Table 9. A pre-test evaluation of the progressive-wave tube indicated that endurance testing would be best carried out in the 160 to 165 dB overall sound pressure level range. corresponding to acoustic spectrum levels in the 130 to 150 dB/Hz range. The results show a good spread in both predicted frequencies and rms stresses. They also show that almost all of the panels could be expected to fail at an acoustic spectrum level of 150 dB/Hz.

5. FINITE ELEMENT SOLUTIONS

The general sonic fatigue theory described in Section 11.2 utilizes as inputs the static stresses or strains due to a uniform unit pressure load and the natural frequency of the fundamental in-phase stringer-bending mode. These stress and frequency inputs were determined for each of the panel configurations given in Table 1, using a variety of finite-element models in conjunction with the NASTRAN computer program. NASTRAN is a general purpose finite-element digital computer program especially suited for the analysis of large complex structures. Its ability to handle a large range of problems has resulted in its adoption throughout the aerospace industry. This wide acceptance and versatility are the primary reasons for the selection of NASTRAN as the fundamental analytical tool of this program. The uniform pressure load condition is widely used in sonic

TABLE 9
PRELIMINARY SONIC FATIGUE ANALYSIS RESULTS

Panel Config-	Acoustic Spectrum Level	Stringer Spacing	Skin Thickness	Radius of Curvature	Fully- Fixed Frequency	RMS Stress (1b/in ²)	Laminate Ftu
uration a	dB/Hz 130 140	b (in) 8	t (in) ,033	R (in) Flat	(Hz) 160	20,900 66,200	(1b/in ²) 70,000
b&e	150 130 140 150	8	.044	Flat	202	209,000 12,800 40,400 128,000	64,000
С	130 140 150	8	.044	Flat	247	14,200 44,800 142,000	96,000
d	130 140 150	8	.066	Flat	308	7,400 23,400 74,000	70,000
f	130 140 150	8	.044	30	825	1,700 5,400 17,000	64,000
g	130 140 150	8	.044	60	510	3,250 11,000 32,500	64,000
h	130 140 150	8	.044	90	.375	4,750 17,500 47,500	64,000
i	130 140 150	4	.044	Flat	674	6,600 20,900 66,000	64,000
j 	130 140 150	4	.044	90	824	6,000 18,000 60,000	64,000
k 	130 140 150	6	.044	Flat	312	10,500 31,700 100,000	64,000
l 	130 140 150	6	.066	90	631	4,100 13,000 41,000	70,000
n 	130 140 150	8	.022	Flat	120	38,400 121,000 384,000	88,000
μ 	130 140 150	8	.022	90	377	7,800 23,000 78,000	88,000
q 	130 140 150	4	.022	Flat	409	19,800 62,600 198,000	88,000
Γ	130 140 150	4	.033	60	782	6,900 22,000 69,000	70,000
s	130 140 150	6	.022	30	828	3,500 11,000 35,000	88,000

Note: $p = 0.055 \text{ lb/in}^3$

fatigue work since its resulting displacement field closely resembles the fundamental in-phase mode shape.

The accuracy of finite-element solutions is highly dependent upon the element size and the applied boundary conditions. Consequently, considerable effort was put forth in the determination of each. This involved many iterations before arriving at optimum model configurations. Due to the nature of the test panel designs, i.e., relatively massive stiffeners interfacing with thin plates, some difficulty was experienced in generating the in-phase mode from the dynamic models. Eventually, well defined stringer-bending in phase modes were obtained for all but two of the panel configurations (the two 30-inch curved panels, f and s, being the exceptions). However, the mode shapes for the stiffer panels exhibited excessive substructure deflections, resulting in low frequency estimates. This conditioning problem was successfully overcome in the static analysis.

Finite element models were also constructed for the shaker specimens described in Section III.4. Computed natural frequencies gave good agreement with the shaker test results, and are given in Paragraph II.5.d.

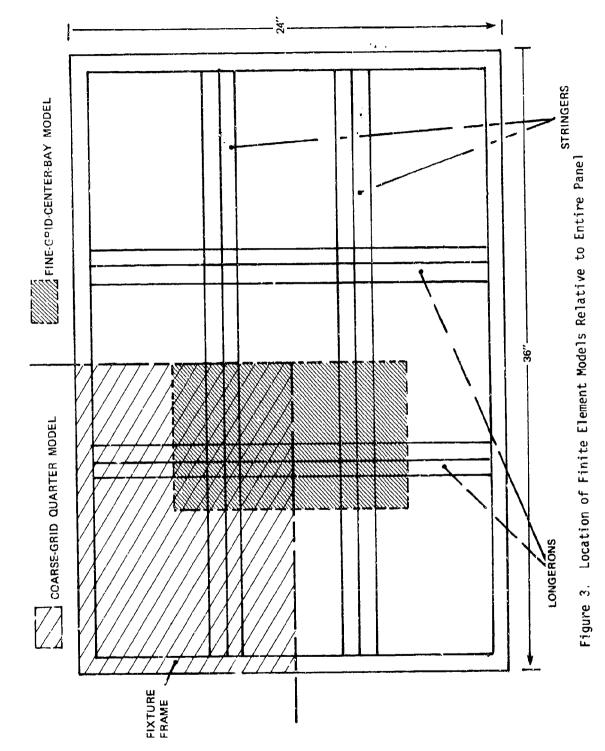
a. Analytical Approach - In order to provide static and dynamic analyses in sufficient detail to support the development of a semi-empirical sonic fatigue design method, finite-element models were constructed to represent each of the panel configurations shown in Table 1. Initially it was believed that relatively coarse grid models would be sufficient for the dynamic analysis. Consequently, models comprising 2-inch plate elements, with bar elements representing the stringers and frames, were constructed. These models were used to generate a set of static and dynamic solutions. Although primarily intended as dynamic models, they also provided a good starting point for the static analysis. The material properties used in these and subsequent models were determined from the Rohr composite laminate properties program "COMPOSITE," described in Section II.3.



The dynamic results from the 2-inch grid models appeared to be satisfactory for the 3 x 3 panel arrays; however, it was decided to use a finer grid for the panels with smaller bays (4 x 3 and 6 x 3 panel arrays). Models comprising 1-inch plate elements were therefore constructed and a second set of results was generated. The mode shapes and natural frequencies generated by the 1-inch and the 2-inch models were in close agreement. However, some difficulties were encountered with both sets of models in identifying the desired in-phase stringer-bending mode. Further modeling refinements did not result in significant improvements in the dynamic solutions, consequently the 1-inch coarse grid quarter models were used for the dynamic analyses.

As expected, neither the 2-inch nor the 1-inch coarse grid models provided the necessary detail for the static analysis, particularly in high stress gradient areas. A set of 1/2-inch models was constructed and another set of static solutions obtained. Accuracy at the skin-stiffener interfaces was still considered inadequate. All of these coarse grid models represented a quarter of each panel array, as shown in Figure 3.

It was then decided to represent the center bay portion of each panel with a fine grid model, also shown in Figure 3. Because of the lack of symmetry of zee stiffeners, these fine-grid models included the stringers on both of the long sides. The maximum stress in stiffened skin panels occurs at the center of, and normal to, the longer edges. Detailed accuracy is therefore of great importance in these areas. This was accomplished by representing the zee stiffeners as a series of plates (thereby creating three-dimensional models) rather than as simple bar elements. In addition, the grid size was optimized by computing the bending moment distributions from three specially constructed small plate (6 in. by 4 in.) models employing, in turn, 1-inch, 1/2-inch and 1/4-inch grid sizes. The results were then compared with hand calculations using Timoshenko (13). Figure 4 shows the results of the comparison. It can be seen that 1/2-inch grid size provides accurate results at the panel center. Even the 1-inch grid has reasonable accuracy at the center of the



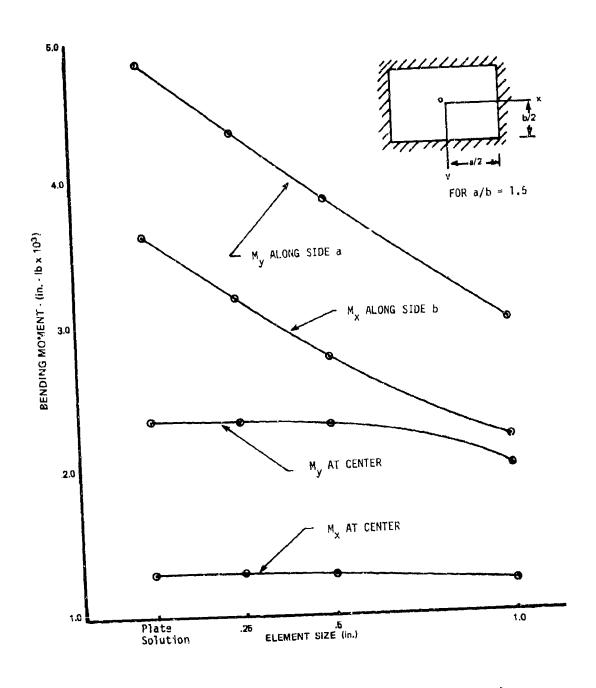


Figure 4. Comparison of Bending Moment Distributions Using Different Size Elements and Plate Solution Taken from Timoshenko (13)

pane!. However, the gradient at the panel edges requires a very fine grid in order to achieve reasonable accuracy. A compromise between structural accuracy and practical constraints, such as computer size limitations, resulted in 1/4-inch elements being selected to represent the skinstiffener interface regions. This results in an 11-14 percent underestimate in computed bending moments at the panel edges, compared to the values calculated using Timoshenko. Although a maximum grid size of 0.875-inch was used in some non-critical skin areas, all strains used in the development of the design method (Section IV) were taken from 1/4-inch elements. There are practical limitations in combining radically different element sizes within one model. In order to limit the number of grid points to within manageable proportions, the smaller elements (1/4-inch) must have higher aspect ratios than the larger elements (1/2-inch). Unfortunately, analytical accuracy deteriorates with increased aspect ratio (above unity). An element aspect ratio of 3:1 is considered the maximum for reasonable accuracy.

In order to obtain boundary conditions for the fine grid center bay models, a cubic-spline computer program was written to interpolate the displacement and rotation fields along the interfaces with the 2-inch coarse grid quarter models. This method assumes the deflected shape which minimizes potential (strain) energy. Conventional "beam theory" shows this energy to be proportional to the integral, with respect to the arc length, of the square of the curvature of the spline. The accuracy of this approach was verified using the previous 1/2-inch grid model. Displacement data at 2-inch intervals on the 1/2-inch model were interpolated to obtain intermediate displacements at 1/2-inch intervals. These interpolated displacements were within 1 percent of the actual results from the 1/2-inch model. Initially it was thought that the finegrid boundary conditions could be adequately described using displacement data only. However, when this was attempted with the 1/2-inch model, it was found that resultant stress and displacement fields were not sufficiently accurate. Consequently, it was decided to also include the interpolated values of the two components of rotation along the boundary.

This improved the accuracy of the interpolated stresses to within 2 percent of the 1/2-inch model results.

During the subsequent static analysis of the curved panels, it was determined that additional in-plane displacements were needed in order to fully define the boundary conditions. Flat panels, under normal loading, do not undergo axial displacements and all the load is taken in pure bending. However curved panels, under normal loading, experience both hoop and bending stresses, requiring the application of in-plane displacement boundary conditions. A further refinement was evaluated, which was to apply rotation and displacement boundary conditions to the out-of-plane zee stiffener elements, in addition to the skin elements. The effects of this refinement on one flat and one curved panel was less than 10 percent and have not been included in the results in Paragraph II.5.c.

A comparison was made in both the static and dynamic analyses, between Z and J stiffener designs. A sample calculation using one of the dynamic quarter models showed no significant differences in natural frequencies nor mode shapes between the Z and the J stiffened panels. No further dynamic analysis of the J stiffeners was performed. Significant differences between the Z and the J stiffened panels did occur in the static analysis results, and are given in Paragraph II.5.c.

b. Effects of Skin Ply Stacking Order - Attempts were made to evaluate the significance of these effects on the computed static stresses. The previous analyses utilized Rohr's "COMPOSITE" computer program to generate laminate elastic properties, which are not dependent upon stacking order, leaving the bending stiffness (EI) to be computed by NASTRAN in the usual manner.

Because laminated composite materials exhibit orthotropic properties, it is necessary to input the total plate constitutive equation

$$\begin{bmatrix} N \\ M \end{bmatrix} = \begin{bmatrix} A & B \\ B & D \end{bmatrix} \begin{bmatrix} \varepsilon \\ \overline{k} \end{bmatrix}$$
 (5)

in matrix form to fully describe the behavior of a general orthotropic plate. Where N and M are the applied loads and ε and k are the resultant strains. The A and D matrices define the extensional and bending stiffnesses respectively. The "B" matrix defines the bending-extensional coupling for the laminate. From a practical standpoint this term is nearly always zero, because ply orientation and stacking orders are selected to give a "balanced symmetric" layup which eliminates bending-extensional coupling. The bending and extensional constitutive equations can therefore be shown below:

$$[N] = [A] [\varepsilon] \text{ and } [M] = [D] [k]$$
(6)

For the isotropic extensional case, NASTRAN computes the constitutive equations

$$A_{11} = A_{22} = (\frac{E}{1-v^2}) t$$
 (7)

$$A_{12} = \nu A_{11} \tag{8}$$

$$A_{66} = (\frac{E}{2(1+v)}) t$$
 (9)

from the data supplied on the PQUAD quadrilateral plate element card (thickness, t) and on the MAT1 material card (E and ν). The remaining matrix terms are zero.

If an orthotropic material is to be analyzed for axial loading, the MAT2 card is utilized to input the material property matrix "G" terms

$$(\frac{E_x}{(1-v_{xy}, v_{yx})}, \frac{E_y}{1-v_{xy}, v_{yx}}, \text{ etc.}).$$
 (10)

The complete constitutive equations are obtained by the product of this matrix and the material thickness which is again input on the appropriate PQUAD card.

For the isotropic bending case, NASTRAN computes the constitutive equations

$$D_{11} = D_{22} = \frac{E t^3}{12(1-v^2)}$$
 (11)

$$D_{12} = \nu D_{11} = D_{21} \tag{12}$$

$$D_{66} = \frac{E t^3}{24(1+v)}$$
 (13)

from the same data supplied for the extensional case. If no additional information is supplied, NASTRAN will also compute the orthotropic bending constitutive equations in the same manner (multiplying the "G" matrix terms by the appropriate $t^3/12$ term).

However, the true bending stiffness of an orthotropic laminate is a function of the laminate stacking order in addition to the laminate elastic properties.

The constitutive equation for bending (the "D" matrix) can be input into NASTRAN using the MAT2 card. In this case the "D" matrix must be factored by the $t^3/12$ term because NASTRAN is programmed to multiply the "G" matrix by the $t^3/12$ term.

The Cosmic version of NASTRAN does not have the capability to accept the complete orthotropic constitutive equation matrix for plate elements.

In many cases, where loading is primarily axial or the laminate has a large number of plies, the inaccuracies introduced by using the extensional "G" matrix to compute the bending constitutive equations is small and this approach has been used with reasonable accuracy. Conversely, if the panel has a small number of plies and the loading is primarily in bending, then the bending "G" matrix can be used.

The Rohr laminate analysis program COMPOSITE outputs the extensional "G" matrix directly in addition to the "A," "B" and "D" matrices.

In the case of the structural analysis of the sonic fatigue panels, an attempt has been made to input both the extensional and bending constitutive equation matrices. This was done using the "PQUAD 1" general quadrilateral element property card which is primarily utilized for the analysis of sandwich structures. This property card allows for separate input of membrane (extensional), bending and shear properties.

The extensional information required is the material identification and plate thickness. The extensional constitutive matrix can be input by identifying a "MAT2" material property card containing the appropriate "G" matrix.

The input data defining the bending properties are the material identification and the area moment of inertia per unit width (I) of the quadrilateral element. NASTRAN is programmed to calculate the isotropic constitutive bending equations using the input values of I ($t^3/12$), the elastic constants and the appropriate numerical values. NASTRAN is also programmed to utilize the "I" value in the computation of the bending stresses.

To obtain the orthotropic constitutive bending equations, the bending material was defined on a "MAT2" material property card containing the "D" matrix factored by 1/I ($12/t^3$). The complete "D" matrix was then obtained internally in NASTRAN using the computational procedure defined above. The results of this investigation were inconclusive, requiring further study beyond the schedule of this program. No correlation was established between the stacking order and the effect on computed stresses.

c. Static Analysis - The analysis of the sonic fatigue panel configurations in this program required the construction of detailed finite-element models to accurately predict the panel responses to a uniform 1 lb/in² applied pressure load. The iterations involved in arriving at optimum model designs are discussed in Paragraph II.5.a. The panel configurations are given in Table 1, and the location of the finite-element models relative to the entire panel arrays is given in Figure 2.

Although there are 20 panel configurations in Table 1, the final analysis results in this section are limited to 18 configurations. Panels "e" and "m" were eliminated prior to the final computer runs. Because of the many iterations involved in obtaining the final analytical results and the consequent effects that this had on program schedule, it became necessary to limit the final analysis to those panels to be used in the development of the design method. Panel "e" was intended to evaluate honeycomb beam stiffeners and panel "m" was primarily intended as a data link to sonic fatigue test panels, comprising a single row of bays, typically used in previous sonic fatigue programs. This program utilizes panels comprising three rows of bays. Geometric similarities allowed the remaining 16 configurations to be represented by 10 fine grid center bay models. Figures A-1 through A-6 in Appendix A show six of these models. The three-dimensional modeling of the stiffeners is clearly seen, as is the smaller grid spacing at the panel edges and along the center line of the center bay.

The 2-inch coarse grid models were used to generate boundary conditions for the fine grid center bay model, utilizing the cubic spline program described in Paragraph II.5.a. The unit uniform pressure load was then applied to the fine grid models, generating a series of stress distributions. Although the subsequent design method would be based on maximum edge stresses and/or center bay stresses, it is desirable to know the displacement patterns and stress distributions over the entire surface. This was accomplished by plotting isopleths of the desired quantities. These are shown in Figures A-7 through A-18 in Appendix A. Static deformations, out-of-plane displacements (Z direction) and stresses in the "y" and "x" directions are given for panels "b," "d" and "f." The plots are consistent with expected structural behavior and show the stiffeners to provide good edge restraint. The stress contours show the high gradients that exist at the skin-stringer interfaces, demonstrating the need for accurate modeling in these areas. These plots were generated prior to some model corrections and the introduction of in-plane boundary conditions (see Paragraph II.5.a); consequently, the stress magnitudes on the plots do not all correspond to the tablulated stresses shown later in this section.

In determining stress magnitudes at critical locations, it was noticed that the curved panels exhibited large stress differences on opposite faces of the skin elements, indicative of significant axial stresses. This is logical following the application of the in-plane boundary conditions to the skin elements, described in Paragraph II.5.a. Figure 5 shows the locations of the stresses given in Table 10. Stresses on both skin faces are given for all the curved panels. They are also given for the flat panels at locations 5 and 6. Location 5 is at the center of the center bay and location 6 is the maximum edge stress. The "y" direction is across the narrow span and is therefore the critical direction. The results show the flat panels to be in pure bending and also show the extent of axial stresses occurring on the curved panels. However, during sonic fatigue testing, back-to-back strain gauges gave equal and opposite readings, indicative of pure bending on both curved and flat panels.

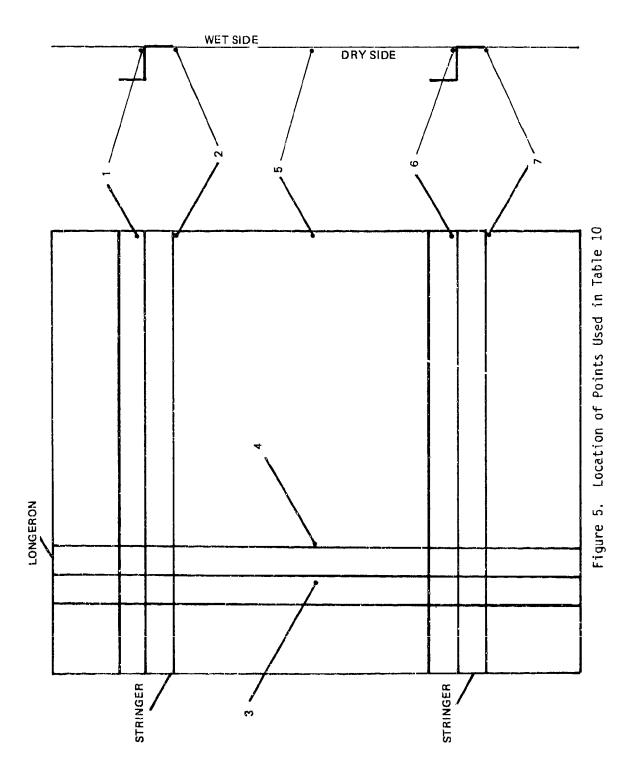


TABLE 10 STATIC STRESS LEVELS FOR ZEE STIFFENED PANELS (KSI)

t 7	2	-20.81	-12.18	-11.60	-4.85	-0.48 -0.89	-0.10 -2.33	3.24	-1.39	-0.71 -1.53	-5.81	0.09	-79.79	-1. 4 0 -5.32	-8.13	-1.11	-0.68 -2.90
Point	×	-5.93	-3.03	25.1-	-1.64	-0.2 4 -0.36	-0.17	0.97	-0.17	-0.47	-1.42	-0.16 -0.5!	-1.58	-9.14 -0.38	07.50	-0.46	-0.06
9	مح	-26.63 26.20	-14.35 14.02	-16.41 16.03	-7.32 7.05	-0. 4 9 -0.87	0.49 -2.91	4.34 -6.90	-3.78 3.81	0.49	-8.71 8.68	1.07	-58.54 57.13	1.16 -8.80	-13.54 13.58	0.21 -2.92	-0.55
Point	×	-7.72 8.65	-3.76 4.99	-2.92 3.86	-i.76 2.60	-0.25	-0.02	1.27	-0.84	-0.19 -1.13	-2.34	0.08 -0.97	-0.83 4.90	-0.07	0.09	-0.10 -1.06	-0.09
2	3y	10.90 -10.68	5.87	6.10 -6.00	2.54	-0.76 -0.58	-1.97 -0.49	-3.49	1.03	-1.71 -9.57	3.28	-1.45 -0.02	26.05 -26.45	-6.53 -1.07	5.19 -5.06	-2.02 -0.74	-1.69
Peint	υ ×	4.49	3.52	1.85	1.29	-7.36 -0.30	-C 73 -0.35	-1.34	0.50 -0.14	-0.85	8.5.7	-6.71	9.50	-1.01	0.55	-0.80	-9.18 -0.13
4	°y	-3.35	-1.18	-0.95	-9.47	-0.46	-0.81 -0.29	1.09	0.01	-1.04 -1.68	-0.61	-0.53 -0.84	0.72	-1.09 -1.12	0.43	-1.15 -1.27	-0.78 -0.71
Foint	x ک	-6.18	-6.00	-2.79	-1.33	-0.14	0.60	3.06	-0.52	-9.27	-2.74	-0.10	-27.68	4.66	-3.83	-0.32	0.46
3	رکی	-6.97	-3.00	-3.04	-2.29	-0.32	0.02 -0.96	2.31	-0.80	-0.70	-1.89	-0.27	-0.51	-0.45	-0.43	-0.75	-0.25 -0.38
Point	×	-11.12	-11.80	-5.91	-3.98	0.04	1.19	7.33	-2.68	0.55	-6.57	0.27 -1.09	-43.52	3.30	-9.09	9.12	1.60
: 2	کِّ	-16.07	-8.81	-9.92	-4.43	-0.54	-6.11	2.15	-1.53	-5.51	-4.54	0.03	-41.84	-0.15	-5.22	-1.05	-1.88 -1.80
Point	υ×	-4.52	-2.23	-1.68	-0.98	-0.27	-0.21 -0.88	-1.46	-C. 26	-0.52 -0.80	-1.15	-5.22	-1.10	-0.28	0.26	-0.50	-0.12 -0.16
t 1	کی	-26.31	-14.35	-17.18	-8.13	-0.49 -0.86	6.36 -2.72	4.54 -6.39	-3.76	0.28	-8.40	0.97	-60.77	-6.55 -7.11	-13.37	-0.23	-0.85 -1.81
Point		28.7-	-3.98	-3.23	-2.15	-0.25	-0.04	1.38	-0.89	-0.27	-2.33	-1.01	-1.89	-0.042	-0.17	-0.25	-3.10 -0.15
	Panel	a gry	r Dry	c Wet	a Syv	f Met	9 set	y Ket Ory	i Wet	J. D. E. C.	* C.	1 wet Dry	n Wet	p Wet	9 West Dry	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	s Wet Dry

Consequently, it was decided to separate out the bending and axial stress components in the analytical results, and to use only the bending stress component in the development of the design method. Table 11 lists the results. Since the design method will utilize strain values rather than stress values, the corresponding bending strains are also shown in Table 11.

In order to provide a direct experimental comparison to the analytical static stresses, a static test was performed on panel "d." The panel was mounted in the same fixture that was used during sonic fatigue testing and that was also used to generate boundary conditions for the coarse grid models. A uniform pressure loading was incrementally applied, from 1 to 7-1b/in² using an air bag. Strains were measured at each load increment using strain gauges. Back-to-back gauges were used at the panel center to measure axial strains in addition to bending strains. The strain response appeared to be nonlinear, with stresses increasing approximately 50 percent for a doubling of load. However, the back-to-back strain gauges gave readings within 2 percent of each other, indicating pure bending. It had been anticipated that any nonlinearities in structural response would show up as membrane (axial) stresses. No explanation is offered for this occurrence, and no evidence of nonlinear response occurred during sonic fatigue testing. Because of the nonlinear response, the comparison with the analytical results varied depending upon which load magnitude was used. At 7 lb/in² the center bay stresses were within 20 percent of the analytical value. The higher the load the better the comparison. Figure 6 compares the analytical results with the one 1 lb/in² and 7 lb/in² test values. Although the results from the 7 lb/in² load correspond more closely to the analytical results at the panel center, than do the 1 lb/in² results; the reverse is true at the panel edges. Another puzzling aspect of this static test was that the biaxial strain relationship at the panel center was markedly different during the static test from both the analytical results and from the sonic fatique test results. In the static test, the strains in the long direction were very small (10 percent) compared to the strains in the short direction.

TABLE 11 STATIC STRESSES AND BENDING STRAINS FOR REGRESSION

Elastic	Center	Stress	(ksi)		Edge	Stress (ksi)	(ksi)	:
Modulus E (1n6 14/3n 2)	Wet	Bry	Bending Stress	Bending Strain	¥et "	Dry	Bending Stress	Bending Strain (uin./in.)
	3	2			3	,		
7.5	+10.9	-10.68	10.79	1,439	-26.63	+26.2	-26.415	3,522
6.7	+ 5.87	- 5.69	5.78	863	-14.35	+14.02	-14.185	2,117
7.5	+ 2.54	- 2.36	2.45	327	- 7.32	+ 7.05	- 7.185	958
6.7	92.0 -	- 0.58	09	13	- 0.49	- 0.87	6[.	28
2.9	76.1 -	- 0.49	74	110	+ 0.49	- 2.91	1.7	254
6.7	- 3.49	+ 0.69	-2.09	312	+ 4.34	6.9 -	29.5	839
6.7	+ 1.03	- 0.92	.975	146	- 3.78	+ 3.81	-3.795	999
7.5	- 1.71	- 0.57	57	9/	+ 0.49	- 2.69	1.59	212
6.7	+ 3.28	- 3.15	3.215	480	- 8.71	+ 8.68	-8.695	1,298
7.5	- 1.46	- 0.02	72	96	+ 1.07	- 2.45	1.76	235
9.4	+26.05	-26.45	26.25	2,793	-58.54	+57.13	-57.835	6,153
9.4	- 6.53	- 1.07	-2.73	250	+ 1.16	8.8	4.98	530
9.4	+ 5.19	- 5.06	5.125	545	-13.54	+13.58	-13.56	1,443
7.5	- 2.02	- 0.74	64	85	+ 0.21	- 2.92	1.565	506
9.4	69.1 -	- 0.97	36	38	- 0.55	- 2.11	.78	83

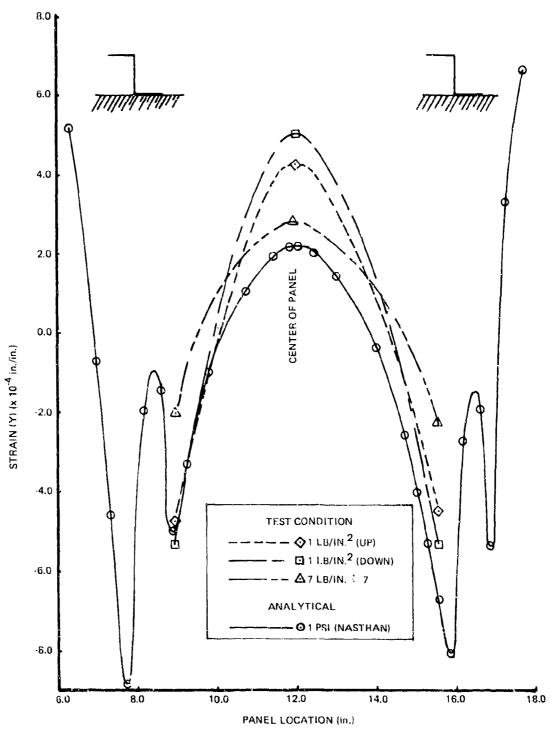


Figure 6. Comparison of Test and Analytical Static Strain (y)
Distributions for Panel d (Z Type Stiffeners)

The analytical results gave a corresponding ratio of 2:1, which is a more reasonable ratio. The sonic fatigue test results gave ratios a little less than 2:1. Thus, the static result seems inconsistent with both the analytical and the sonic fatigue test results, in addition to appearing to be less logical. Conversely, the static test results showed the edge stresses to be approximately 85 percent to 90 percent of the center bay stresses, whereas the analytical results showed the same edge stress to be approximately three times the corresponding center stress.

Under fully-fixed edge conditions, the edge stress should be twice the center stress, thus the static test result appears more logical. The sonic fatigue test results showed a corresponding ratio very close to the static test results. It is surprising that the analytical results would produce a higher stress ratio between the edge and center stresses than one would obtain under fully fixed edge conditions. In summary, the static test gave a logical relationship between center and edge stresses, but an unexplained relationship between biaxial stresses at the panel center; whereas the finite-element results gave a logical relationship between the center panel biaxial stresses, but a surprising relationship between center and edge stresses. The sonic fatigue test results, which are more typically plagued with inconsistencies, gave logical relationships for both biaxial and center-to-edge stress ratios.

A set of analytical results was generated using a J type stiffener in place of the Z stiffeners, for stiffener design comparison purposes. Since the stiffeners in this program were adhesively bonded to the skins, the J configuration offers twice the bonded footprint area on the skin than does the Z configuration.

The static analysis utilizing the J stiffeners was accomplished in much the same way as with the Z stiffeners. Portions of the previous finite-element models were utilized, except for areas near the stiffeners which were modified to incorporate the additional flange of the J design. Identical boundary conditions from the 2-inch coarse grid model were used



and a unit pressure load was again applied. The results for panel "b" are shown in Figure 7. As expected, the stress distributions for the two stiffener designs are quite similar across the majority of the panel, with the J stiffener effecting a 20 percent stress reduction at the panel center. The major difference occurs at the panel edge, where the additional attach flange of the J stiffener significantly reduces the peak stress by avoiding the abrupt stiffness change at the attach radius of the Z stiffener.

d. Dynamic Analysis - The dynamic analysis of the sonic fatigue panel configurations in this program required the construction of finite-element models to represent a quarter of each panel array. The primary purpose of the analysis was to determine the natural frequency and corresponding mode shape of the fundamental in-phase stringer-bending mode for each panel configuration. The quarter model (shown in Figure 3) limits modal solutions to those that are symmetric or antisymmetric about the panel array center lines, thereby excluding certain intermediate modes that are not of interest to this program. The quarter model does, however, cover all the bays in one quadrant, thereby facilitating the identification of a stringer-bending mode in which all bays vibrate in-phase. Skin members were represented by the NASTRAN plate element "CQUAD2." Stringer and frame members were intially represented by bar elements.

Problems were encountered in identifying an in-phase stringer-bending mode for certain panel configurations, particularly those panels having greater stiffness due to curvature and/or close stringer spacing. In such cases, the response was dominated by deflections of the substructure to the extent that computed frequencies were not responsive to changes in skin thickness. In addition, it was not possible to distinguish between overall panel-array modes and coupled "bay" modes. Such structural behavior would be typical of panels having inadequate stiffening members, incapable of properly serving as panel breakers. However, both the static model results and measurements made during sonic fatigue testing showed

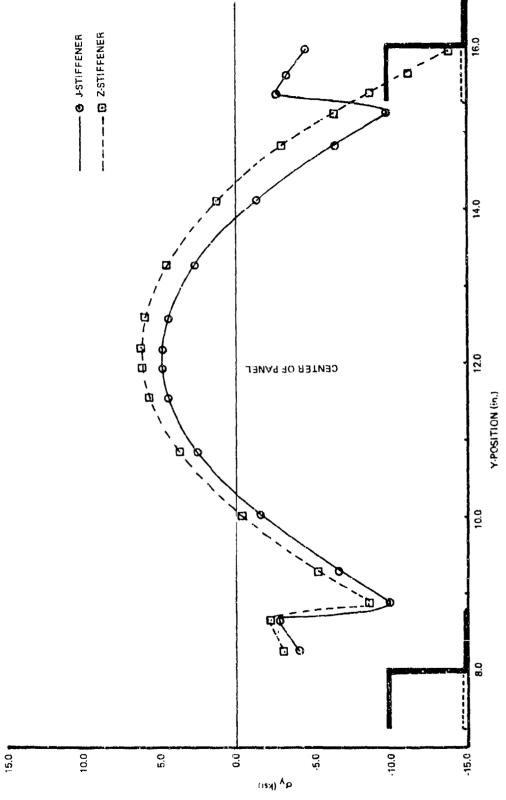


Figure 7. Comparison of Static Stress Results Between J and Z Type Stiffeners for Panel b

\$8

the stiffening members to be adequate and to properly break up the overall panel arrays into their individual bays. This modal identification problem was therefore assumed to be related to the finite-element models, the NASTRAN plate elements or even fundamental analytical problems associated with finite-element techniques. This type of problem is not confined to this program. Previous sonic fatigue programs have reported⁽²⁾ similar difficulties regarding the dominant behavior of substructure in the dynamic analysis of skin stringer structures using finite-element techniques. The problem is compounded in curved panels by the inherent limitations of flat finite-elements to represent highly curved structures. NASTRAN does have available curved plate elements. However, advice from several sources, including AFFDL, cautioned against using them.

Various attempts to solve the problem were undertaken. NASTRAN has three dynamic solution methods available: "Inverse-Power," "Givens" and the "Determinant Method." The "Inverse-Power" method was being used when the modal identification problem was encountered. The other two methods were consequently tried; however, the results from all three methods were strikingly similar. Many of the mode shapes obtained during this exercise were observed to be similar to those generated in Reference 2.

Finite-element methods and computer programs such as NASTRAN are known to experience mass conditioning problems when analyzing thin sheets reinforced with relatively massive stiffeners. This aspect of the problem led to using dynamic models similar to the coarse grid quarter models used in the static analysis, combined with representing the stiffeners as plate elements as in the fine grid three-dimentional models used in the static analysis. This resulted in a significant improvement in the generation of the in-phase stringer-bending mode for all but the two 30-inch curved panels (f and s). These two panels failed to go erate recognizable in-phase modes. Other panels that had previously failed to generate this mode (d, i, j, l and r) now produced an in-phase mode, but with excessive stiffener deflections and at unreasonably low frequencies. The

compatibility of test frequencies with fully fixed frequencies, calculated using Reference 5, confirmed that the problem was with the finite-element analysis results. Figures A-19 through A-24 in Appendix A show six of the ten models.

A further refinement of the model was then made. Previously, the stiffener skin interface had been modeled with a series of single elements whose properties were composed of an homogeneous superimposition of the individual skin and stiffener flange properties. It was thought that the interface between the massive stiffener element and the thin skin element could be the source of mass ill-conditioning. These areas were therefore remodeled with the frame and skin elements individually represented. Connection between the two was provided through the use of multipoint constraints (MPC) that enforce displacements of equal magnitude, normal to the panel, for pairs of adjacent grid points. This required some resequencing of grid points, which resulted in a significant increase in the stiffness matrix bandwidth. The problem was overcome by using a preprocessor program that resequenced the grid numbering. The results from this effort were disappointing, however, with no improvement in the dynamic response of the problem panels.

Another area of concern in the dynamic analysis was the sensitivity of the results to the boundary conditions applied to the test panel fixture frame. During sonic fatigue testing, both steel and aluminum frames were used on selected panels. Also, changes were made in the elastic restraining forces acting on the panel-fixture assembly. Neither of these variations influenced the dynamic response of the test panels. However, the analysis results were found to be highly dependent upon such variations. It was also noted that the fixture frame had much greater predicted deflections from the analysis than occurred during testing. The reasons for this inconsistency are not known. It was decided to reduce the influence of these boundary conditions and the fixture displacements by modifying the finite-element models to eliminate the out-of-plane motion of the fixture. This resulted in changes in response frequencies,

but did not clarify the modal identification problems. The final dynamic results were generated with this fixture motion eliminated.

Although some analytical difficulties remained unsolved, the majority of the panels produced well defined in-phase stringer-bending modes, many of them occurring in the expected frequency range. Figures A-25 through A-28 in Appendix A show the first four mode shapes for panel "b." The frequency progression of these four modes is interestingly consistent with the elastic properties of the panel and its boundary conditions. The bay having the maximum response is seen to shift in turn from that of least fixity (center bay), to that bay with one short side restrained, to that with one long side restrained and finally to that bay with two sides restrained (corner bay), with increasing frequency. It is also clear that Figure A-25 is the desired in-phase stringer-bending mode, occurring at 171 Hz. A list of the complete set of dynamic solutions is given in Table 12. No solutions are offered for panels "f" and "s." The first four modes obtained for panel "f" are shown in Figures A-29 through A-32 in Appendix A. The first modes are first order modes within each bay, but all contain a combination of in-phase and out-of-phase components. The fourth mode (Figure A-32) shows the first of the second-order modes. One last attempt was made to force a first order in-phase mode by forcing an in-phase displacement at the center of each bay. Under this condition the model did not generate a solution (no roots were found). This confirmed that the desired mode was not simply being missed in the modal search procedure, but was actually nonexistent within the analytical framework presented here.

Early in the program, finite-element models were constructed to represent the shaker specimens. The purpose of these models was to ensure that the shaker specimens were designed to fall within the test envelope of the shaker to be used and to avoid having shaker test specimens with torsional and bending modes too close together. It was important in the shaker test program to avoid exciting torsional modes. This analysis also served as an indication of the accuracy with which NASTRAN, combined with the

TABLE 12
TABULATED RESULTS OF NATURAL FREQUENCY SOLUTIONS

Pane1	Panel lst Bending Frame Free (In-Phase)	Panel Ist Bending Frame Fixed (In-Phase)	Panel lst Torsion Frame Free	Panel lst Torsion Frame Fixed	Panel Description
a	139	·•	-	-	3 x 3 Flat
b	171	-	177	-	3 x 3 F1at
С	179	-	187	-	3 x 3 Flat
d	-	246	271	275	3 x 3 Flat
f	-	-	464	463	3 x 3 R = 30
g	398	-	285	-	3 x 3 R = 60
h	318	-	236	-	3 x 3 R = 90
i	-	305*,332*	570	570	6 x 3 Flat
j	-	341	611	612	6 x 3 R = 90
k	302	+ 2 76	312	312	4 x 3 Flat
1	347*	317*	520	520	4 x 3 R = 90
n	94	-	-	-	3 x 3 Flat
р	219	-	160	-	3 x 3 R = 90
q	-	299	330	353	6 x 3 Flat
r	-	348*	-	483	6 x 3 R = 60
S	-	-	372	350	4 x 3 R = 30

^{*}Significant Stringer Movement

laminate properties generated by the COMPOSITE program, would represent the composite laminates used on this program for the sonic fatigue test panels. Figure 8 shows the finite-element model used to represent the shaker specimens. Table 13 gives the first four plate bending modes for the shaker specimens described in Section III. Hand calculated values using Den Hartog $^{(14)}$ are shown for comparison. The hand calculated values assume the zee stiffener to represent a fully-fixed support, resulting in slightly higher values than the first anti-phase mode. The fact that the first in-phase mode frequencies are higher than the hand calculated values is probably due to stiffening effects of the zee along its attach flange, which effectively shortens the length of cantilevered skin. Figure 9 shows the first six modes for shaker specimen type 2. In the shaker specimen analysis, the term "torsion" refers to the skins twisting out-ofplane and not to stringer torsion. These results show the torsion and bending modes well separated. Table 14 shows a comparison of the first four skin bending mode frequencies with measured values on the shaker table. The relatively close agreement between measured and calculated values even for the higher order modes is indicative of a sound analytical approach.

This early optimism turned out not to be fully justified when analyzing the more complex multi-bay panels, as discussed earlier in this section.

This concluded the dynamic analysis using the finite-element models. Because of the progressive underestimation of computed frequencies with increasing panel stiffness, these computed frequencies are thought to be unsuitable for use in developing a sonic fatigue design method. In order to present alternative frequency prediction techniques, some additional dynamic analysis was performed and the results are presented in Section II.6.

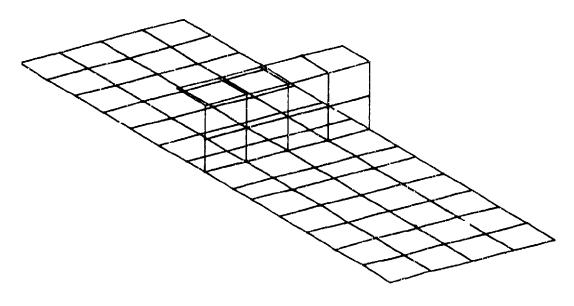


Figure 8. Finite Element Model for Shaker Specimens

TABLE 13
NATURAL FREQUENCIES OF SHAKER TEST SPECIMENS

B1	NASTRAN Anti Pha	Generated se Modes	Frequenc In Phas	Hand Calculated	
Panel Number	First	Second	First	Second	Frequencies (Den Hartog)
1	40	254	61	346	49
2 & 6	58	352	77	438	62
3	56	366	89	505	74
4	81	507	122	692	97
5	73	399	74	455	77
7	33	203	45	253	36

Panel Configuration (Not to Scale)

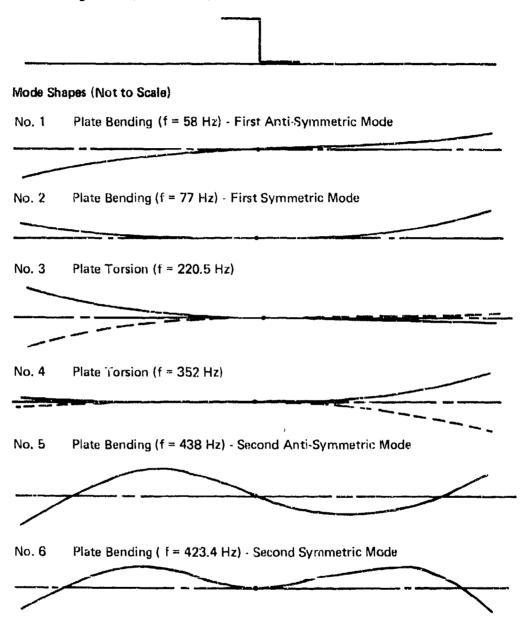


Figure 9. Mode Shapes of Shaker Specimen No. 2

TABLE 14

COMPARISON OF MEASURED AND CALCULATED FREQUENCIES
FOR SHAKER SPECIMEN TYPE 2

Mode Shape	Calculated Frequencies (Hz) Original Model	Measured Frequencies (Hz)
First anti-phase	58	65
First in-phase	77	91
Second anti-phase	352	443
Second in-phase	438	534

6. ADDITIONAL FREQUENCY ANALYSIS

Because of the unresolved difficulties with the dynamic analysis using finite-element techniques, it was decided to generate a set of solutions for the in-phase stringer-bending mode, using a set of equations developed by $\operatorname{Lin}^{(8)}$. Lin's approach utilizes differential equations applied to a row of continuous panels. By treating the skin and stringers as integral parts of the structure, the method utilizes stringer properties in addition to skin properties, thereby facilitating accurate comparisons between different stringer properties and designs. Differential equations are used to represent flat and curved panels. The flat panel equation is derived from a well known fourth order equation of motion, applying $\operatorname{Levy's}^{(15)}$ solution and appropriate boundary conditions to develop the following equation for the frequency of the in-phase stringer-bending mode:

$$k_{1} \sinh \frac{k_{1}}{2} \left\{ \left[E_{b} I_{\eta} \left(\frac{n_{1} \pi}{2} \right)^{4} - p_{b} A \omega_{m}^{2} \right] \cos \frac{k_{2}}{2} - 2 \frac{D}{b^{3}} k_{2}^{3} \sin \frac{k_{2}}{2} \right\}$$

$$+ k_{2} \sin \frac{k_{2}}{2} \left\{ \left[E_{b} I_{\eta} \left(\frac{n_{1} \pi}{2} \right)^{4} - p_{b} A \omega_{m}^{2} \right] \cosh \frac{k_{1}}{2} \right.$$

$$- 2 \frac{D}{b^{3}} k_{1}^{3} \sinh \frac{k_{1}}{2} \right\} = 0$$

$$(14)$$

where

$$k_{1p} = b_p \left[\omega_{in} \left(\frac{h_p \rho_p}{D_p} \right)^{1/2} + \left(\frac{m\pi}{2} \right)^2 \right]^{1/2}$$
 (15)

$$k_{2_{p}} = b_{p} \left[\omega_{m} \left(\frac{h_{p} \rho_{p}}{D_{p}} \right)^{1/2} - \left(\frac{m\pi}{\ell} \right)^{2} \right]^{1/2}$$
 (16)

and

A = cross-sectional area of stringer

D = bending stiffness for skin, $Eh^3/12(1 - v^2)$

E = modulus of elasticity of skin material

E_b = modulus of elasticity of stringer material

I_n = moment of inertia of stringer cross section

m, n = positive integers

 $\omega_{\rm m}$ = natural frequency for flat continuous panels, radians/sec

t = time, sec

b = width of individual panel

h = thickness of skin

e = length of individual panel

ρ = mass density of skin material

 ρ_b = mass density of stringer material

The curved panel solution is obtained by expressing the strain and kinetic energies in terms of generalized coordinates. The equations of motion are then derived by a Lagrangian formulation.

The results of this analysis are shown in Table 15. For convenience, trequencies calculated from AGARD design nomographs (5), the finite-element models, Lin's equations (8), and the sonic fatigue tests are all presented for comparison purposes. It is not known why Lin's equations failed to generate solutions for panels "j" and "l." It is interesting to note that Lin's equations gave unexpectedly high frequency values for the 30-inch curved panels (f and s); the same two panels for which the finite-element

TABLE 15
COMPUTED AND MEASURED NATURAL FREQUENCIES

				Fi	requencies	(Hz)	
Configuration	Skin Thickness "t" (in.)	Stringer Spacing "b" (in.)	Radius of Curvature "R" (in.)	Agard ⁽⁵⁾ Fully Fixed	Nastran	Lin ⁽⁸⁾	Test
d	.033	8	Hat	160	139	151	143
b	.044	8	Mat	202	171	177	170
d	.066	8	flat	308	246	281	340
f	.044	8	30	825	-	1,208	505
y	.044	а	60	510	398	583	350
h	.044	8	90	375	318	363	290
i	.044	Ą	Flat	674	332	558	800
j	.044	4	90	824	340	-	950
k	.044	t	flat	312	302	292	380
1	.066	6	90	631	347	-	680
n	. 02?	3	Hlat	120	94	101	140
р	. 022	8	90	377	219	447	180
g	.022	4	Hat	409	299	363	370
r	. 033	4	60	782	348	442	780
s	. 022	6	30	828	-	1,366	380

analysis failed to generate solutions. It is also interesting to note that of the three sets of calculated frequencies, the AGARD nomograph results showed the best correspondence to the test results.

SECTION III EXPERIMENTAL

1. INTRODUCTION

The purpose of the experimental program was to provide the empirical data base for the design method described in Section IV. This phase of the program consisted of designing and fabricating a range of shaker test beam specimens and "progressive-wave tube" (FJT) multi-bay test panels. The multi-bay panels covered a range of stringer spacings, skin laminate thicknesses and radii of curvature typical for aircraft application. The configurations are shown in Table 1. They were instrumented with strain gauges and microphones and their response characteristics measured over a wide range of sound pressure levels, before being tested to failure. The shaker tests augmented the PWT tests by providing additional random fatigue data for the composite skin laminates used in the multi-bay panel designs.

2. TEST SPECIMEN AND FIXTURE DESIGN

a. Progressive-Wave Tube Test Panels -- Twenty-seven multi-bay test panels, comprising eighteen configurations, were designed and fabricated for subsequent sonic fatigue testing in a progressive-wave tube. Seven of the configurations had duplicate panels and one configuration (m) was a reference panel. The reference panel provided a data link to a set of existing Rohr test panels, which were also tested in this program.

These existing panels included an aluminum skin-stringer panel to provide a data link between graphite and aluminum panels. The configurations of the new panels are listed in Table 1. They comprise flat and curved graphite-epoxy skins, ranging from 4 ply (.022") to 12 ply (.066"), stiffened with adhesively bonded graphite-epoxy Z stringers and longerons in 3 x 3, 4 x 3 and 6 x 3 panel arrays. One configuration (e) had honeycomb beam stiffeners and two configurations (b and c) had additional panels fabricated with J stiffeners, thus facilitating a comparison between different stiffener designs. Figure B-1 in Appendix B shows engineering drawings of the test panels.

The overall test panel size was kept constant (24-inch by 36-inch) in order to minimize tooling and test fixture costs. Ten of the configurations consisted of nine 8-inch by 12-inch equal size bays in 3 x 3 arrays. Ten configurations were flat and eight were curved, with radii of curvature of 30-inch, 60-inch and 90-inch. These curvatures encompass radii ranging from small aircraft nacelles through to wide body fuselages. Five different skin laminates were used, two of which (b and c) had the same number of plies but with different orientations. This served to isolate the effects of ply orientation for a given number of plies. With the exception of the reference panel (m); 4-inch, 6-inch and 8-inch stringer spacings were used in 6 x 3, 4 x 3 and 3 x 3 arrays respectively. Panel e had honeycomb beam stiffeners, utilizing a nonmetallic core material. This is a lightweight, low cost stiffening concept whose sonic fatique resistance relative to the more conventional Z stiffeners is of considerable interest. Thus, with 27 panels, a comprehensive range of design parameters were covered, with duplicate panels of some configurations provided to check test repeatability and to provide more reliable fatigue data points. The panel parameters (stringer spacing "b," laminate thickness "t" and radius of curvature "R") were varied such that any two panel responses can be related by varying one parameter at a time, thereby facilitating a quantitive identification of the parametric cause of the difference in response.

The reference panel (m) comprised a single row of bays, duplicating the panel geometry of the five existing Rohr panels, shown in Figure 8-2 in Appendix B. Panels 1 and 5 provide a direct comparison between aluminum and graphite aulti-bay structures. Panels 2 and 3 are identical unstiffened graphite panels, representative of a current nacelle structure in commercial service on an experimental basis. Panel 4 had a single honeycomb stiffener.

b. Stiffener Design -- Three types of stiffeners were evaluated in this program; graphite epoxy Z and J section stiffeners and honeycomo beam stiffeners with graphite reinforced caps. The program concentrated on the Z stiffeners which are widely used on aircraft structures. The J stiffeners were included because of their ability to reduce edge stresses (compared to a Z) for minimal cost and weight increase. In aluminum structures, Z stiffeners are inexpensively formed, whereas J stiffeners have to be more expensively extruded or machined. In graphite structures, however, both stiffener types are similarly fabricated. Consequently, the J section is a more cost effective design in graphite than in aluminum. The honeycomb stiffeners, as mentioned earlier, were included for their low cost and low weight advantages.

Stiffener details are shown in Figure B-1. The Z and J stiffeners were constructed from $^\pm$ 45 deg. graphite epoxy laminates with unidirectional fibers buried in the free flanges. The number of $^\pm$ 45 deg. laminates were varied from configuration to configuration in order to provide the appropriate stiffnesses for their respective skins. The Z stringers were 1-inch deep and the longerons were 1-1/2-inch deep. Their stiffnesses were designed to ensure that they effectively served as panel breakers. This was accomplished by using Reference 8 to calculate their fundamental in-phase stringer-bending mode frequencies, and comparing the results with corresponding fully-fixed frequencies of individual bays calculated using Reference 5. If the stiffeners have adequate bending stiffness, the frequency of the stringer-bending mode will approach the fully-fixed value. The results of this comparison can be seen in Table 15, and show

the Z stiffeners to be effective. At stringer-longeron intersections, continuity of the attached and free flanges was maintained for both stringers and longerons. The webs of the stringers were also continuous and were clipped to the webs of the longerons, which were partially cut away. Titanium clips are shown in Figure B-1. These were later changed to steel following some clip failures during the first scnic fatigue tests. For the honeycomb stiffeners, the intersections consisted of honeycomb core splices with a foaming adhesive locally applied. The graphite caps were continuous. At the edges of the panels, the attach flanges of the stiffeners extended under the test fixture frame and the upstanding stiffener webs were clipped to the fixture web. Figure 10 shows a photograph of a honeycomb beam stiffened panel. Examples of zee stiffened panels are shown in Figures 29, 30 and 31. For cross reference purposes with Section II of this report, the stringers run in the X-direction and the longerons in the Y-direction.

c. Progressive-Wave Tube Fixture Design -- The test panels were terminated by relatively stiff channel sections, shown in Figure B-1. There were two fixturing approaches considered in this program. One was to bolt a picture frame/panel assembly rigidly to the progressive-wave tube (PWT). The other was to suspend a stiff picture frame/panel assembly on captive wires. The former approach more closely approximates fullyfixed edge conditions, which is more convenient when the test results are to be compared to simplified analyses where fixed edges are usually assumed. This approach has the disadvantage of the panel response being affected by vibrations in the PWT itself. The latter approach eliminates any response interference from the PWT and allows the fixture to be accurately represented in the finite-element models. Since the fixture is constrained only spatially in the PWT, its boundary conditions are able to be accurately represented in the analysis. The latter approach was chosen for this program. An additional advantage of this approach was that it was a relatively simple matter to remove a panel from its frame and thereby make response measurements under two different boundary conditions, in order to evaluate their effects. A set of steel frames was

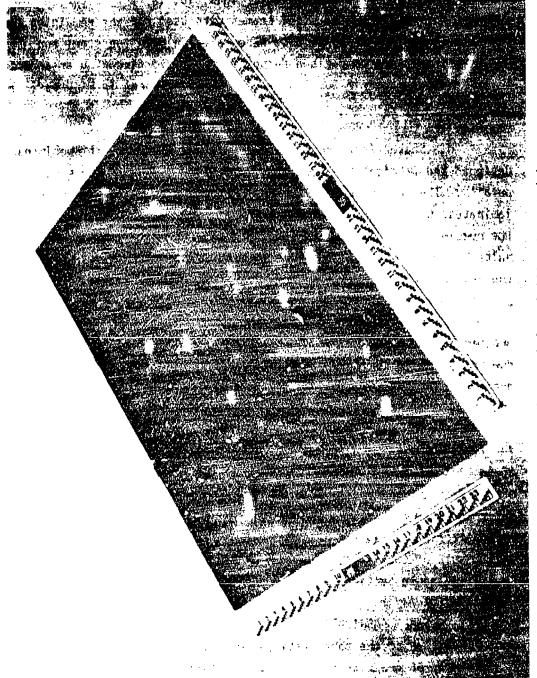


Figure 10. Honeycomb Beam Stiffened Panel (e)

added to the program as back-up fixturing should the aluminum frames experience any sonic fatigue damage. This did, in fact, occur on one of the curved panels, and the steel frames were used for the remaining curved panels. Some panel response data were taken in both the steel and aluminum frames for comparison purposes. The test fixturing arrangement is discussed further in Section III.5, and can be seen in Figures 22 and 24.

d. Shaker-Test Specimens -- Eighty-one shaker test specimens were designed and fabricated. Figure B-3 in Appendix B shows the specimen details. The specimens consisted of 3-inch by 10-inch sections of skin laminates, with stringer sections attached across the short dimension. The specimens represented each skin-stiffener combination used on the multi-bay test panels. A set of specimens having the stringer riveted to the skin was included to provide for a fatigue life comparison with bonded joints. The shaker specimens were intended for fatigue testing the skin-stringer joints in order to develop fatigue curves to augment the progressive-wave tube test results. This objective was not fully realized due to some adhesive bonding quality problems encountered early in the program. These problems and their effects are discussed in Sections III.3 and III.4.

The fixturing for the shaker tests was originally a simple tee section, 15-in. long, accommodating five specimens at a time. The upstanding webs of the Z stringers were mechanically fastened to the upstanding leg to the tee. The assembly was then simply bolted to the shaker table for testing. This fixturing was later changed when the shaker test program was modified as a result of the adhesive bonding problems mentioned above. The changes are discussed in Section III.4.

3. TEST SPECIMEN FABRICATION

Fabrication of the sonic tatigue test panels involved the manufacture and assembly of graphite epoxy skins and stiffeners fabricated from Hercules AS-3501 Pre-Preg. The skins were laid up and cured, on a flat or

curved tool as appropriate, from 12-inch wide graphite tape. Each ply was oriented with respect to a reference direction in order to build up the desired panel stiffness properties. After cure of the skin, the stiffeners were attached in a secondary bond cycle using 3M's AF147 adhesive.

The Z and J stiffeners were laid up and cured on a separate tool. Layup of these stiffeners included $^{\pm}$ 45 deg. plies, from the flanges through the web, for shear stiffness and strength. Additional unidirectional fibers were added to the free flanges of the stiffeners for bending stiffness and strength. Following adhesive bonding assembly with the skin, the stringer-longeron intersections were stabilized with angle clips, which were mechanically fastened in place.

For the sandwich stiffened panels, the stiffeners were fabricated in place on the skins by cocuring the core-to-skin and cap-to-core bonds simultaneously with the cure of the cap. Since the longerons utilized deeper core than did the stringers, the caps for both were continuous across the intersections. The only tie then required at the intersections was a foaming core splice adhesive, cocured with the remainder of the stiffeners as described above. Fiber orientation in the caps was primarily unidirectional.

All panels required an edge buildup to allow for mechanical fastening in the test fixture. This was accomplished as part of the layup and cure of the panel skins. Provisions were also made for attachment of the ends of the stiffener webs to the fixture.

Fabrication of the shaker specimens was basically the same as for the sonic fatigue test panels. For the shaker specimens, however, it was more efficient to fabricate several large panels and subsequently cut them into the required size for the individual specimens.

5,

A quantity of 25 basic tools plus 2 rate tools were designed and fabricated. Tooling for the shaker specimens was minimal, with only two assembly bond jigs and one Z section layup tool required. The flat sonic fatigue panels required eight tools. The remaining 16 tools were for the curved panels.

Figures 11 through 17 show photographs of the tools and layup. Figure 11 shows the bond jig for the zee layup. The zees were made by cutting hat sections in half. The beam in the center of the tool is for the hat layup. Around the edge of the tool is a rubber tube bonded in place with RTV. This acted as a vacuum seal for the rubber bag (Figure 13). Figure 12 shows the same tool with the graphite-epoxy fabric laid down for the hat section. Figure 13 shows the tool with the silicone rubber bag in place. This was a reusable bag, which effects cost savings and improves laminate surface condition, as compared to using disposable bags. Figure 14 shows a pair of cured hat sections. Figure 15 is an assembly tool, which was used to locate the zees on a skin laminate. The two beams, when holted down, locate the zee section. Figure 16 is the warresponding locating tool for the honeycomb stiffeners. Figure 17 shows a layup of graphite/epoxy prepreg for the skin elements.

Coupon tests were performed on each layup to determine resin content, density, fiber content and void content. Two 1-inch square coupons were used for each layup. Ultrasonic C-scans were performed on each specimen to check for bondline voids.

During specimen fabrication, problems were encountered in two areas. The first problem occurred in the layup of the zee stringers and longerons. The bond tool failed to generate adequate pressure in the zee radius to be adjacent to the skins. As a result, this radius had sporadic areas of surplus resin and resin starvation. This bond pressure deficiency resulted in inadequate interlaminar strength. In addition, excess resin areas are prone to surface cracking, which in turn can result in premature fatigue crack initiation under the kind of severe test conditions for

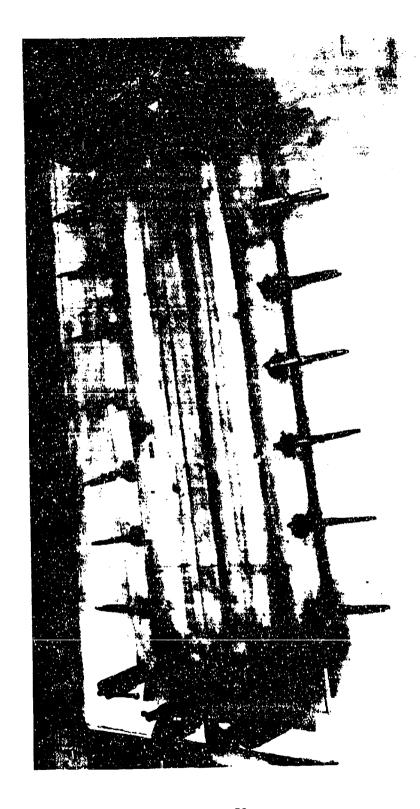




Figure 11. Bond Jig for Z Layup



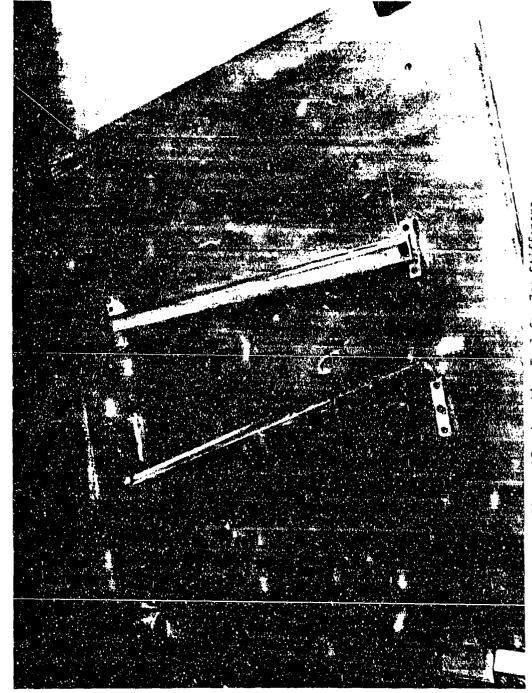
Figure 12. Bond Jig with Hat Section in Place



igure 13. Bond Jig with Bag in Place



figure 14. Cured Hat Sections



igure 15. Locating Tool for Lee Stiffeners



Figure 16. Locating Tool for Honeycomb Stiffeners



igure 17. Layup of Graphite Epoxy Skin

which these specimens were intended. "Ithough there were no reliable criteria for the strength requirements in the stiffener radii, the fact that zee stiffeners are not symmetrical sections and can be expected to experience some rotation under random acoustic loading conditions, led to them being rejected as unsuitable for sonic fatigue testing. The bond tool was then modified to provide more effective throw-in blocks in the radii, and a set of good quality stiffeners was then fabricated. Although this problem did not affect the sonic fatigue test panels, some of the shaker specimens had already been completed before the problem was discovered. The effects that this problem had on some of the shaker test results are discussed in Section III.4.

A second, and more serious, problem was discovered during the early shaker tests. The first specimens tested (see Section III.5) experienced premature failure in the adhesive joint between the stiffeners and the skins. This caused considerable concern, since the fabrication of the shaker specimens had been completed, and fabrication of the multi-bay parels was in progress, with some of them already completed. Visual examination of the failed adhesive joints revealed excessive porosity in the adhesive. This type of porosity, consisting of a large number of very small voids, does not show up on altrasonic C-scans. In addition, there was no graudite fiber pull-out around the failed joints. Fabrication of the multi-bay panels was them suspended, and a thorough investigation of the adhesive bonding problem as initiated. The investigation centered on an examination of the bonding process, but also included a reevaluation of AF:17, the adhesive selected for this program. AF:47 is a tough, elactomeric adhesive with high peel strength. It is used extensively on he F16 airplane and has good strength properties over the temperature range for which graphite-epoxy structures are considered suitable. It is, however, an adhesive that is particularly susceptible to moisture during facrication

1000000

The initial investigation of the bonding process and the condition of the adhesive revealed a higher moisture content than was considered acceptable. An additional batch of shaker test specimens was fabricated after additional storing of the adhesive in a dessicator in order to eliminate any moisture. Some of these specimens were statically tested by simply pulling the skin and stringer sections apart. A 10 percent increase in static strength was obtained, compared to the original shaker specimens. Comparative shaker tests were then carried out. Some riveted specimens were added to this comparative test, in order to provide a reference to which the bonded specimens could be compared. The results of this comparative testing were disappointing. Although the "dried" adhesive produced significant fiber pull-out upon failure, the fatigue life did not significantly increase. Table 16 shows the results.

As a result of this adhesive problem, and also because of the extreme importance of stiffener and skin laminate quality, a thorough investigation was carried out to determine the history and quality of all the sonic fatigue pane. Components and assemblies, including additional assessments of adhesive bond quality. The following tasks were performed:

- (1) The weight percent of resin and void percent by volume of all skins were determined and tabulated. The results are given in Table 17. Acceptance criteria for this program required a resin content of 27 percent. Consequently, skins bl and cl were rejected. q was considered marginal at 26 percent. However, the flatwise tension tests performed on the rejected cl skin (see Item 3 below) produced good results, indicating that q was an acceptable laminate.
- (2) Sections of 2 stiffeners were cut, mounted and photographed.

 The zees made on the original tool were found to be resin

 rich. However, the zees used for the sonic fatigue test

 panels were found to be representative of production quality.

TABLE 16
SHAKER TEST RESULTS FOR ADHESIVE EVALUATION

<u>Sperimen</u> (All ⊥ype 2)	Overall RMS Stress Level (lb/in ²)	Cycles to Failure
Riveted	7,370	234,000
Bonded - dried	8,040	3,000
Bonded - dried	6,432	6,000
Bonded - original	Gauge Lost	5,400
Bonded - original	9,179	5,400

TABLE 17
VOID AND RESIN CONTENTS OF SKIN LAMINATES

a-1 6 28 .64 1.	.61
a -1 0 20 .04 1:	**
a-2 6 29 .47 1	. 60
b-1 8 24 1.20 1.	.63
b-2 8 31 -0- 1	.61
c+1 8 24 1.29 1	.63
c-2 8 29 .175 1	.60
d 12 27 .31 1	. ú3
e-1 8 33 .26 1	. 58
e-2 8 30 .21 1	.6 0
f-1 8 31 .57 1	. 59
t+2 8 31 .46 !	.59
g-1 8 29 .575 1	.61
q-2 8 27 .79 1	.6"
h 8 29 .11 1	.64
i 8 33 .03 1	. 58
j 6 27 .155 1	.63
k-1 8 31 -0- i	. 60
k-2 8 31 .765 1	. 58
1 12 29 .224 1	.61
m 8 28 ,16 1	. 62
n 4 28 1.37 1	.60
p 4 27 .63 1	. 63
- q 4 26 .58 1	. 6 2
r 6 29 .36 1	. 62
s 4 27 1.595 1	. 59

- (3) Flatwise tousion tests were performed on the rejected of skin laminate and on a specially fabricated d (12 ply) laminate. The results are given in Table 18. They show the columnate to have comparable strength to the dolaminate, indicating the percent resin content criterion to be conservative.
- (4) A range of shaker specimens were fabricated using different adhesives and different processes, for comparison with the original specimens. The adhesives used were AF147, the current selection, and FN1000. FM1000 is an older adhesive that has excellent strength properties and is easy to use. However, it is environmentally susceptible and is not widely used in production. It is, however, an excellent reference adhesive. Using two plies of AF147 was also evaluated. Table 19 shows the results of the static tests and Table 20 shows the shaker test results. The AF147 was found to have superior static strength, but FM1000 did better in fatigue. It was also clear that a second ply of AF147 resulted in a significant improvement in fatigue life.

Following the above tests, the failed static and shaker test specimens bonded with AF147 were found to have porosity uniformly dispersed in the weave pattern of the knitted fabric in the bond line. Additional testing was then performed in order to determine the cause of this porosity.

These tests included the comparative evaluation of (1) solvent wiping subsequent to grit blasting, (2) no solvent, just dusting with a clean dry cloth, (3) an evaluation of the amount of vacuum used during bagging and curing, (4) oven drying of composite details and glass cloth (used as air bleeder) and (5) evaluation of weight loss during oven drying. All of the above were evaluated through lap shear testing and visual examination of failure mode. Volatile contents determinations were also made. The results are given in Table 21. In the lap shear tests, Process 2 gave the highest failing stress, but more importantly, the bond line porosity was

TABLE 18
FLATWISE TENSILE TEST RESULTS ON SKIN LAMINATES

Specimens from Panel c-1 (Flatwise Tensile)

Specimen No.	Failing Stress (psi)
c-1-1	3480
c-1-2	3200
c-1-3	3310

NOTES: 1. Resin content 23.6% by weight, voids 1.29% by volume.

2. Specimens c-1-1 and c-1-2 failed between surface plies, Specimen c-1-3 failed approximately in the center of the laminate.

Specimens from Panel d Noted in Item 3 (Flatwise Tensile)

Specimen No.	Failing Stress (psi)
d-1	3200
d-2	3340
d-3	3180

NOTES: 1. Resin content 32.8% by weight, voids 0.21% by volume.

2. All failures occurred at the approximate center of the laminate.



TABLE 19

COMPARATIVE ADHESIVE EVALUATION - STATIC RESULTS

Failing Load (Lbs.)	Adhesive									
220	Original Lot AF-147, dried (48 hrs.)									
205	Original Lot AF-147, as received									
168	Second Lot AF-147, Dried (120 hrs.)									
206	Second Lot AF-147, 1 ply, dried									
242	Second Lot AF-147, 2 plies, dried									
186	FM~1000									
200	Original Lot AF-147, cut from Panel c-1									
202	Original Lot AF-147, cut from Panel c-1									
220	Original Lot AF-147, cut from Panel c-1									

TABLE 20

COMPARATIVE ADHESIVE EVALUATION - SHAKER TEST RESULTS

Time To Failure (Minutes)	Adhesive
125	FM-1000
37	AF-147, 1 plv, dried
63	AF-147, 2 plies, dried
29	AF~147 - original group

TABLE 21
AF-147 ADHESIVE PROCESSING EVALUATION

1	One-half	inch (nafraví	lan	Shoar	Specimens	(Adherends	cut	from	Danal	c-11	
١.	Une-naii	THULL	JVELLAP	Lap	SHEat	Sher mens	(Aunerenus	CUL	I FOIL	ranei	(-I)	•

Process	Avg. Failing Stress (psi)									
1 2 3	3240 3430 3065									
Adherends grit blasted, wiped with MEK and air dried 30 minutes; 25" Hg vacuum used during bag check and cure.										
Adherends for 45 mi	grit blasted and wiped with clean dry cloth. and glass breather cloth oven baked at 150°F nutes. 10" vacuum used during bag check and ited to atmosphere during cure.									

- 3 Same as Process 2, except 25" Hg vacuum was applied to assembly throughout cure.
- 2. Volatile Content Determination

Process

1

2

Four adhesive specimens were cut from the roll, placed in a $200^{\circ}F$ oven, withdrawn at the noted intervals and weighed.

Spec. No.	Time at 200°F	% Weight Change (Decrease)
1	15 mins.	0.53
2	45 mies.	0.55
3	90 mins.	0.49
4	240 mins.	0.65

reduced by approximately 75 percent from the original specimens. Processes 1 and 3 exhibited excessive porosity, similar to that of the original specimens. Volatile content was determined to be within normal limits for adhesive films. The major factor in the porosity problem was concluded to be the amount of vacuum used during bag check and the lack of subsequent venting to atmosphere during cure. The pulling of vacuum during curing combined with the presence of slight moisture is what caused the poor bond quality. All subsequent assemblies were then tabricated with the AF147 adhesive system (single ply) using the optimized bonding process. Subsequent sonic fatigue tests on joints utilizing Process 2 showed order-of-magnitude improvements in sonic fatigue life over joints utilizing Process 1. It is interesting to note that a major improvement in joint quality relative to porosity and random fatigue life corresponded to a very modest improvement in static strength.

This adhesive evaluation underscores the crucial importance of bond quality in a program of this type, and the need to rectify any problems prior to fabricating a large number of expensive test structures. Fortunately, in this program, the problem was discovered and rectified prior to the fabrication of most of the multi-bay test panels. Those that had already been fabricated were eventually subjected to sonic fatique testing (see Section III.5), and failed prematurely in the bonded joints. They were subsequently replaced with new panels and successfully tested. Unfortunately, the fabrication of the shaker specimens had already been completed prior to the resolution of the bonding problem, and in addition, many specimens were used in the process of achieving a solution. This resulted in a major change in the objective of the shaker tests. It was not now possible to use the existing specimens to evaluate the skinstiffener joint fatique proper ies. Instead, they were used to evaluate the skin laminate fatigue properties, which were unaffected by the bonding problem.

NOTE: It was later learned that the manufacturer of the AF147 adhesive had been having problems with air porosity in this adhesive, and that this had been a contributing factor in the bonding problem experienced by Rohr. The manufacturer, like Rohr, has now overcome the problem.

4. SHAKER TESTS

The shaker test program was originally intended to provide additional fatigue life and mode of failure data on the skin-stringer adhesively bonded joints. The data was to augment the sonic fatigue test data from the multi-bay panels. However, as a result of the adhesive bonding problems, discussed in Section III.3, tests were redefined in objective and scope.

Early shaker tests revealed poor bond quality between the skin and stringer elements. The resulting investigation indicated that the remaining specimens would be similarly deficient. Part of this resulting investigation consisted of performing shaker tests on some of the original specimens and comparing the results with those from a variety of new specimens utilizing different adhesives and process parameters. In this endeavor, the shaker tests proved to be a valuable aid in both discovering the bond problem and in evaluating solutions.

One of the major justifications for shaker testing the skin-stringer joints was the belief that the modes of failure and cycles to failure would correlate with the sonic fatigue test results. This belief turned out to be fully justified. The shaker tests that revealed the poor bond quality were characterized by rapid failures, with stiffeners completely delaminating from the skins, with virtually no graphite fibers being pulled from the skin laminates and occurring at relatively low strain levels. Some early sonic fatigue tests on panels made prior to the resolution of the bonding problem displayed the same failure characteristics. Subsequent testing of specimens having good bond quality resulted in considerable skin laminate damage prior to and during skin-

stringer joint failure in both the shaker and the sonic fatigue tests. Additionally, shaker tests performed on the riveted specimens resulted in failures in the zee radius adjacent to the skin. This same mode of failure occurred during sonic fatigue testing of riveted multi-bay panels.

The specimens were ganged together in groups of five, mechanically fastened through the stringer webs to the upstanding leg of a horizontal tee bar, and subjected to 1/3 octave random loading centered around the specimen response frequency and tested on a Ling B290 shaker having a capacity of 1,500 force pounds. This method was specifically intended to primarily load the skin-stringer joint. Following the discovery and resolution of the bonding problem, it was decided to use the remaining shaker specimens to develop random fatigue data for the skin laminates. In order to accomplish this, the test fixture was modified to support the skin elements as cantilevers, making sure that the skin-stringer joint was well away from the point of maximum stress on the skin. The skins were mounted in tapered blocks in order to avoid abrupt changes in stiffness, and strain-gauged at the point of expected maximum strain. Testing was then carried out as before, with 1/3 octave random loading. Figure 18 shows the shaker test setup.

Complications arose during the early tests due to the high strains required to cause fatigue failures of the laminates. Conventional strain gauges do not have significant fatigue life at the strains required to fail the graphite laminates. To overcome this problem, the specimen holding fixture was strain-gauged and tests carried out to establish a relationship between the fixture gauge and the specimen gauges. This was done using static loading of up to 4,000 microinches/inch on the specimen, and noting the corresponding fixture gauge readings. Correspondence between the specimen and fixture strain gauges was also determined by apply a sinusoidal load up to a specimen strain of 3,000 microinches/inch. Finally, similar correspondence was also established using low level random excitation. The fixture gauge was found to read approximately 1/20 of the specimen gauges. Although there was little variation from specimen

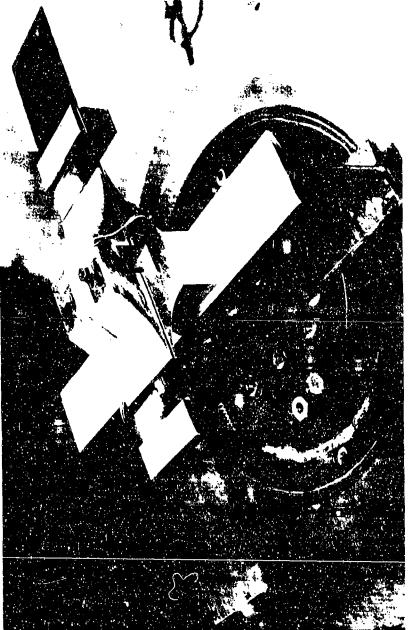


Figure 18. Shaker Test Set-Up

74

to specimen, nevertheless strain conversion factors were measured for each test.

The remaining shaker specimens were then tested to failure. The results are shown in Figures 19 and 20. Figure 19 shows actual rms strains vs. cycles to failure. The curve drawn represents minimum values. The numbers in parentheses refer to the specimen types given in Figure B-3 in Appendix B. Since the elastic modulus varies between different specimen types, there are advantages in presenting data in strain form, allowing users to apply their own modulus values. Figure 20 shows the same fatigue data plotted as rms stress vs. cycles to failure. These curves are used in Section IV in conjunction with the progressive-wave tube test results.

5. PROGRESSIVE-WAVE TUBE TESTS

Sonic fatigue tests were performed on the twenty-seven panels shown in Table 1 and existing panels 1, 2, 4 and 5 shown on Figure B-2 in Appendix B. The tests were carried out in a progressive-wave tube (PWT) at the Acoustic Test Facility, Rockwell International (Los Angeles Aircraft Division), Los Angeles, California. The facility is powered by four Ling EPT 200 transducers, each capable of generating 10,000 acoustic watts. Sine and random inputs are available with frequency spectrum control from 50 Hz to 1,200 Hz. Indefinite endurance tests can be carried out at overall sound pressure levels of 167 to 168 dB. The main test section is in a 6-foot by 1-foot duct cross-section, capable of taking two panels simultaneously, one above the other. The PWT has an acoustic wedge termination into a reverberation room. Rockwell personnel operated the PWT. All instrumentation, data acquisition, signal conditioning and data reduction were performed by Rohr personnel using Rohr's mobile Vibro-Acoustic Laboratory. Figure 21 shows the Rockwell facility and the Rohr mobile laboratory. Figure 22 shows the test section with panels installed. The main purpose of the tests was to obtain strain and frequency response data for the test panels under random acoustic excitation at grazing incidence, and to test the panels to failure, using the data generated to develop a sonic fatigue design method.

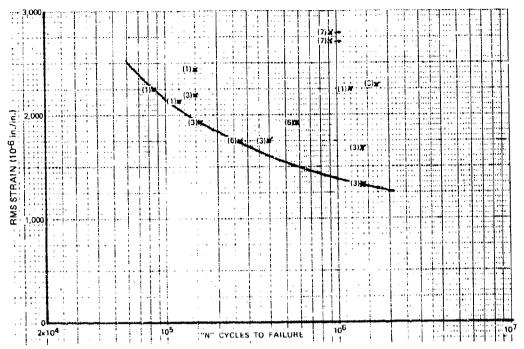


Figure 19. Shaker Test Fatigue Curve: Strain v Cycles to Failure

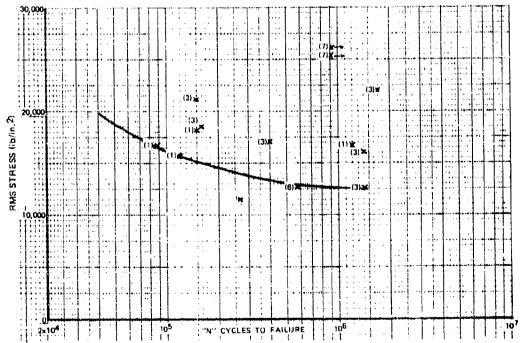


Figure 20. Shaker Test Fatigue Curve: Stress v Cycles to Failure

76

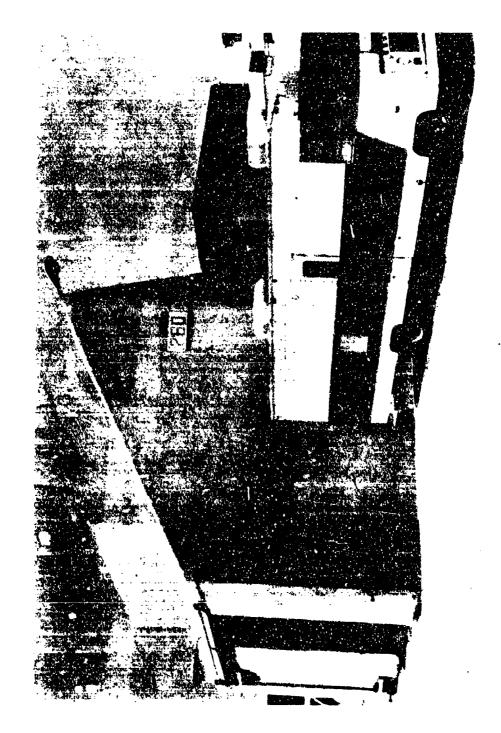
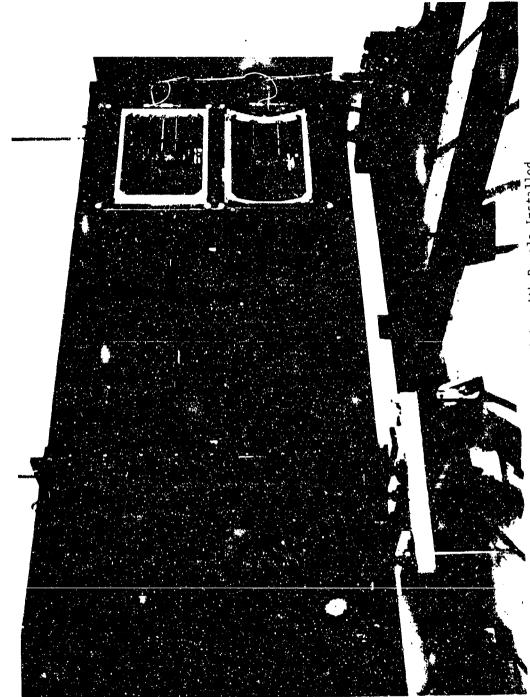


Figure 21. Rockwell Facility and Rohr Mobile Laboratory



re 22. Progressive Wave Tube with Panels Installed

- a. Evaluation of Progressive-Wave Tube (PWT) Prior to the actual test program, a series of measurements were made in the Rockwell PWT in order to determine the maximum overall and spectrum acoustic levels available, without noticeable "clipping". Amplitude distribution plots were also made in order to determine if the acoustic field was reasonably Gaussian. Three microphones were used, in a vertical spread along the center line of the test panel openings. The results showed acoustic spectrum levels of around 140 to 145 dB/Hz to be attainable with broadband loading. Reducing the acoustic loading spectrum to 1/3-octave showed an increase in maximum acoustic spectrum levels of approximately 8 to 10 dB. Figure 23 shows the amplitude distribution function for the center microphone with broad-band input. These data showed the Rockwell facility to be suitable for this program.
- b. Instrumentation All the test panels were instrumented with sufficient strain gauges and microphones to accurately identify dynamic strains, mode shapes and acoustic loading. The center bay of each panel was the most heavily strain-gauged. All panels had biaxial gauges at the center of the center bay and adjacent to both zees on the longer sides. Strain gauge and microphone locations are shown on Figure B-1 in Appendix B. Sheet 1 shows locations for panel "b." Referring to the numbering system for panel b, the other test panels were instrumented as follows:

Panels a, c, d, f, g, h, n. p had strain gauges at positions 3, 4, 7, 8, 10, 11, 18, 26 and 31. In addition, panels a, b, d, n and p had back-to-back gauges for positions 3, 4 and 10.

Panel e was gauged as per Figure B-1, sheet 2.

Panels i, j, q and r had gauges in positions 3 and 4 on each of the four center bays, plus positions 7, 8, 10 and 11 on one center bay, plus position 31.

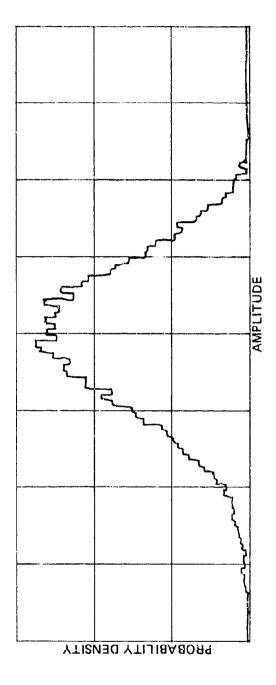


Figure 23. PWT Microphone Amplitude Distribution

Panels k, I and s had gauges at positions 3 and 4 on each of the two center bays, plus positions 7, 8, 10 and 11 on one center day, plus position 31.

Panel m had gauges at positions 1 through 13 on one of the center bays, plus a gauge corresponding to "4" on the remaining seven bays.

The J stiffened panels were instrumented as panel b.

Back-to-back gauges were used on selected panels in order to separate out membrane and flexural strains. Strain gauges were also installed on the test fixture to check for unwanted resonances.

Small (1/8-inch) strain gauges were used to provide for good resolution. Larger strain gauges result in excessive strain averaging, particularly near stiffeners and fixtures where there are high strain gradients. Since these locations are where maximum strains and fatigue failures occur, good resolution is of particular importance. Each panel had two flush-mounted microphones installed. "Kulite" pressure transducers were used. Several panel/fixture assemblies had extra microphone holes provided to facilitate acoustic measurements on all four panel sides. "Kulite" transducers are a strain gauge 'ype microphone and therefore used compatible signal conditioning to that used for the strain gauges. Their high natural frequency (above 70 KHz) and low mass makes them especially suitable for mounting on vibrating structures. Three B&K condenser microphones were installed and monitored inside the PWT as part of the facility operation.

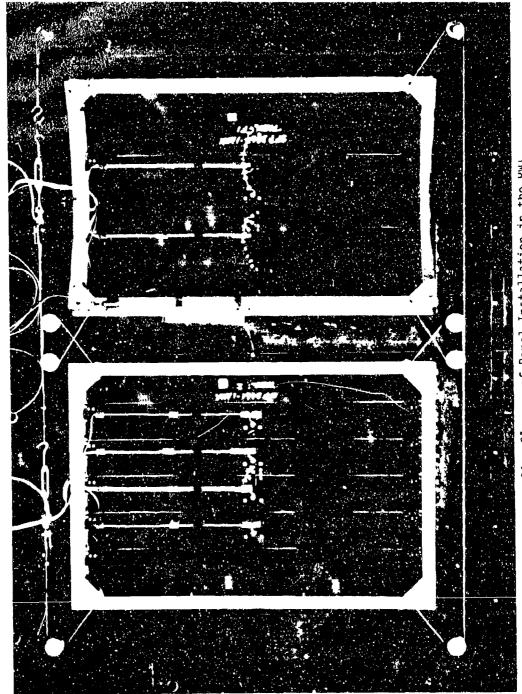
c. Data Acquisition - The data acquisition consisted of twenty channels of strain gauge signal conditioners, coupled through a patch panel to a 14-track FM tape recorder. Two channels were set up for handling microphone (Kulite) signals. Prior to each test run, insertion calibrations for all data channels were recorded on magnetic tape. These insertion calibrations consist of applying a calibration resistor in parallel across each strain gauge to simulate a known compressive strain.



Post test calibrations were also performed as a check, and as a safeguard against neglecting gain changes made during test runs.

d. Test Procedure - Each panel was installed in the progressive-wave tube and subjected to acoustic loading at grazing incidence. The panel-fixture assemblies were suspended on wires, in order to isolate them from PWT vibrations and to achieve accurate boundary condition representation for comparison with the analytical results. Figure 24 shows a closeup view of the panel-fixture installation in the PWT. Load cells were incorporated into the wire harness supporting the panels. This allowed the wire tension to be adjusted identically for each test panel and also facilitated dynamic monitoring to ensure that there were no significant resonances in the panel suspension system. The turnbuckle-pulley arrangement, seen in Figure 24, automatically centered the test panels in the specimen windows.

The test procedure for each panel started with a sine sweep from 50 Hz to 1.200 Hz. The sine sweep was used to identify major panel resonances. This was followed by full spectrum (50 Hz to 1.200 Hz) random acoustic loading from 140 dB to 165 dB in 5 dB steps at 30 second intervals. All strain gauge and microphone outputs were recorded on magnetic tape throughout. In addition, real-time frequency response plots were made for one key strain gauge and microphone. Where the number of transducers for a given panel exceeded the 14 channels available on the tape recorder, these runs were repeated until all transducer outputs, including the fixture gauges and the load cell, had been recorded on magnetic tape. The overall strain levels from all the strain gauges were monitored throughout. When the strains reached levels suitable for endurance testing, the random response check would not proceed to the next acoustic load level. Careful response monitoring is of particular importance in setting the test levels for panel endurance runs. The strain and acoustic levels measured during these random response checks form the data base for the design method in Section IV. Endurance runs were then made at selected sound pressure levels until panel failure occurred. A target of



digure 24. Closeup of Panel Installation in the PW!

10 hours exposure time was set as a maximum. The intention in the endurance runs was to avoid rapid or protracted failure times and to obtain a good spread of fatigue life data. Panels that could not be failed within 10 hours at 165 dB were subsequently subjected to reduced bandwidth testing, with correspondingly higher acoustic spectrum levels. During endurance runs, panel gauges were continually monitored for changes in response (frequency or strain levels) indicative of structural failure. In addition, periodic visual inspections of the panels were made. First signs of visual damage were noted.

The panels often had slow progressive fiber failures, where the time from first visual damage to major damage affecting panel response was several hours. In such cases, both times were noted. Major damage was defined as any skin damage extending through the laminate thickness or fracture or separation of stiffeners from the skin in one of the center bays.

In addition to the basic tests described above, the following additional tests were carried out:

- (1) Testing identical panels in steel and aluminum fixture frames.
- (2) Testing a panel without a fixture frame and also rigidly bolted to the PWT.
- (3) Full depth vs. panned down closures on the honeycomb beam stiffeners.
- (4) Testing with and without the stiffeners clipped to the fixture frame.
- (5) Comparison between bonded and riveted skin to stiffener joints.

- (6) Switching panel positions in the two test windows.
- (7) Measuring response on one panel, with other test window open.
- (8) Same as above with hard wall installed in other test window.
- e. Data Reduction A Spectral Dynamics Digital Signal Processor, Model SD360 was used to perform all spectral analyses. The SD360 is a self contained fast fourier transform analyzer, capable of displaying and plotting, in real-time, the complex relationship of two signals, both in the time domain and the frequency domain. An analysis range of 1.2 KHz was selected, corresponding to a filter bandwidth of 2.16 Hz. The actual aliasing filter cutoff was 960 Hz. Overall sound pressure levels and rms strain levels were determined by converting the signal to a d.c. value proportional to its instantaneous rms value, integrating over a 20 second period, and reading the value on a digital voltmeter.

Frequency spectra were generated for all microphones and strain gauges at the endurance test sound pressure levels. Spectra were also generated at each sound pressure level (140 dB to 165 dB) for selected gauges. The strain gauges selected for spectral analysis over the full response range were the center biaxial pair (numbers 3 and 4) and the gauge near the zee radius (number 10). Overall rms levels were measured for all transducers at all sound pressure levels. Cross-spectral density measurements were made between corresponding strain gauges on adjacent bays. Integrated power spectral density plots were made for some panel gauges in order to determine the relative contributions of individual modes to the overall rms strain value.

f. Progressive-Wave Tube Test Results - The first panels to be tested were the existing panels, shown in Figure B-2. Tables 22 and 23 summarize the overall rms stress levels. Panels 1 and 5 have the same geometry, and offer a comparison between a graphite and an aluminum panel. The stresses on the graphite panel (5) ranged from 50-75 percent of the



TABLE 22 OVERALL RMS STRESS LEVELS FOR EXISTING PANELS 1, 5 and 4

	Ļ	165	-	•	-	2874	4027	•	1	•	'		-	4362	329€	'	-	ı	-	'	'			-
	Single Stiffener	160	-	'	,	2385	3464	1575	1715	1575	1648	'	'	3933	2767	-	-	-		'	-	-	'	'
	Single S	155	'	·	١	1642	2660	1112	1273	1166	1186	'	'	3002	1896	,	'	'	•	-	-	'	-	
	4 -	150	-	•	'	1012	1836	730	824	737	771	'	,	1111	1186	•	-	,	'	•	-	,	'	,
	Panel	145	-	·	'	657	1320	456	496	429	469	'	'	1635	784	٠	-	,	'	-	-	,	•	1
	inger	165	2291	2124	2198	1749	-	_	-	_	978	1675	1608	1742	871	•	1240	2010	938	1575	•	1997	2044	1983
/IN ²)	Skir-Stringer	160	1608	1461	1515	1119	,	+	717	1253	570	945	1079	1092	509	858	824	1407	563	858	1052	1474	1508	1139
ELS (LB	Graphite S	155	884	918	978	670	-	-	402	737	342	563	919	637	335	529	469	864	335	509	67.7	116	918	697
ESS LEV	5 - Gra	150	469	422	449	275	1	•	241	429	208	315	348	355	168	315	295	496	201	281	302	456	462	348
OVERALL RMS STRESS LEVELS (LB/IN ²)	Panel !	145	261	241	248	168		1	101	214	121	201	154	147	101	194	121	214	114	174	147	295	255	188
VERALL	inger	165		-		3200		ı	-		_		3000	-	1	-	1350	3600	-	'	1	-	4100	4700
Öl	kin-Str	160	2200		1	2040	1	,	,	-	-	-	2150	1970	٠	1	870	2920		_	-		3400	3200
	Aluminum Skin-Stringer	155	1380	•	1	1070	1	•	'	1750		-	1400	1350	1	-	50C	2000	'	-		_	1850	1700
	שוא - ו	150	720	-	_	700	-	•	'	1256	'	_	006	006	-	-	350	1300	-	_	-	-	1200	OVB
	Panel	145	430	•	•	470		,	1	92	,	-	200	500	,	•	200	750	1	-	,	1	720	573
	OASPL	Number (06)	_	2	8	4	5	9	7	8	6	10	11	12	13	14	15	16	17	81	19	20	21	22

TABLE 23 OVERALL RMS STRESS LEVELS FOR EXISTING PANEL 3, FLAT AND CURVED

- 1												
	hite	165	-	-	3015	-			1		2144	,
	Panel 3 - Unstiffened Graphite	091	-	_	3551	_			•		3015	4288
	stiffer	155	-	ı	2613	ı			•		2278	3886
	3 - Un	150	1575	1387	1876	١			1		1642	2814
	Panel	145	1059	951	1106	-			•		1039	1642
	ature	165	ı	ı	2680	5079			1		1	ı
	Panel 3 - With 30 Inch Curvature	160	3390	1742	1843	3350			1943		603	1045
	ch 30 Ir	155	2345	908	1206	2077			1139		342	570
	3 - Wit	150	1474	929	670	1306			610		214	275
	Panel	145	804	315	369	0/9			362		134	174
	OASPL (dR)	Gauge Number	-	2	8	4	ເກ	9	7	8	6	10

corresponding aluminum values (1) in the maximum stress direction (short direction). In the long direction (strain gauge 15) the stresses were comparable. Panel 4, which has four times the bay span as panel 5, shows a corresponding stress increase of from 2 to 4 times. The unstiffened panel (3) was tested both as a flat panel and with a curvature of 30-inches. The 165 dB data points may not be valid comparisons, since the panel was undergoing extremely large deflections at this high load. The 165 dB points may also represent the onset of failure. The center stresses were reduced to 1/3 to 1/2 of their original values due to curvature, whereas the edge stresses were reduced to 1/5 to 1/7 of their original values. The response of panels 1 and 5 were plotted against sound pressure levels in order to compare the degree of linear response between the aluminum and graphite panels. Figures 25 and 26 show the results. The dotted lines represent linear response. These graphs show both the aluminum and the graphite panels to be responding in a linear fashion. Figure 27 shows the graphite skin-stringer panel following sonic fatique failure. Figure 28 shows sections of honeycomb stiffeners with skin laminate fibers still attached. The time to failure for panel 5 was 15 minutes at 165 dB. Panels 3 and 4 lasted for 5 minutes.

These photographs show the mode of failure to be in the skin laminate at the stiffener locations. This shows that the secondary bond between the skin and stringers is superior to the interlamina bond strength, as it should be. This is because the adhesive strength in the laminate comes from the epoxy matrix material, which is selected for criteria other than just pure strength. Flow characteristics, for example, are very important when laying up a large surface area. The adhesives used to bond the skin and stringers together are chosen primarily for strength. Consequently, extensive fiber pull-out on failure is indicative of good bond quality. This mode of failure also indicates that the flatwise tension strength of the laminate may be a critical parameter in sonic fatigue resistance. This is a property that is not commonly measured or quoted in structural property specifications of composite laminates. This conclusion has considerable logical appeal, since stress concentrations and extra inertia

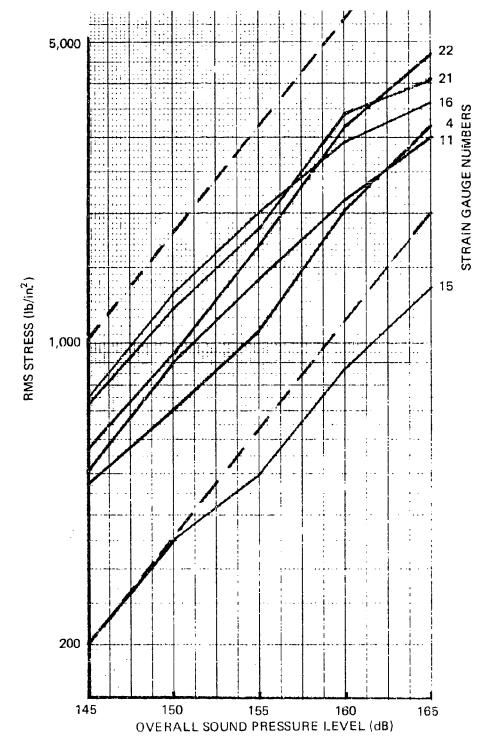


Figure 25. Panel 1 - Linear Response of Aluminum Skin-Stringer Panel

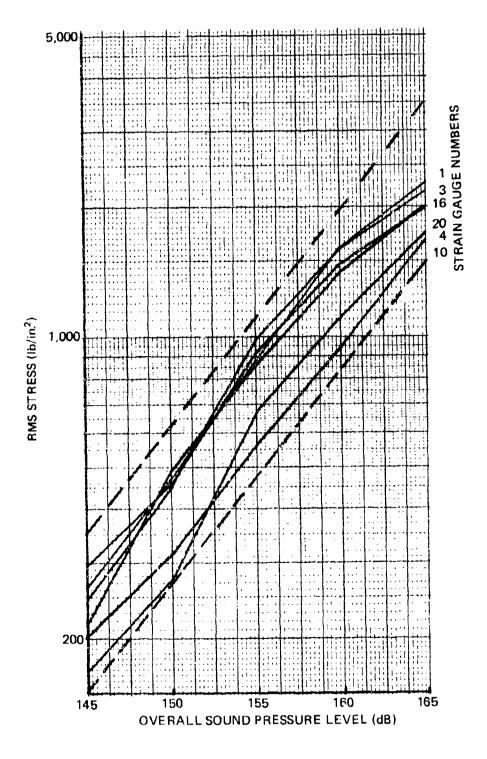


Figure 26. Panel 5 - Linear Response of Graphite Skin-Stringer Panel

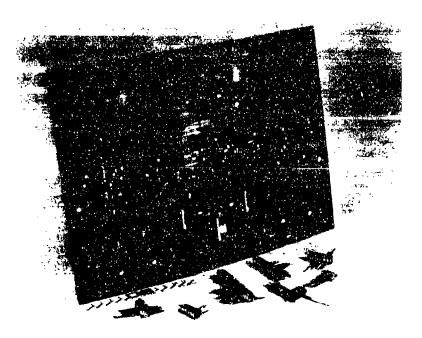


Figure 27. Rohr Panel No. 5 After Sonic Fatigue Failure



Figure 28. Sections of Failed Honeycomb Stiffener from Panel No. 5

forces are experienced by the surface laminate underneath the stiffeners during dynamic behavior. Since the interlamina strength will be the same between each lamina, failure will occur at the first bonded interface. This mode of failure also indicates that mechanically fastening the stiffeners to the skins may result in longer sonic fatigue life than using bonded stiffeners. This is because fasteners will distribute stresses across the whole skin laminate, rather than just into the surface laminate. As a result of these findings, it is recommended that flatwise tension tests be performed on composite skin laminates in the future. Such tests may provide valuable information in selecting the best resin systems and adhesives for sonic fatigue critical applications of advanced composites structures.

The next, and most important phase in the sonic fatigue test program, was to test the multi-bay panels shown in Figure B-1. These are the panel tests upon which the design method in Section IV was based. The first of these panels were fabricated prior to the resolution of the adhesive bonding problems, discussed in Section III.3. Some of these panels failed prematurely, with the stiffeners delaminating from the skins, with no fiber pull-out occurring. The response data for these panels is unaffected by the weak bond, but the times to failure are not representative of the panel's fatigue lives. The panels that had been fabricated with suspect bonds were: al, cl, fl, gl, i, kl, n and q. Panel al gave good response data up to 160 dB, but failed prematurely at 165 dB, with very slight skin damage. Since this was a configuration for which there was a planned duplicate panel (a2) yet to be made, there was no need to refabricate al. Panels cl and gl also had duplicate panels scheduled, and it was decided to rivet the suspect skin-stringer joints on panel g in order to provide a comparison between bonded and riveted joints. Panels i and kl failed prematurely with no skin damage occurring. These panels were subsequently riveted back together and retested in order to provide additional response comparisons between bonded and riveted specimens. Panels n and g gave good response data and failed with significant fibers being pulled from the skin laminate. Panel fl gave

good response data and did not fail after 9 hours at 165 dB. Figure 29 shows panel al following sonic fatigue failure. The skin-stringer joint areas show a mixture of weak bonding (white areas) with no attendant fiber pull-out and satisfactorily bonded areas with fiber pull-out occurring. Figure 30 shows panel n following sonic fatigue failure. Here the suspect bonding process does not seem to have resulted in a weak joint, and the failure shows extensive skin laminate damage. It should be pointed out that skin laminate damage is a desired mode of failure and represents a successful test. Figures 31 and 32 provide a good example of this desired mode of failure. They show the front and back faces respectively of panel p following sonic fatigue failure. In this case the skin-stiffener bond strength and the skin laminate quality are well demonstrated by the even distribution of the failure through the entire thickness of the skin laminate.

Table 24 gives the overall rms strain levels for those panels whose response data was subsequently used in the development of the design method. Corresponding response spectra are given in Appendix C. Omitted from this table are those panels whose purpose was to investigate specific effects, outside the main design method; such as the J stiffened panels, the honeycomb stiffened panels (e), panel m - the 8 x 1 array and panel c - which was designed to investigate the effects of ply orientation. Strains are given in microinches/inch for the following strain gauges: 3- center of bay, long direction; 4 - center of bay, short direction; and 10-edge, short direction, normal to longest side. Strain gauge 10 gave the highest measured strains for the majority of the panels, and represents the location of maximum interest in this program. At the panel centers, where the response strain magnitudes are

Figure 29. Panel al after Sonic Fatigue Testing

Figure 30. Panel n after Sonic Fatigue Testing



igure 31. Panel p after Sonic Fatigue Testing -- Back Face

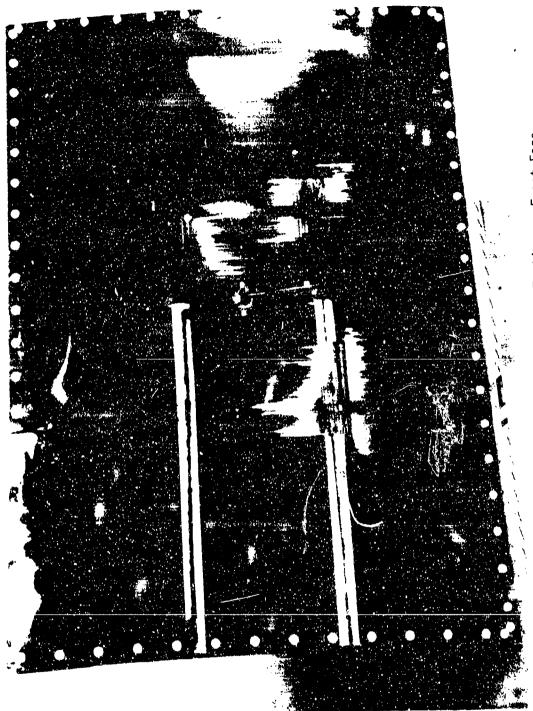


Figure 32. Panel p after Sonic Fatigue Testing -- Front Face

TABLE 24
OVERALL RMS STRAINS (MICROINCHES/INCH) USED IN THE DEVELOPMENT
OF THE DESIGN METHOD

		0[-agb3	Ų.	١	1	425	247	595	721	258	312	١.	283	١,	۱ ا	١.	446	
	8	i8-retneJ			342	417	120	204		293	200	,	161		,	١,	333	
	165	p-veines		1	412	416	152	299	,	325	503	•	197		,	,	348	
		Center-3			334	285	141	368	'	194	169	•	227	,	,	,	278	
		0[-96p3		114	482	274	154	400	466	168	216	295	179	85	'	312	265	
	gg B	i8-mainal		343	288	290	28	130	210	201	148	569	102	238	•	370	99	
	160	A-netneJ		338	337	284	103	205	276	226	151	322	124	249	,	381	†	315 302
		£-netne⊃		221	249	183	96	280	276	140	110	254	140	244	,	220	88	279
S		ე[-მწⴒე		342	358	174	78	250	586	133	137	112	109	355	455	202		262
EV	dB.	i8-natna∂		1	221	148	36	۳۶	121	172	1100	187	99	224	344	248	118	184
PRESSURE LEVFLS	155	₽-natnaJ		275	261	183	52	120	167	192	101	227	79;	234	354	255	129	190 193 184 262 279
RES		Center-3			199	113	19	149	187	117	1/	183	87	208	213	168	118	130
SOUND		Center-10		225	267	101	49	151	150	84	86	142	68	307	253	141	88	
- 1	dB G	i8-retnec		195	164	112	24	53	68	107	76	113	42	201	192	198	82	107 149
OVERALL	150	₽-yətna⊃		199	190	109	34	2	93	120	2	144	വ	209	198	203	6	
8		Center-3		149	135	67	39	73	<u>.</u>	75	47	133	53	181	124	127	78	211 701
İ	145 dB	01-9ըb3		161	147	57	8	93	5	47	59	34	43	266	116	93	62	-6
		i8-netas		144	96	88	18	31	45	56	48	75	28	177	83	132	53	65
		ħ-n9⊅n9∂		148	114	28	25	44	6	3	4	8	8	185	86	. 98	57	68
		6-retre2		113	85	39	27	42	62	42	8	7	뜅	191	57.1	95	48	63
	<u> </u>	0[-a6p3		102	11	34	22	5	54	92	2	53	28	13.7	96	28	4.4	84
	g	i8-nataa∂		87	55	32	5	12	27	92	23	44	2	124	2	83	25	35
1	149	4-retneo		9	65	33	2	29	38	8	33	23	ΞĮ.	5	72	83	38	38
		Center-3		69	49	26	22	m	39	25	24	44	24	141	45	54	E	37
•		eisat2 Roitsool	Panel Configuration	g	ç	p	y.	5	٤	-	i-j	ید		u	d	0	L.	S

comparable in both directions, it is necessary to combine their effects using the relationship

$$\varepsilon_{\text{rms}} = \frac{\varepsilon_{y}^{-v} \times y}{1 - v_{yx}} \frac{\varepsilon_{x}}{v_{xy}}$$
 (17)

where ϵ_y is from strain gauge 4 ϵ_x is from strain gauge 3

and ν_{XY} and ν_{YX} are from Tables 2 through 6. The resulting biaxial strains are also given in Table 24.

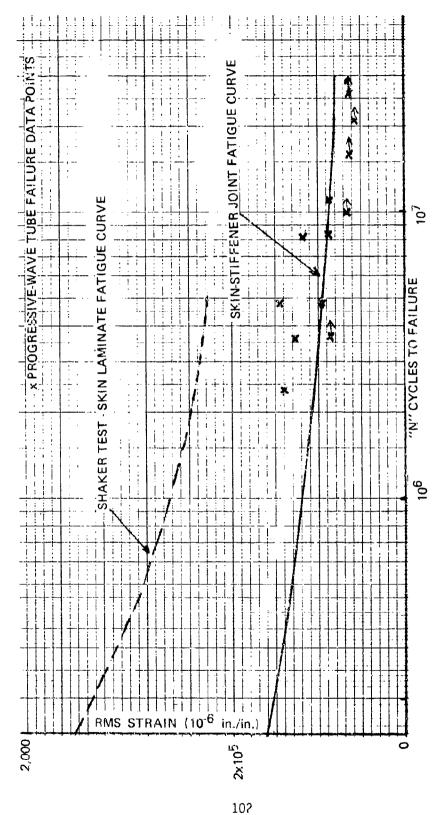
A detailed discussion of the results in Table 24, as they relate to the development of a design method, is given in Section IV. In general, the results show basic logical trends, such as decreasing strains with increasing skin laminate thickness; and increasing strains with both increasing stringer spacing and increasing radii of curvature. There are, however, several inconsistencies in the data; panel a is identical to panel b except for having fewer skin plies, yet it has lower edge strains than does panel b at the higher sound pressure levels. Panel n. which has even fewer skin plies, also has lower strains at the higher sound pressure levels. However, it should be remembered that the different skin laminates have different ply orientations, and consequently, different elastic modulii. Panels a and d have an elastic modulus of 7.5 x 10° $\frac{2}{16}$ Panel b has a value of 6.7 x $\frac{10}{10}$ and panel n has 9.4 x $\frac{10}{10}$. Although this program compared two different ply orientations for the same laminate thickness (panels b and c), this variable was not represented over a number of panels sufficient to permit its inclusion as a quantitative variable in the design method. Instead typical symmetric ply orientations were chosen, with the expectation that the resultant design method would be applicable to other similar laminates. This limitation should be remembered if radically different ply orientations are used in conjunction with the results of this program.



Although there were a few exceptions, the maximum strain response on the panels occurred at the center of, and normal to, the longest bay side, adjacent to the radius of the zee (strain gauge 10). This is as it should be, and also corresponds to the finite-element static analysis results.

The measured strains did not linearly increase with overall sound pressure level, but increased at a lower rate, which varied from panel to panel. It is not entirely clear whether or not this is indicative of nonlinear structural response. The response frequencies of the in-phase stringer-bending mode for the panels listed in Table 24 were given in Table 15, where they can be seen to correspond quite well to the fully-fixed frequencies calculated from Reference 5.

Fatigue lives, as expected, showed considerable scatter. Figure 33 shows the fatigue life data points for the multi-bay panels. The data points are shown superimposed on the shaker test fatigue data. The curve shows the strain endurance level to be approximately 400 microinches/inch. Taking a conservative line through the data, the curve for the skinstiffener joint appears to be approximately 42 percent of the shaker test curve for the skin laminate. This ratio is similar to that for riveted aluminum skin-stiffener panels. The lowest strain at which a panel failure occured (excluding the defective panels) was 411 microinches/inch, and that appears to be an outlier compared to the other data points. The next lowest failure strains were 444/446 microinches/inch, occurring at approximately 10^7 cycles. Virtually all of the panels (again excluding the defective panels) displayed the same failure mechanism. The first signs of failure were isolated failed skin fibers at the skin-stiffener joints. The number of failed fibers would gradually increase, often over a period of several hours, without having any effect on the panel response. Only when the damaged skin fibers had extended across nearly all of the skinstiffener joints was a change is response detected. This would usually be closely followed by a major failure of the skin laminate. This failure mechanism presents a problem in defining the effective fatigue lives of the panels. If the first visible sign of skin damage is the criterion



Strain vs. Cycles to Failure Sonic Fatigue Test Fatigue Curve: Figure 33.

j.

for failure, then the cluster of fatigue data points shown on Figure 33 in the 10^6 - 10^7 range would occur in the 5 x 10^5 to 10^6 range. Also, some panel fatigue data points shown as run-outs had very slight fiber damage. These effects would cause the assumed endurance level to drop from 400 to 300 microinches/inch. From a structural point of view, failure should be defined in terms of significant damage or a reduction in load carrying capability. On an actual aircraft, however, it seems likely that any structural component showing visible signs of damage would be removed, even if the damage were unlikely to propagate. Several sonic fatigue test panels exhibited a small number of fiber failures early during testing, but did not experience any damage propagation, even after several million more cycles.

Phase and cross-spectral density functions were generated between corresponding strain gauges in adjacent bays in order to identify the stringer-bending, in-phase mode. Figures 34 through 37 are for panel r (6 x 3, 6 ply, 60-inch radius). Figures 34 shows the sine sweep at the center of the center bay. Figures 35 and 36 show the random response spectra for the centers of two adjacent center bays. From these spectra it can be seen that the major response modes occur at 350-430 Hz and at 750-800 Hz. Figure 37 shows the corresponding phase relationship between the adjacent bays (top plot) and the associated cross-spectral density function (bottom plot). From this figure, it can be seen that the response in these two bays is coupled at the major response peaks (shown by peaks in the cross-spectral density function) and that the coupled response peaks at 360 Hz and 400 Hz are 180 deg. out of phase, whereas the response at 760-780 Hz is the in-phase mode. The cross-spectral density plots also assist in more precisely defining the coupled mode frequencies.

Another example of the value of phase and cross-spectral density functions in identifying response modes is shown in Figures 38, 39 and 40. Figures 38 and 39 show response spectra for adjacent bays. Figure 38 shows two distinct response peaks, at 240 Hz and 400 Hz, but Figure 39 only shows one peak, at 215 Hz. From these two plots alone, modal

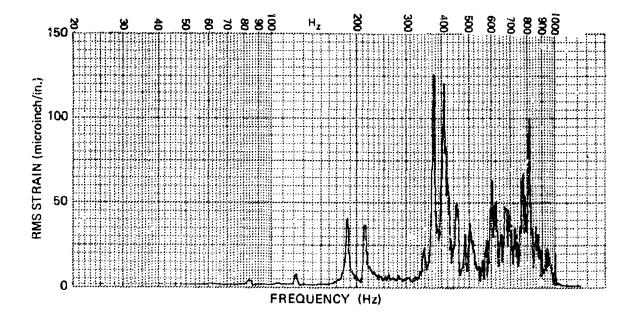


Figure 34. Sine Sweep - Panel r, Gauge 4

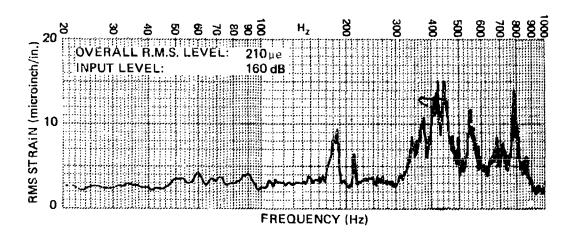


Figure 35. Random Response - Panel r, Gauge 4-1

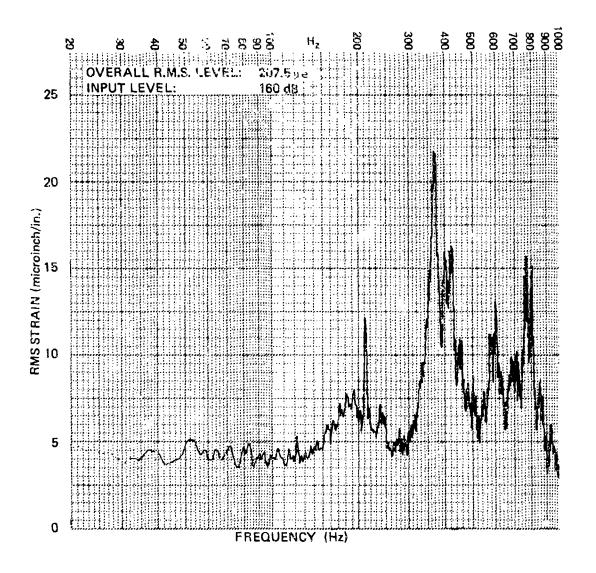


Figure 36. Random Response - Panel r, Gauge 4

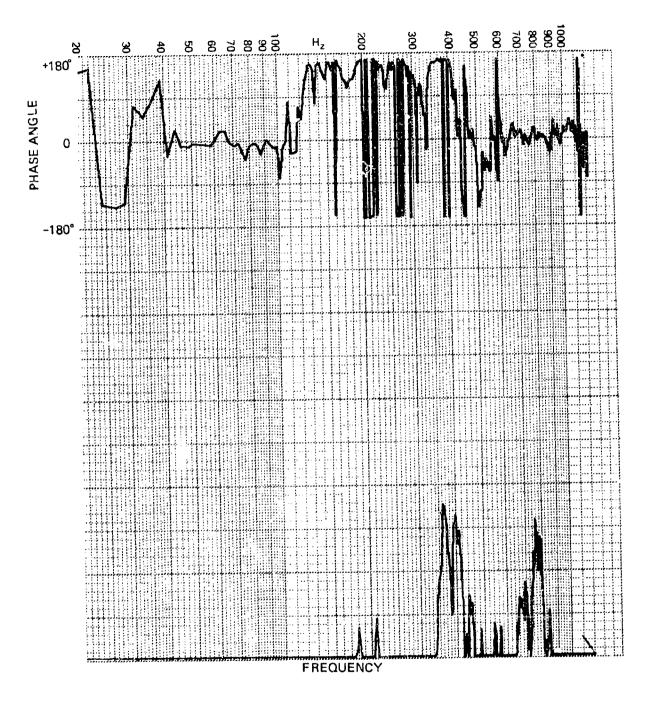


Figure 37. Phase and Cross Spectral Density - Panel r, Gauges 4 and 4-1

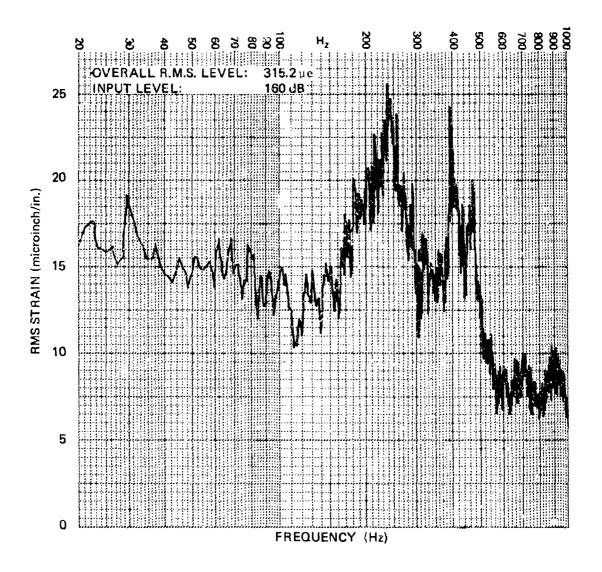


Figure 38. Ran'om Response - Panel s, Gauge 4-1

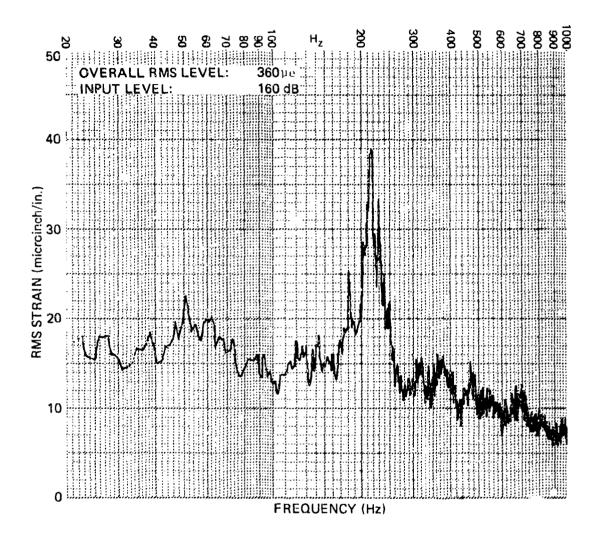


Figure 39. Random Response - Panel s, Gauge 4-2

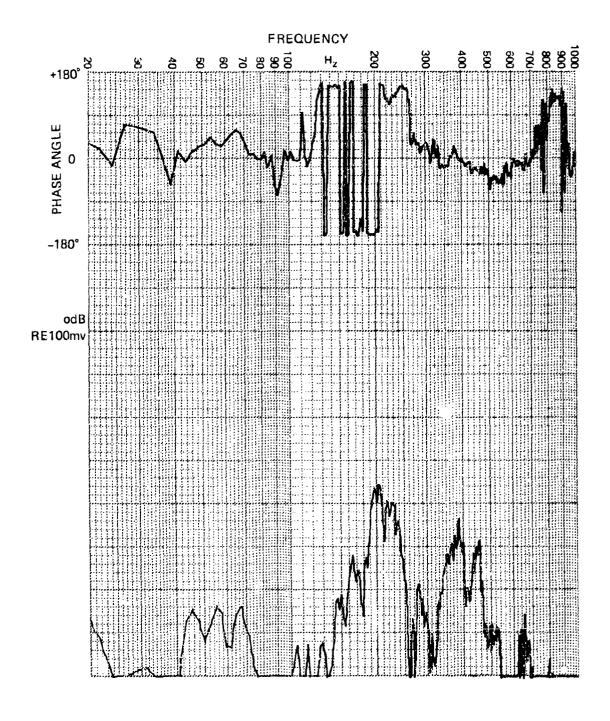


Figure 40. Phase and Cross Spectral Density - Panel s, Gauges 4-1 and 4-2

identification is not possible. Figure 40 shows the corresponding phase and cross-spectral density plots. The phase plot shows the 200 Hz region to be out-of-phase. But since the response spectra (Figures 38 and 39) do not show identical peak response frequencies, the cross-spectral density plot is required in order to identify the frequencies at which the response is coupled between the adjacent bays. Then it can be clearly seen that the out-of-phase mode occurs at 200 Hz and the in-phase mode occurs at 380 Hz.

Table 25 compares overall rms strain levels for Z and J stiffeners, and also between a quasi-isotropic laminate (b) and a more highly oriented laminate (c). Strains are given at the panel centers and at the edges, over a range of overall sound pressure levels. Figures 41 through 48 give corresponding strain spectra at 160 dB. The comparison between the Z and J stiffeners does not present a clear picture. At the panel centers, the strains are comparable for both stiffener types, although it can be seen that for the (b) panel at 160 dB and 165 dB, the J. stiffener resulted in higher strains than did the Z. Looking at the spectra on Figures 41 and 42 (note scale difference) it can be seen that the higher J stiffener strains are due primarily to the response peak at 275 Hz. The fundamental 170 Hz peak was reduced by the introduction of the J stiffener. The same comparison for panel c (Figures 43 and 44) also shows the J stiffener effecting a reduction in response at the fundamental mode frequency. In this case, without a significant increase in the amplitudes of the higher frequency modes. Corresponding comparisons of the edge strains show significant response reductions on panel b, but not on panel c. The corresponding spectra for panel b (Figures 45 and 46) show a 2:1 reduction in the peak response level due to the J stiffeners. Panel c also shows a reduction in the response of the first mode, but the increased response in the other modes results in an increase in the overall strain level. In general, it is clear that, compared to the Z stiffeners, the J stiffeners resulted in a lower response level for the fundamental stringer-bending mode, but had a tendency to stimulate the stringer-torsion mode at 280 Hz. Figure 49 shows the 160-170 Hz peak to be in-phase and the 270-280 Hz peak

RESPONSE STRAIN COMPARISONS BETWEEN Z AND J STIFFENERS AND BETWEEN $(0,\pm45,90)_{\rm S}$ AND $(0_2,\pm45)_{\rm S}$ PLY ORIENTATIONS

		Center Strain (Gauge 4)	rain 4)			Edge Strain (Gauge 10)	ain 0)	
	Panel b	a	Panel c	U	Panel b	þ	Panel c	Ç
Sound	(0, ±45, 90) _s	, 90) _s	$(0_2, \frac{+45}{2})_s$	45) _s	$(0, \pm 45, 90)_{s}$, 90) _s	$(0_2, \pm 45)_{\rm S}$	145) _S
Pressure Level	7	Ĵ	7	J	2	ŋ	Z	ت
140	65	49	57	65	22	53	57	61
145	114	109	901.	115	147	118	112	125
150	190	169	168	176	297	182	185	197
155	261	248	230	227	358	263	253	256
160	337	388	312	306	482	381	330	359
165	412	566	419	416		493	432	•

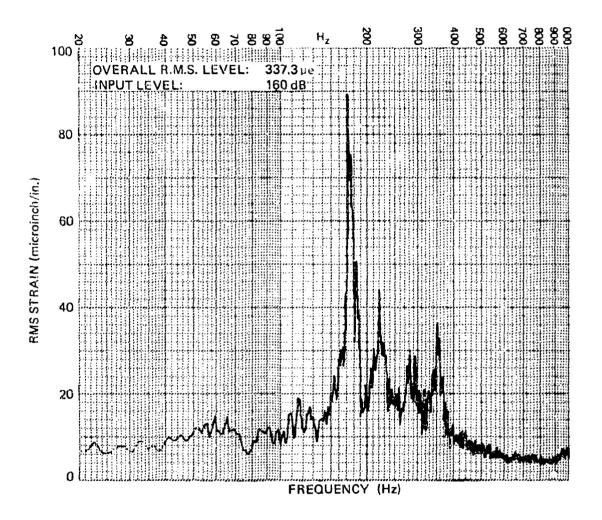


Figure 41. Center Strain - Panel b, Z Stiffener

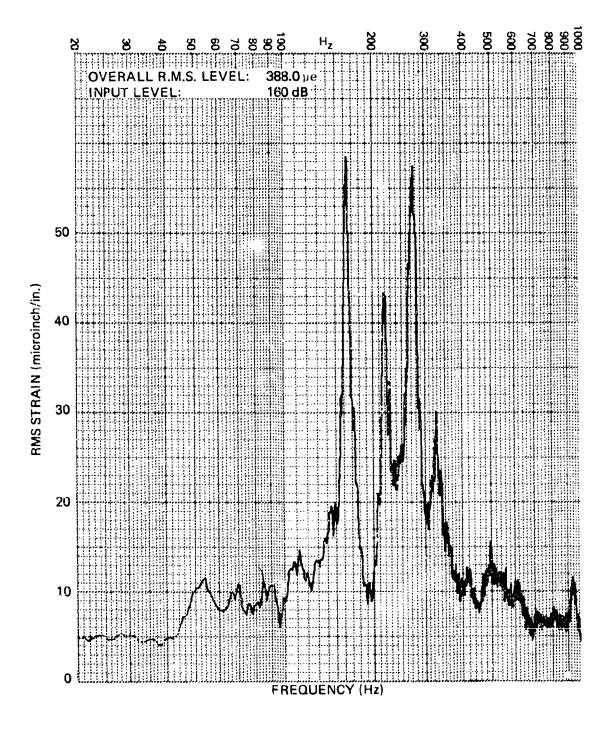


Figure 42. Center Strain - Panel b, J Stiffener

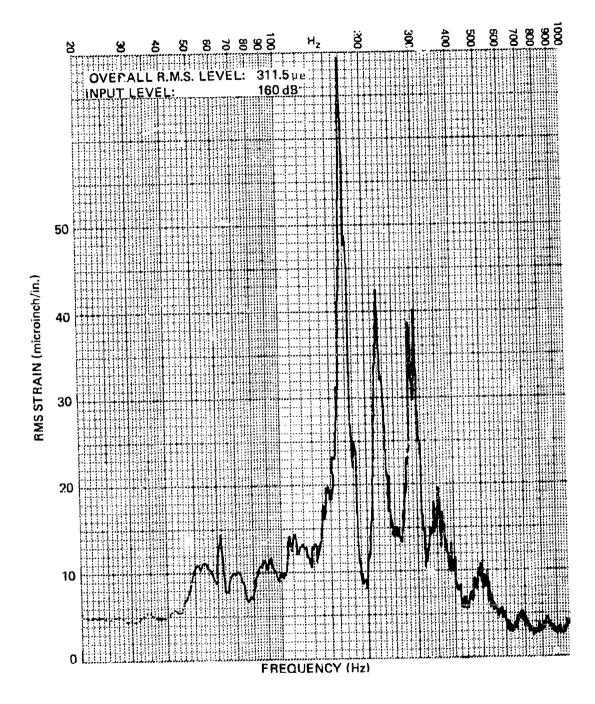


Figure 43. Center Strain - Panel c, Z Stiffener

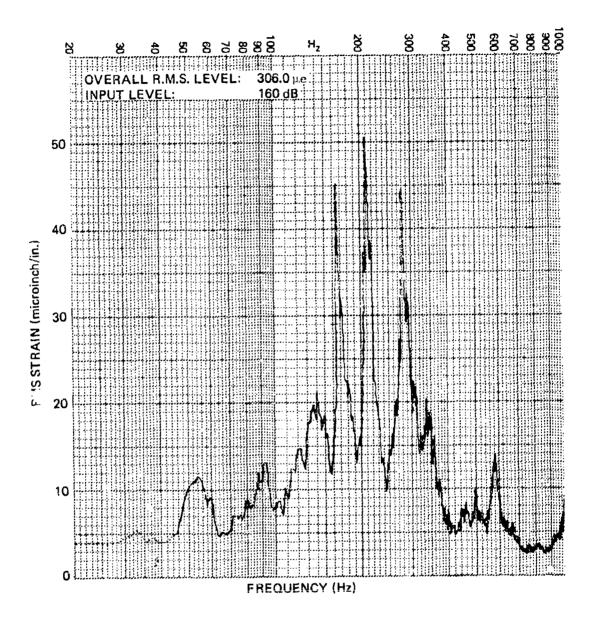


Figure 44. Center Strain - Panel c, J Stiffener

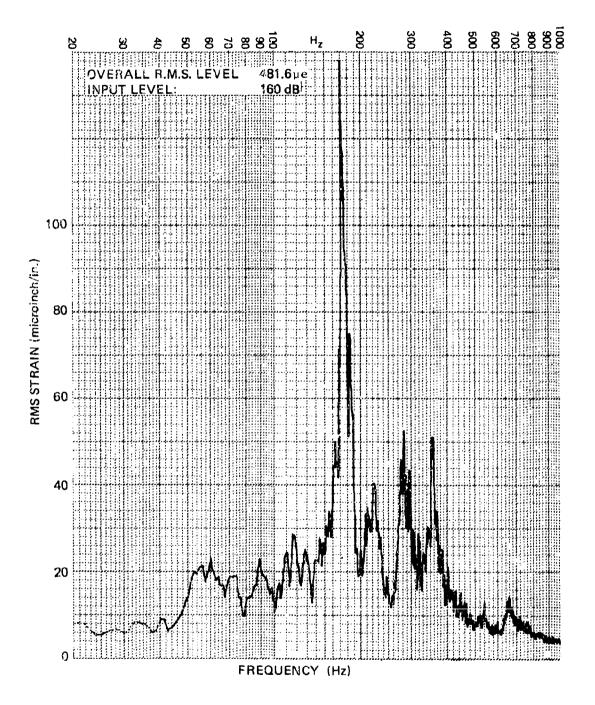


Figure 45. Edge Strain - Panel b, Z Stiffener

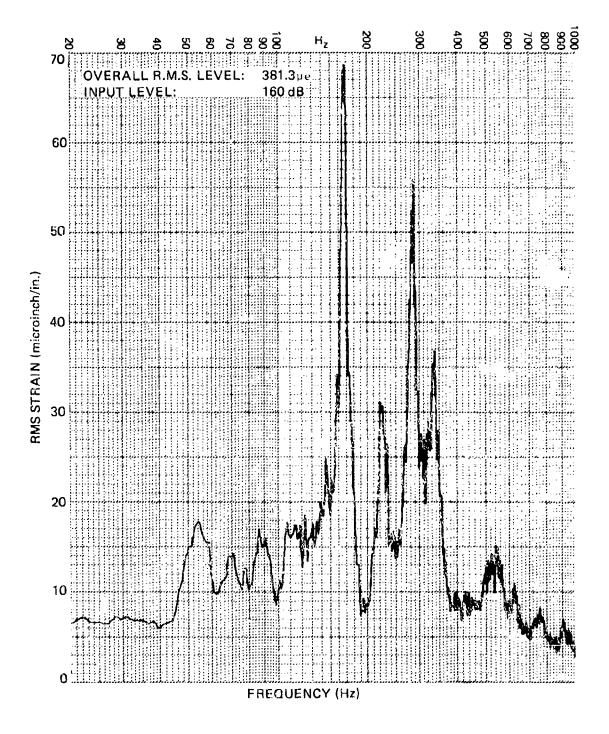


Figure 46. Edge Strain - Panel b, J Stiffener

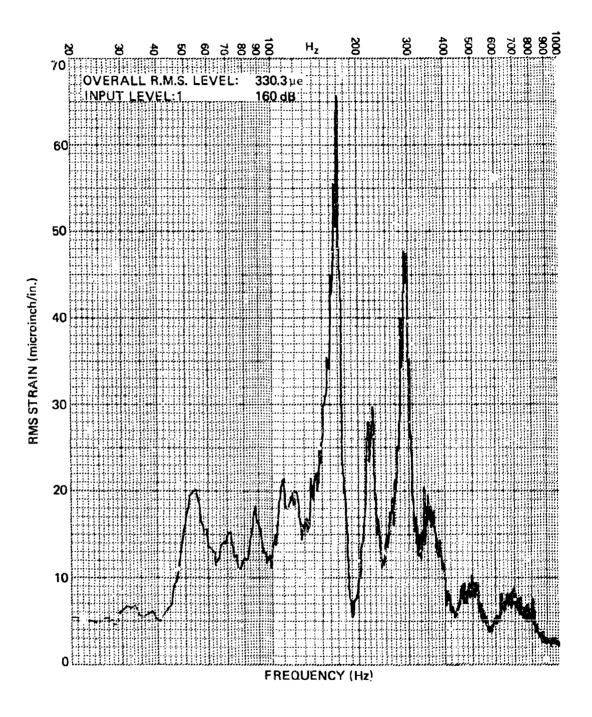


Figure 47. Edge Strain, Panel c, Z Stiffener

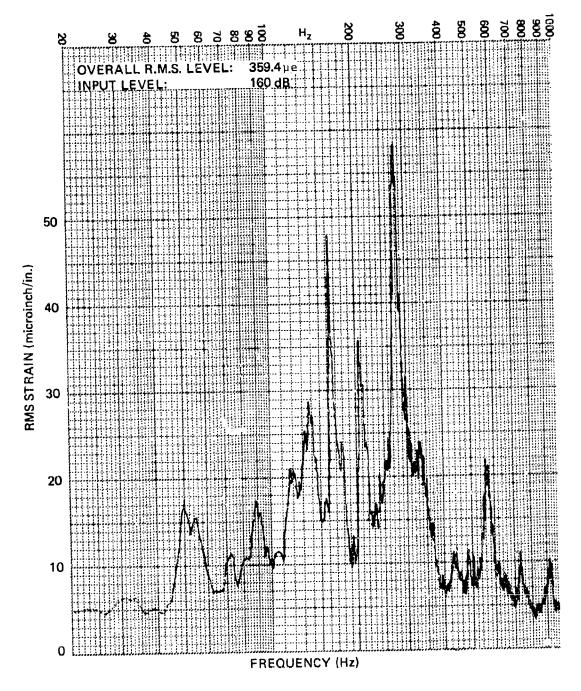


Figure 48. Edge Strain - Panel c, J Stiffener

FREQUENCY

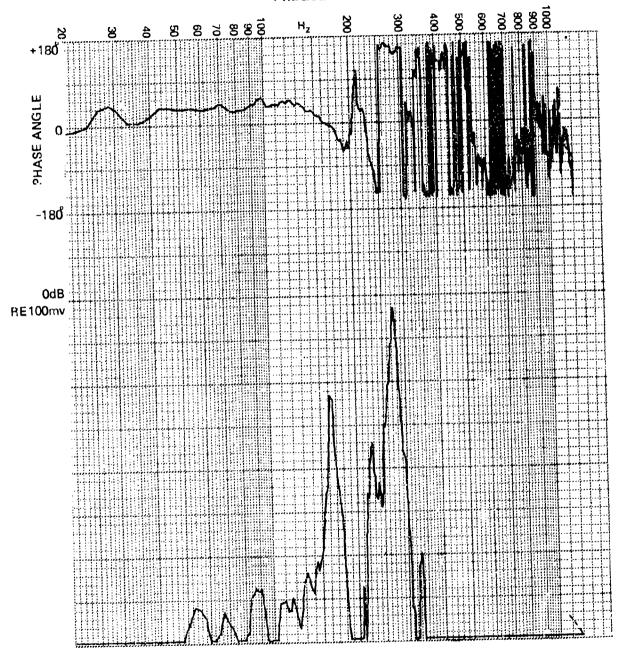


Figure 49. Phase and Cross Spectral Density for Panel b, J Stiffener, Gauges 4 and 28

120

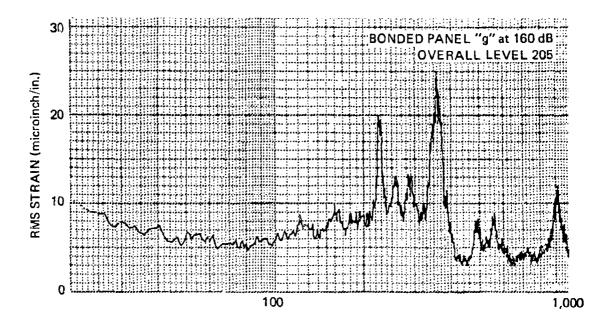
to be out-of-phase. The J-stiffened panels did, as expected, exhibit longer fatigue lives than did the Z-stiffened panels. For panel b, the J stiffener increased the fatigue life from 50 minutes (for the Z stiffener) to 7 hours. For panel c, the fatigue life increased from 1 hour to 17 hours. This large increase in fatigue life, without a major reduction in response was due to the increased bonded footprint area of the J compared to the Z. This results in more extensive fiber pull-out from the skin laminate upon failure, hence there is slower damage propagation and longer fatigue lives. Based on these results, the J configuration appears to be an attractive stiffener concept.

Table 25 and the corresponding spectra also provide for a comparison between the laminates used for panels b and c. The more highly oriented "c" laminate shows a significant reduction in response of the edge strains (approximately 25 percent). The center strains are similar for both laminates. However, the reduction in edge strain does not occur when using the J stiffener. The corresponding frequency spectra do not provide any additional information on the response difference between the two laminates. The difference between the two laminates involves taking two of the eight plies running in the lc | bay direction (90 deg., in the X direction) and running them in the short direction (0 deg., Y direction-between stringers). Looking at the overall results, it was concluded that these two laminates had comparable sonic fatigue resistance.

Three panel configurations (g, i and k) were used to compare the response of bonded and riveted joints. Table 26 summarizes the overall rms strain levels at the center and edge of the center bay of each panel. The differences between strains at the bay center do not appear to be significant. There is a tendency for the edge strains to be a little lower on the riveted panels than on the bonded panels, but the differences are neither large nor consistent. Figure 50 shows a comparison of response spectra for panel g at 160 dB. Although the overall levels differ (205 to 162 microinches/inch), the spectra are remarkably similar.

COMPARISON OF EVERALL RMS STRAIN LEVELS FOR BONDED AND RIVETED PANELS TABLE 26

	-				-		-	_			\neg	_	Т		
		- -	Dinotod	אואנובה	82		78		Ξ		194		279		413
		Panel k	3	Bondea	20		84		142		211		295		1
train	10,	.,-		Bonded Riveted Bonded	35		46		63		102		162		254
Edge Strain	(Gauge 1C)	Paneli		Bonded	26		47		84		133		168		528
				Bonded Riveted	50		7.6		127		204		317		503
		r load	מו	Bonded	15		õ	3	15.		250		400		585
			¥	Bonded Riveted	ū	5	7.6		-	2	199		797		408 809
			ranei K	Bonded	S	20	Ú	200	7 7 7	\$	227		200	7,7	
	Strain	÷	<u>, </u>	Riveted		40	i.	S.	}	80			27.7		335
	Center Strain	/+ =60ps	Panel	Rended		31	;	94	;	120			200	277	325
			5	Donated Privated Bonded Riveted	200	28	42		64		94		162		556
			Pane' q	Dondari	מבוסבו	29				70		97	300		562
			Sound	Pressure	revel	740		145		150		155		160	165



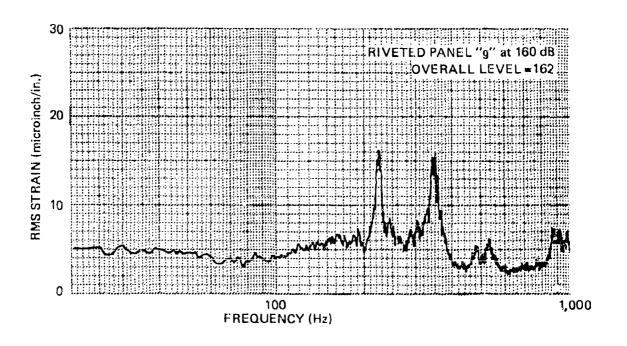


Figure 50. Comparison of Strain Spectrum for Bonded and Riveted Panels

Overall, it appears that the riveted joints do not significantly affect panel response. They do, however, affect the mode of failure. The riveted panels experienced partial failure in the Z radius adjacent to the skin, in addition to skin laminate failures. The fatigue lives of the riveted panels were not significantly longer than for the bonded panels with good quality joints. However, observations of damage propagation during testing indicated that heavier stiffeners and more rigid clipping at the stiffener intersections would result in longer fatigue life for the riveted panels. This is because the riveted panels experienced significant stiffener and clip damage prior to skin failure. This was not true of the bonded panels, where skin damage was the primary mode of failure. Another factor to bear in mind is that a slightly substandard bond is difficult to detect and may result in a highly premature fitigue failure. A slightly substandard rivet joint is detectable and will have a less severe affect on fatigue life.

Figure 51 shows the strain spectrum corresponding to the top spectrum on Figure 50, without the stiffener webs clipped to the fixture frame. Although the overall strain level increased from 205 to 240 microinches/inch, due to removing the clips, the spectra show this increased strain to be predominantly below 200 Hz. This indicates that providing proper attachments at the panel boundaries is desirable and reduces the low frequency overall panel motion.

Early testing of a curved panel in an aluminum fixture resulted in a fixture failure. Steel backup fixtures had been fabricated for such an eventuality, and consequently, it became necessary to determine whether or not the steel versus the aluminum fixtures affected panel response. Figure 52 shows the results of this comparison. As expected, no significant panel response effects were observed.

Early in the test program, several side experiments were performed in order to ensure that testing two panels simultaneously would not produce any unwanted response interrelationships. One of the panels was

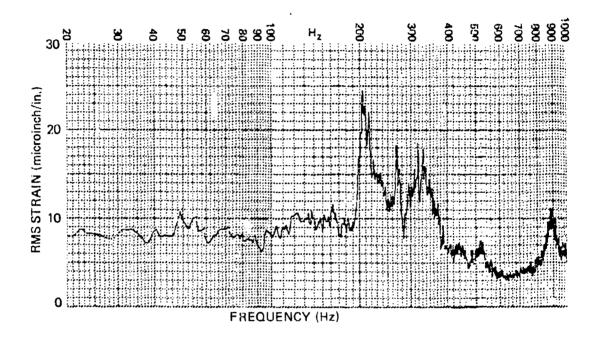


Figure F1. Strain Spectrum for Panel g-Stiffener Clips Not Attached, Gauge 4

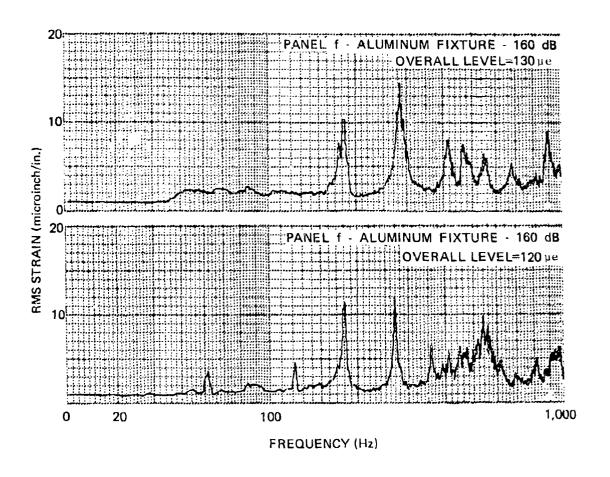


Figure 52. Comparison of Strain Spectrum for Aluminum and Steel Fixtures

concurrently tested in the top and bottom test windows, paired with different panels and also paired with a steel plate in the second test window. No significant effects on the panel responses were noted. The second test window was left open at one point and the only noticeable effect was a 2-3 dB drop in acoustic levels in the PWT. When the driver outputs were increased to bring up the acoustic level to that previously used, there was not noticeable change in the response characteristics of the test panels due to the open window.

In order to evaluate some boundary condition effects, panel d was tested for response under three different edge conditions. First, it was suspended in the test window without a fixture frame, i.e., with free edges. The fixture support wires supported the panel at the four corners only. Then the panel was bolted into the wall of the PWT, simulating fixed edge conditions. Finally, the panel was supported in the regular fixture frame and suspended on the fixture support wire, as used on the remaining panels. The effect of these different boundary conditions can be seen in Table 27. The overall rms strains show that the free edges result in lower response levels than when using the test fixture or fixed edges. When it was decided to perform the sonic fatigue tests using a picture-frame fixture, supported on wires, it was hoped that the response in the center bay would be the same as for fixed edges. The overall strains appear to confirm this. Figures 53, 54 and 55 show corresponding edge strain spectra at 165 dB for the three edge conditions. The stringer bending mode occurs at 340 Hz. This basic mode occurs with all three boundary conditions. The major response effects of the boundary conditions occur at 160-180 Hz and at 250 Hz. The modes at these frequencies do not occur when the panel is freely supported. If these extra modes were due to vibrations of the PWT wall, they would not occur when the panel is in the fixture frame, supported on wires unless the PWT variations were transmitted through the wire harness. If this were the case, the load-cell in the wire harness would detect them. Figure 56 shows the corresponding frequency spectrum for the load-cell. As can be clearly seen, there was no significant dynamic response occurring in the

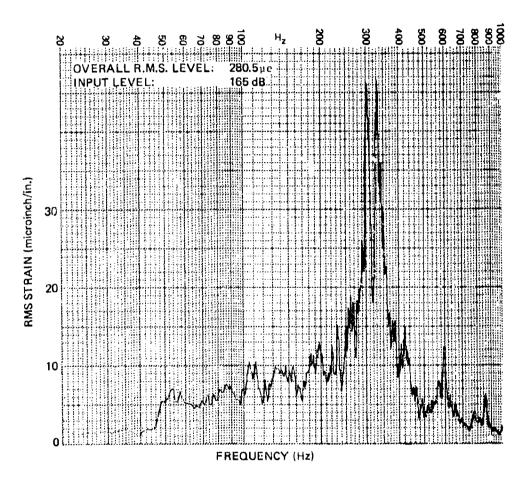


Figure 53. Response Spectrum for Panel d - Free Edges, Gauge 10

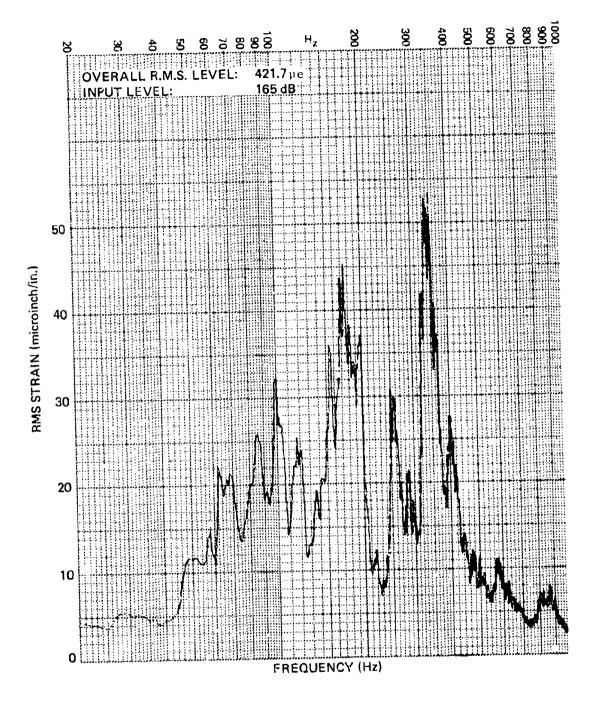


Figure 54. Response Spectrum for Panel d - Fixed Edges, Gauge 10

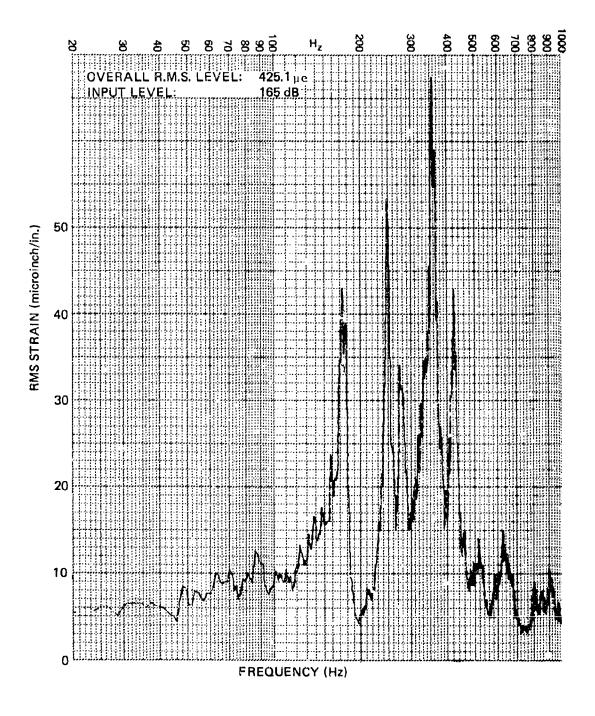


Figure 55. Response Spectrum for Panel d - Regular Test Fixture, Gauge 10

TABLE 27

OVERALL RMS STRAIN LEVELS (MICROINCHES/INCH) FOR PANEL "d" WITH DIFFERENT EDGE CONDITIONS

	Center	Strain (Edge S	Strain (Ga	
Sound Pressure Level (dB)	Free Edges	Fixed Edges	Edges Supported in Test Fixture	Free Edges	Fixed Edges	Edges Supported in Test Fixture
140	23	34	33	24	37	34
145	31	55	58	35	59	57
150	49	119	109	56	124	101
155	88	171	183	107	186	174
160	140	261	284	190	296	274
165	226	372	416	281	422	425

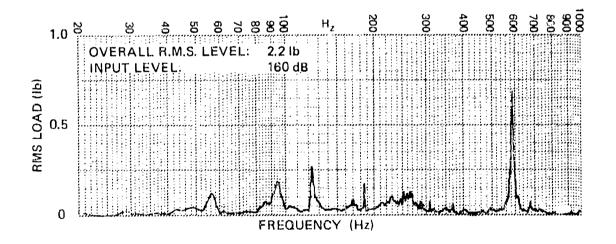


Figure 56. Load Cell Spectrum

wire harness supporting the panel fixture assembly. If the modes at the 160-18J Hz and 250 Hz were associated with the regular fixture frame, they would not have occurred when the panel was bolted to the PWT wall (for this test the panel was first removed from a fixture frame and then bolted directly to the PWT wall). The major response difference between the fixed edge conditions and the regular test fixture occurs at 100 HZ and below. The response peaks in this frequency region appear to be due to the effects of the PWT wall. Thus, the panel support system chosen for this test program appears to be structurally similar to the more typical method of bolting the panel to the PWT wall, without picking up PWT dynamic effects.

Two honeycomb beam stiffened panels, shown in Figure B-1, were tested and the results compared to an equivalent panel with Z stiffeners - panel b. The results are shown in Table 28. The first panel (e1) had panned down closures for the honeycomb stiffeners, as shown in Figure B-1. This panel failed in these closures after 1-1/2 minutes at 165 dB. The second panel (e2) was subsequently modified, replacing the existing panned down closures with full depth closures, clipped to the fixture in a similar fashion as the Z stiffener attachments. This panel failed after 5-10 minutes at 165 dB.

Although these times to failure seem short, the maximum strains on both panels were high, such that if superimposed on the fatigue curve on Figure 33, both panels appear to be on, or slightly above, the curve drawn for the Z-stiffened panels. The maximum strains on both el and e2 were higher than those shown in Table 28 (which are presented for comparison purposes), and occurred at the center of the shorter sides. It is not known why the honeycomb stiffened panels had different maximum reponse locations compared to the Z-stiffened panels. In any event, the comparison between the honeycomb and zee stiffeners was inconclusive. It does seem probable that the honeycomb stiffeners would have been more effective if the core material had had greater shear strength.

TABLE 28
COMPARISON OF OVERALL RMS STRIFFENED PANELS
AND Z STIFFENED PANELS

	Cei	Center Strain (Gauge 4)	uge 4)		Edge Strain (Gauge 10)	le 10)
	l	Stiffene	r Type		Stiffener Type	r Type
Sound Pressure		Honeycomb- Panned Down	ycomb- Honeycomb- ed Down Full Depth		Honeycomb- Panned Down	Honeycomb- Full Depth
Level (dB)	(P) (P)	Closure (el)	Closure (e2)	(q) Z	Closure (el)	Closure (e2)
140	65	56	74	77	65	94
145	114	103	129	147	134	166
150	190	189	207	267	245	287
155	261	262	261	358	343	382
160	337	350	385	482	455	521
165	412	440		1		ı

Ideally, a sonic farigue design method should be based on using acoustic spectrum levels to predict strain spectrum levels at corresponding frequencies. However, individual response spectrum levels usually vary inconsistently, compared to overall response levels, making them unsuitable for analysis purposes. An example of this is shown in Figure 57. The spectra shown are for the same strain gauge at 160 dB (top) and 165 dB (bottom). The overall rms strain level increased from 310 to 435 microinches/inch due to the 5 dB increase in acoustic load. However, the strain spectrum level at the major response mode (170 Hz) actually decreased slightly (from 82 to 68 microinches/inch). The increased overall strain level was due to increases in the strain response at other frequencies. Inconsistencies of this type make it impractical to use the strain spectrum levels in the development of the design method. This leads to a dilemma in the treatment of random strain data. Spectrum levels, with their narrow bandwidth, often vary unpredictably; whereas overall levels, with their wide bandwidth, include response that does not contribute to fatique. It has been suggested that 1/3-octave or 1-octave bandwidth measurements may provide the necessary stability without being influenced by superfluous data. Again referring to Figure 57, it can be seen that some of the increase in overall rms strain was due to the low amplitude strains in the 250-1,000 Hz region. This is quantitatively demonstrated in Figure 58. Superimposed on the power spectral density function, is the integrated power spectral density. From this plot it can be seen that the major response peak at 170 Hz contributes only about 20 percent of total power spectral density (mean square). Whereas the low amplitude response above 250 Hz accounts for 40 percent of the total spectral density. Based on this data, it might be thought that increasing the sound pressure level from 160 to 165 dB would not necessarily bring about a more rapid sonic fatigue failure. However, data taken during the test program clearly pointed to a definite relationship between the overall rms strains and fatigue failures, leading to the conclusion that some low amplitude strains that might be thought of as not contributing to fatigue failure do, in fact, make a significant contribution. As a

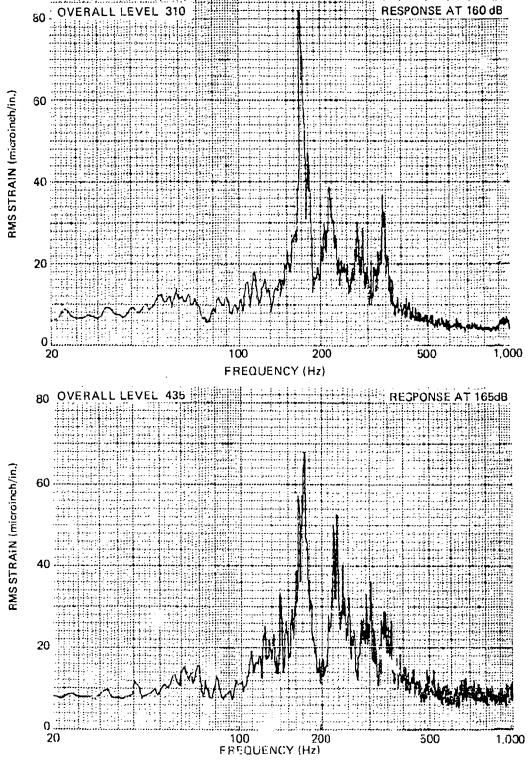


Figure 57. Comparison of Strain Spectrum at 160 dB and 165 dB (Panel b)

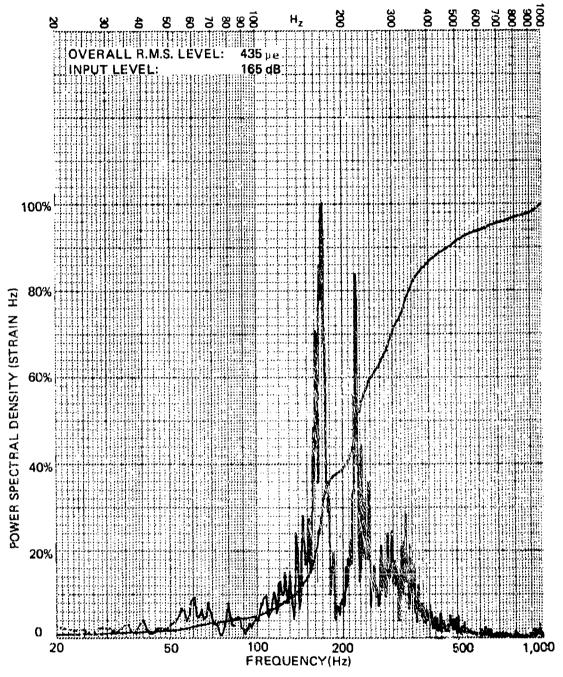


Figure 58. Integrated Power Spectral Density for Strain Response, for Panel b, Gauge 4

result, overall rms strains generated in the PWT test program were used in the development of the design method, described in Section IV.

Integrated power spectral density functions were generated for another purpose. The PWT had a tendency to generate an acoustic peak in the 150-180 Hz region (see Figures C-1 through C-6). It was found that this peak could be satisfactorily controlled by adjusting the bias voltage in the EPT 200 acoustic drivers. In most cases the peak did not significantly affect panel response; where it did, integrated PSD functions were used to quantify the effects. Figure 59 shows a situation where the response spectrum makes it appear as if the acoustic peak has produced a major response peak at 180 Hz. However, the integrated PSD curve shows that only 14 percent of the energy is contained within that peak. When converted to rms levels, this unwanted peak accounted for less than 10 percent of the overall rms strain level. In a situation where spurious peaks have a major effect on response levels, the integrated PSD function provides a quantitative tool for subtracting the effects out.

The strain spectra generated during the progressive-wave tube tests (contained in Appendix C) were used to determine damping ratios for various panels, using the "half power-point bandwidth" method. The damping ratio is found from the following relationship:

$$\zeta = \frac{\Delta f}{2f}$$

where

5 = Damping ratio

Af = Frequency bandwidth (Hz) at the half-amplitude point of major strain reponse peak

f = Center frequency of major strain response peak

The values obtained showed considerable scatter and did not show any significant correlation with strain response levels. Consequently, damping was not included as a design parameter in Section IV. Instead, the use of a typical value was recommended.

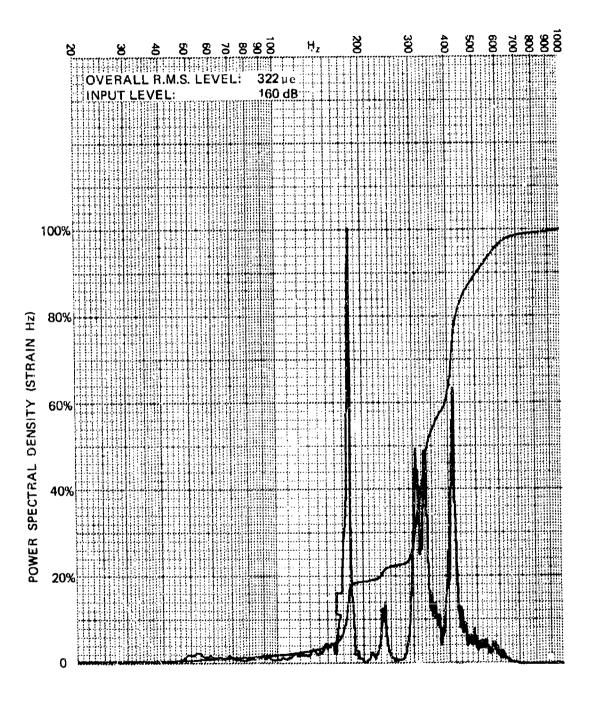


Figure 59. Integrated Power Spectral Density for Panel k, Gauge 4-1

Damping ratio values obtained ranged from 0.02 to 0.08. However, the higher values occurred when more than one response mode appeared to be contained within the major response peak. In those cases where the response peak was clearly a single mode only, damping ratio values were typically 0.02 to 0.03. These damping values were compared to values obtained in Reference 2 for aluminum skin-stringer structures. Reference 2 quotes values of 0.010 to 0.018 using the "logarithmic decrement" method. However, when the "half power-point" method was used on response spectra in Reference 2, values in the region of 0.05 were obtained. Based on these observations, it was concluded that the damping characteristics of graphite and aluminum panels do not significantly differ.

Some further discussion of the progressive-wave tube test results, as they relate to the development of the design method, is contained in Section IV.

SECTION IV DEVELOPMENT OF DESIGN METHOD

1. INTRODUCTION

The primary objective of this phase of the program was to utilize the analytical and experimental results to develop a practical semi-empirical sonic fatique design method for graphite-epoxy skin-stringer panels. Measured random strains from the sonic fatigue tests were compared to those calculated from Miles' equation (1), using as inputs the static strains calculated from the finite-element analyses. The test results were also compared to values determined from the AGARD nomographs $^{(5)}$ for fully-fixed edge conditions. Finally, multiple stepwise regression analyses were performed to develop empirical relationships between the measured strains and frequencies and various combinations of panel configuration parameters and finite-element analysis results. From these regression analyses, design equations were developed and a design nomograph constructed. A worked example is also presented. Section IV.5 presents the design method and nomographs as a self-contained unit. capable of being used independently of the remainder of this report. Appendix C contains the test data (overall acoustic and strain levels and spectra) used in the development of the design method.

An early problem encountered in the development of the design method involved the use of acoustic spectrum levels as loads. In Paragraph III.5.f, reasons for not using strain spectrum levels were given. The main reason is that although the response spectrum levels show

logical overall trends, the individual variations from one data point to another are too large and unpredictable for use in developing a design method. Acoustic spectrum levels, however, while exhibiting a certain degree of unpredictable variation, are sometimes consistent enough to facilitate their use as the load function. However, in this program the acoustic spectrum levels varied in such a way as to invalidate their use as a regression variable. Figures C-2 through C-7 show the test acoustic spectra. These spectra correspond to flat, 1/3-octave spectra. Consequently, the spectrum levels (1 Hz bandwidths) decrease with increasing frequency. Since panel frequencies increase with panel stiffness, the stiffer panels were effectively tested at lower acoust'c spectrum levels. This resulted in a high degree of interdependence between the acoustic spectrum levels and the panel configuration parameters, thereby violating the necessary assumption of independent variables. A problem similar to this was encountered in Reference 3. In that case the problem was overcome by dividing the load into the dependent variable (measured rms strain). When that was attempted in this program, the resulting regression equations showed good accuracy and satisfied all the usual statistical requirements (F-values, t-values, Durbin-Watson statistics, etc.). However, when these equations were used on combinations of panel configurations other than those used in the test program, it was found that the equations were numerically dominated by changes in the acoustic spectrum levels, and were not sufficiently responsive to changes in panel dimensions. When comparing responses between two very different panels, the stiffer panel had a much lower response and a lower acoustic spectrum level at the major response frequency than did the less stiff panel. The regression analysis largely attributed the lower response to the reduced acoustic spectrum level, rather than to the increased panel stiffness. However, a review of the integrated power spectral density plots showed that the major response peaks, associated with the pertinent acoustic spectrum levels, usually accounted for less than 25 percent of the overall strain response. Thus, since the overall sound pressure levels did not vary from panel to panel, as did the acoustic spectrum levels, the reduced response of the stiffer

panels was, in fact, due largely to the changes in panel configuration parameters. Consequently, regression analyses using the overall sound pressure levels as the load function, resulted in acceptable design equations.

2. SUMMARY OF ANALYTICAL AND EXPERIMENTAL RESULTS

RMS stresses and frequencies calculated using the AGARD nomographs $^{(5)}$ were given in Table 9. The static strains and stringer-bending mode frequencies, analytically determined from the finite-element models and the NASTRAN computer program, were given in Tables 11 and 15, respectively. Table 15 also listed frequencies calculated from the AGARD nomograph, Lin's equations and those measured during the progressivewave tube tests. The rms strains measured during the progressive-wave tube tests that are pertinent to the design method were given in Table 24. Table 29 contains calculated and measured frequencies, static strains, rms strains calculated using Miles' equation and measured rms strains. These are the data subsequently used in the regression analyses. For the reasons given in Paragraph I1.5.d, the frequencies computed from the finite-element models were not used for the design method. The strains calculated using Miles' equation have very high values, compared to the test strains. This was expected and is due to using the overall sound pressure level rather than the spectrum level as the load, for the reasons given in Section IV.1. The only purpose of generating these calculated strains was to determine if there was a consistent relationship between them and the measured strains.

3. REGRESSION ANALYSIS

Regression analysis is a statistical method for investigating functional relationships between variables, based on sample data. It is particularly suitable when the data are imprecise and there is a need to determine optimum relationships. The basic approach is to use samples of data to calculate an estimate of a proposed relationship and then to evaluate the fit using statistics such as "F" and "T."

TABLE 29
SUMMARY OF ANALYTICAL AND EXPERIMENTAL RESULTS

Overa11	ains* Edge	102	161	225	342	4:1	11	147	267	358	482	•	34	57	101	1,74	274	425
Measured Overall	Center Ed	87	144	195	ı	343	55	96	164	221	288	342	32	28	112	148	290	417
	Calculated RMS Strains ↑ *	8,785	15,753	27,871	49,379	87,852	5,933	10,639	18,823	33,349	59,334	105,574	3,315	5,945	10,518	18,635	33,154	58,993
Overall Sound Pressure	Level dB	140	145	150	155	160	140	145	150	155	160	165	140	145	150	155	160	165
	trains* Edge	3,522					2,117						958					
	Static Strains* Center Edge	1,439					863		_				327					
es (Hz)	Measured (PWT)	143					170						340					
Frequencie	Calculated (AGARD)	160					202						308					
Panel	Configur- ation	กซ					د						ъ					

* Microinches/inch

 $[\]dot{\tau}$ RMS strains calculated from Miles' Equation using computed static strains and fully fixed frequencies.

TABLE 29 SUMMARY OF ANALYTICAL AND EXPERIMENTAL KESULTS - Continued

and the common of the common o

Overal1	rains*	Edge	22	30	49	78	154	247	51	93	151	250	400	595	24	101	150	586	466	721	56	47	84	133	168	258
Measured Overal	RMS Strains*	Center	15	18	24	36	81	120	21	31	53	81	130	204	27	46	68	121	210		56	26	107	172	201	293
	70	RMS Strains +*	158	284	503	891	1,585	2,821	1,131	2,028	3,588	6,357	11,311	20,126	3,203	5,745	10,164	18,008	32,039	57,008	2,897	5,195	9,192	16,287	28,976	51,559
Overall Sound Pressure	Leveï	ф	140	145	150	155	160	165	140	145	150	155	160	165	140	145	150	155	160	165	140	145	150	155	160	165
	Static Strains*	Edge	28						254						839						995					
	Static	Center	13						110						312						146					
es (Hz)	اقوا	(PWT)	505						350					-	390						008					
	Sa	_	825						510						375						674					
Panel	Configura-	ation	4-						מ						٦											

TABLE 29 SUMMARY CF ANALYTICAL AND EXPERIMENTAL RESULTS - Continued

Overall ains*	Eage	41	59	98	137	216	312	05	34	142	211	295	28	43	89	109	179	283	187	566	307	355	408
Measured Overall RMS Strains*	Lenter	37	48	70	100	148	200	44	75	113	187	565	20	28	42	99	102	161	124	177	201	224	238
Calculated	Strains =	1,200	2,151	3,807	6,745	12,000	21,352	4,521	8,107	14,343	25,412	45,212	1,164	2,087	3,693	6,543	11,640	20,712	13,291	23,833	42,167	74,709	132,918
Overali Sound Pressure Level	dB	140	145	150	155	160	165	140	145	150	155	160	140	145	150	155	160	165	140	145	150	155	160
Strains*	Edge	212						1,298					235						6,153	•			
ان ا	Center	9/						480					96						2,793				
S (HZ) Measured	(PWT)	950						380					680				-		140				
Frequencies Calculated M	(AGARD)	824						312	1				631						120				
Panel Configur-		į	,					يد.	:				-	•					Ľ				

6.

TABLE 29 SUMMARY OF ANALYTICAL AND EXPERIMENTAL RESULTS - Concluded

Ľ,

Overall ains* Edge	96 116 253 455	58 93 141 202 312	44 62 108 160 265 446	48 91 149 262 444
Measured Overall RMS Strains* Center Edge	70 83 192 344	83 132 198 248 370	34 53 85 118 190	35 65 107 184 302
Calculated RMS Strains **	2,029 3,639 6,438	5,754 10,319 18,256 32,346 57,548	1,152 2,066 3,656 6,478 11,525	1,494 2,647 4,709
Overall Sound Pressure Level dB	140 145 150	140 145 150 155	145 145 150 160 160	145 145 150 155 160
trains* Edge	530	1,443	209	83
Static Strains* Center Edg	290	545	82	38
as (Hz) Measured (PWT)	180	370	780	380
Frequencies Calculated M	377	409	782	85 85 8
Panel Configur- ation	۵	σ	<u>s</u>	ω ₁

The regression analyses performed in this section utilized a modified multiple-stepwise regression computer program. Stepwise regression involves a forward selection procedure for the independent variables, with the provision for eliminating variables, as in backward elimination procedures. The program analyzes the relationship between a dependent variable (measured overall rms strains) and a set of independent variables (panel configuration parameters). The independent variables are selected in order of importance for entering into the regression, based on the reduction of sums of squares. The user can override this feature and enter the independent variables in any chosen sequence. The program has six algebraic transformations available, as follows:

Linear
$$y = a + b_1x_1 + b_2x_2 + \dots b_nx_n$$

Log $y = a + b_nx_n$

Log $y = a + b_n \log x_n$
 $y = a + b_nx_n + c_nx_n$
 $1/y = a + b_nx_n$
 $y = a + b_nx_n$
 $y = a + b_nx_n$
 $y = a + b_nx_n$

where y is the dependent variable and x_1 , and x_2 ... x_n are the independent variables.

For each variable entered the program computes the mean values, standard deviations and cross-correlation coefficients. For each step in the regression analysis, the program computes and lists the following:

Sum of Squares Reduced: This is an indication of the amount of points summed around a mean value line for a certain step.

Proportion Reduced:

Indication of how well a variable explains the regression at a certain step.

Cumulative Sum of Squares Reduced:

Indication of how much the dependent variable correlates with the independent variables entered at that point.

Cumulative Proportion Reduced:

Indication of how well the independent variables explain the regression at that step.

Multiple Correlation Coefficient:

Indication of how much the dependent variable correlates with the independent variables entered at that point.

F-Value:

A measure of the scattering of values about the mean accounted for by the regression. It is used in conjunction with F-tables to determine the degree of fit of the regression equation.

Standard Error of Estimate:

A measure of the dispersion of the observed points about the regression equation. It is in fact the "standard deviation of the residuals."

Regression

Coefficients:

Coefficients of the regression

equation.

Standard Error of

Regression

Coefficients:

Indication of the confidence level for the regression coefficients.

T-Values:

Ratio of intercept to standard error of regression coefficient. It is used in conjunction with T-tables to determine the accuracy of the corresponding regression coefficient.

Table of Residuals:

Difference between actual and estimated values for the dependent

variable.

Durbin-Watson

Statistic:

Test for lack of autocorrelation between error terms. A bad statistic is indicative of an independent

variable being omitted.

Von-Neumann's Ratio:

The ratio of the mean-square

successive difference to the variance.

The following is a description of the sequence of regression operations with examples of compute, program outputs used to develop the rms strain nomograph in Section IV.5:

The input data were of the form

$$\left(\frac{\epsilon_{\text{rms}}}{\text{SPL}}\right) = F(b, t, R)$$
 (18)

where [©]rms is the overall rms strain from strain gauge 10, i.e., the maximum edge strain.

SPL is the test overall sound pressure level in lb/in corresponding to the strain value.

b is the stringer spacing in inches.

t is the skin laminate thickness in thousandths of an inch, and

R is the radius of curvature in inches.

Table 30 lists the input data in the order (left to right) b, t, R and $\left(\frac{\epsilon rms}{SPL}\right)$. At the bottom of the table are the means and standard deviations of the input data. An explanation of the R = 150 value is given later in this section.

The program then computes the cross-correlation coefficients between the variables, giving the output in the form of a correlation matrix. This is shown at the top of Table 31. Regression then proceeds with the linear form of the regression equation: $y = a + b_n x_n$. Each variable is entered in turn and a corresponding regression coefficient determined. The program also computes at each stage the parameters shown on the remainder of Table 31. Three sets of statistics are shown, one for each of the independent variables. The bottom set represents the final linear equation, which may be written:

$$\left(\frac{\varepsilon_{\text{rms}}}{\text{SPL}}\right)$$
 = 224.0 + 358.2 b -51.65 t + 11.22R (19)

The program then used this equation to calculate a set of estimated values for the dependent variable $\left(\frac{\varepsilon_{rms}}{SPL}\right)$. The results are shown in Table 32. As can be clearly seen from the percent deviation column, the linear equation does not have acceptable accuracy. The average deviation is given as 40 percent.

TABLE 30
REGRESSION INPUT DATA

TI 电影响	######################################	000 000 000 000 000 000 000 000 000 00		Y = 800 2005-500 2028-80
INPUT CARD #	556 4.00 558 4.00 559 6.00 550 6.00 601 6.00	000 33.00 000 33.00 000 33.00 000 33.00 000 4.00 000 4.00	0 60.000 0 80.000 0 80.000 0 60.000 0 30.000	1186200 1172.800 980300 915200 863500 1744200 1619500 1532400
3 10	MEAN 6-61290 2-22581 2-09677 6-95666 1	STANDARD DEVIATION 1.64322 14.66279 47.49934		

TABLE 31

REGRESSION RESULTS FOR LINEAR EQUATION

CORRELATION MA		(RMS)	
ROW 1 b 1.00000	t R 0-22549 -0-1343	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	
ROW 4 0-24349	1.00000 0.1478	3 -0.50589	
ROM 3 -0.13435	0.14783 1.6006	0.31608	
ROW 4 0.32089	-0.50589 J.31se		
VARIABLE ENTERED		1100000	
SUM OF SQUARES REDUCED PROPORTION REDUCED IN	IN THIS STEP 18	178738 - 145 0 - 256	
CUMULATIVE SUM OF SQUA SUMULATIVE PROPORTION	KES REDUCEU 18 REDUCES	1787±8.145 0.256 UF	71031620.831
FOR 1 VARIABLES ENTER MULTIPLE CORRELATION (ADJUSTED FOR O F-VALUE FOR ANALYSIS STANDARD ERROR OF ES (ADJUSTED FOR D	COEFFICIENT U FI I I I I I I I I I I I I I I I I I I	• 206 • 506 • 627 • 553 • 553	
VARIABLE REGRESS NUMBER CUEFFIC 2 -37 42306 INTERCEPT 3129.5514	3041 6.19553	T-VALUE	
VARIABLE ENTERED	1		
SUM OF SQUARES REDUCE PROPORTION RE UCEU IN	O IN THIS STEP 19 THIS STEP	156919.001 0.199	
CUMULATIVE SUM OF SCU CUMULATIVE PROPORTION	ARES REDUCED 32 REDUCED 32	337657.746 0.455 OF	71031020-831
FOR 2 VARIABLES ENTE MULTIPLE CORRELATION	N COEFFICIENT	2.675	
F-VALUE FOR ANALYSI STANDARD ERROR OF E	S OF VARIANCE 20 STIMATE	J.468 4.654 9.633 6.554	
VARIABLE REGRES	SION STD. ERRUR (CIENT REG. COEFF	GF COMPUTED	
2 -44.835 1 300.945 INTERCEPT 1460.656	6883C 7.2564° 33129 64.7651°	-6.177 4.040	
VARIABLE ENTERED	3		
SUM OF SQUARES REDUCED IN	IN THIS STEP AC	0423886.655 0.231	
CUMULATIVE SUM OF SEUM CUMULATIVE PROPORTION	AREC DEMISER	751744.401	71031620.831
STANDARD FRROM OF H	N COEFFILIENT (CARTANCE (CARTANCE 42)	-829 -822 -331 -851 -000	
VARIABLE REGRES: NUMBER CUEFFIC 2 -51.654(1 35b-228) 3 11.216(INTERCEPT 224.016)	ILENT REG. CUEFF. 35640 5.65092 11376 50.32665 52906 1.71303	T-VALUE -9.141 7.118	

TABLE 32
TABLE OF RESIDUALS FOR LINEAR REGRESSION EQUATION

	TABLE UF	RESIDUALS		
CASE NO.	Y VALUÉ 3506-80060	Y ESTIMATE 3067.7233	KESIUUAL +39.07445	% DEVIATION 12.52000
	2605.5J000	2499.52213	162.97787	6-44689
3	2826.80000 2900.0000	2499.52213 2499.52213	329.27787 400.47787	11.84020 13.80958
5	2194.50000 1155.2000	2499.52213 1365.11529	-365.02213 -207.91529	-13.89939
6	1155.20000 1094.20000	1365.11529 1363.11529	-207.91529 -200.91529	-13.89939 -17.99821
.43456789	1697.80060	1363.11227	-200.71527 -200.31529	-24.57643 -24.1679 <u>)</u>
9	1006-10000	1303.115.9	-262.31529 -295.01529	-27.02057
10 11	945.50Cuu 823.80000	1363.11529 1363.11529	-417.61529 -539.31529	-44.16872 -65.46677
le	886.20000	1000-00907	-180-40 9 67	-20-35767
13 14	963.66000 916.30000	1066.60967	-157-00967 -150-30967	-17.26140
15	616.50000	1066.60967	-25V.10967	-16.4039d -30.031y3
16 17	580 -00006 1331 -0000	1066-60967	-480-60907	-30-031y3 -83-89822
18	1731.0000 1605.70000	1783.06590 1783.0659c	-52.00590 -177.30290	-3.00765 -11.04502
19	1547.50000	1783.00590	~235.26590	-15-2000k
20 21	1292.60000 1017.20663	1783.06590 1783.06590	-490.46590 -765.86590	-37.94414 -75.29157
žŽ	6444 • 80 0 00	3635.92897	2808_87103	43.58353 28.86767
40 21 22 23 24	5111.50000 3336.90000	3635.92497 3635.92697	147>•57103 49•0∠897	
25	1962.70000	2203.01051	-240 -31 051	-8.95128 -11.11194
26 27 28 29	1702.70000	2263.61651	~42U.31631	-13-5/152
28	1534.80000 1236.20000	2203.01051 2203.01051	-008.21651 -966.81651	-43.53707 -78.20875
29	768.90000	1153.52004	-184.62064	-50.02297
3¢ 31	576.90000 527.2000	1153.52004 1153.52664	- 376.62664 020.32664	~99.9526 2 -118.80247
32 33	476-10000	11,3.52064	-677-4 (004	-142.2666 3
33 34	529.00000 479.40000	1153.52004	~063.92004	-117-61692
35	1756.60000	1155+52664 1490+0よう51	-014.12664 200.57449	-140.61882 15.27206
36	1786.50000	1490.02551	296-47449	10.29527
37 38	1645 -60000 1533 -70000	1490.02991 1490.02951	155.57449	9.45397 2.94766
≥8 39	1379.60000	1490.02551	-116.42551	-8.00417
40 41	1153.90000 1665.0000	1490.02551	-326.12351 30.97562	-29.12952
42	1752.70000	1620.52430 1820.52438	-73.82438	2.0d929 -4.21204
43	1605-2000-	1820.52438	-221.52438	-13.78796
44 45	1396.50000 965.50000	1626.52438 ~20.33800	~430.02436 991.83868	-30.79301 102.72796
46	828.80000	-¿6.35868	855.13868	102.72796 103.17793
47 48	742.46000 667.50000	-26.3300d -26.33600	7c b73d66 69383668	105.54778 105.94587
49	610.30000	-20.33868	u+4.638uB	104.45486
50	549.00000	6.33668	272.33868	104.77757
51 52 53	3317-20066 2226-96600	2962.93122	334.20676 -136.03122	10.67975 -33.05183
53	2746.70000	2962-93122	-216.73122	~7.87240
54 55	1186.50000 1172.80000	625.31640 625.31648	261.18352 547.48352	47.29739 40.88175
56	469* 9 0000	ひとつ。ろんじもひ	324-96552	36.21172
\$7 58	9150000	625.51646	289.86352	21.67434 27.58350
J.	863.50000	625.31648	230.15352	27.7837U

59	1744.20000	1573-471 3	176.72275	9.76803
60	1619-50000	1573.47725	46-02275	2.84179
61	1606-15000	15 73.47 725	34.64273	118د0ء ٤
62	1532.40000	1573.47725	-41.07725	-2.68:58

AVERAGE & DEVIATION IS 40.21602

DURBIN-WAISHN STATISTIC 15 1.11983

VUN NEUMANN S RATIO IS 1-13019

The program repeats this analysis procedure for each of the algebraic transformations listed above. They can then be compared with each other and the best one selected. In this case, the best transformation was the Log-Log form:

$$Log y = a + b Log x_n$$

Table 33 gives the mean and standard deviations of the transformed variables and also the cross-correlation matrix.

Table 34 gives the statistical parameters calculated as each variable is entered. At the bottom of the table are the coefficients for the final regression equation:

$$Log \left(\frac{\varepsilon_{rms}}{SPL}\right) = 3.0806 + 1.1045 Log (b)-1.2069 Log (t) + 0.5519 Log (R) (20)$$

Where ϵ_{rms} is in microinches/inch, b is in inches, t is in thousandths of inches, R is in inches and SPL is in lb/in².

This is the equation used to generate the rms strain nomograph in Section IV.5.

Table 35 gives the corresponding residuals, showing an average deviation of 23 percent.

There are many aspects of the regression analysis that can be observed from the data contained in Tables 30 through 35. The emphasis in this program is not on the formal statistical tests, but on relating the regression results to what is known about the data.

Referring to Table 34, it is seen that as each successive variable is entered, the multiple correlation coefficient and F-value increased, while the standard error decreased. The T-values also increased. If by adding one of these variables (b, t or R), or an extra variable, the statistics



TABLE 33

CROSS-CORRELATION MATRIX FOR VARIABLES USED IN FINAL REGRESSION EQUATION

TRANSFORMATION CODE = 2 LOGARITHMIC TYPE CURVE. GENERAL EQUATION FORM IS $\log y = a + b \log x$.

VARIABLE	MEAN	STANDARD DEVIATIÚN
1	0.80489	0.12180
2 3 4	1.94624 3.11562	0.25561

CORRELATION N ROW 1 b 1.00000	.t .t 0.23993	R -0.14990	(rms) 0.26480
ROW 4 0-23993	1.00000	0±15846	-0.56220
RDW 3 -0.14990	0.15646	1.06000	0 - 35886
ROW 4 U-26480	-0.56220	0.3>886	1.00000

TABLE 34

REGRESSION ANALYSIS RESULTS FOR FINAL REGRESSION EQUATION

VARIABLE ENTERED 2		
SUM OF SQUARES REDUCED IN THIS STEP	1.213	
CUMULATIVE SUM OF SQUARES RELUCED CUMULATIVE PROPORTION REDUCED	0.316 OF	3.838
FGR 1 VARIABLES ENTERED MULTIPLE CORRELATION COEFFICIENT C.562 (ADJUSTED FOR L.F.)		
STANDARD ERROR OF ESTIMATE		
VARIABLE REGRESSION STD. ERPOR OF NUMBER CUEFFICIENT REG. CGFF. 2 -0.86981534 0.16518 INTERCEPT 4.50532512	CUMPUTED T-VALUE	
INTERCEPT 4.50532512	3.200	
VARIABLE ENTERED 3		
	0.790 0.206	
CUMULATIVE SUM OF SQUARES REDUCED CUMULATIVE PROPORTION REDUCED	2.603 0.522 OF	3.838
FOR 2 VARIABLES ENTERED MULTIPLE CORRELATION COFFFICIENT U.722 (ACJUSTED FOR D.F.)		
F-VALUE FOR ANALYSIS OF VARIANCE 32.202 STANDARD ERRUR OF ESTIMATE 0.176 (ADJUSTED FOR D.F.) 0.178		
VARIABLE REGRESSION STD. ERRUK OF NUMBER CDEFFICIENT REG. CGEFr. 2 -0.98246594 0.14106 3 0.4900940 INTERCEPT 3.86040976	COMPUTED T-VALUE	
2 -0.98246594 0.14106 3 0.45054767 0.08940 INTERCEPT 3.86040976	-6.965 5.040	
VARIABLE ENTERED 1		
SUM OF SQUARES REDUCED IN THIS STEP	1-000 0-261	
CUMULATIVE SUM OF SQUARES REDUCED CUMULATIVE PROPORTION REDUCED	3.003 0.785 GF	3.838
FOR 3 VARIABLES ENTERED MULTIPLE CORRELATION COEFFICIENT 0.885		
F-VALUE FOR ANALYSIS UF VARIANCE 69.560	,)	
SIANDARD ERROR OF ESTIMATE	1	
VARIABLE REGRESSION STD. EKROK OF NUMBER CHEFFICIENT REG. CHEFF. 2 —1.20050298 0.09964	CUMPUTEG T-VALUE	
2 -1.20c70.298 0.09964 3 0.571/2333 0.062c1 1 1.1c45330c 0.13245	-12.112 6.901 6.339	
INTERCEPT 3.06061391		



TABLE 35
TABLE OF RESIDUALS FOR FINAL REGRESSION EQUATION

SELECTION.... 3

	TABLE OF	RESIDUALS		
0. 123456769012345678900123456789000000000000000000000000000000000000	Y VALUE 5506-50000 2826-80000 2826-80000 2194-50000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1094-20000 1731-00000 1731-00000 1731-00000 1731-00000 1747-80000 1747-80000 1748-80000 1748-80000 17536-70000 17536-70000 17536-70000 17536-70000 17536-70000 17536-70000 17536-70000 17536-70000 17536-70000 1754-70000 1756-50000	Y 195440 11975-39640 1975-39640 1975-39640 1975-396831 1975-396831 1975-396831 1210-995831 1210-995831 1210-995831 1210-995831 1210-995831 1210-995831 1210-995831 1210-995831 1210-995831 1210-995833 918-66396 918-66396 918-66396 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655703 1437-655819 1191-300204	Name	100.000
59 60 61 62	1744-20000 1619-50000 1606-10060 1532-40000	1365.18479 1365.18479 1365.18479 1365.18479	3/9-01521 254-31321 240-91521 167-21521	21.73003 15.70332 15.0001 10.91198
			DITCLEASE AU	15 1.24243
		AUN MEUI	MANN'S RATIO	15 1.26280

deteriorated, it would indicate that that variable was unwanted. The regression would then probably be repeated with that variable deleted.

The final F-value is used to check the statistical accuracy with which the regression equation represents the data. Referring to F-tables, for 62 observations and three independent variables, an F-value of greater than five corresponds to a better than 1 percent level of significance. T-values are similarly evaluated. Here a T-value of 2.4 corresponds to a 1 percent level of significance. Although F and T values are important, it was found that in this program many completely unsatisfactory regression results met high levels of statistical significance. Consequently, F and T values were not used to evaluate the effectiveness of a particular regression analysis, but only to ensure that high levels of significance were being met. What was found to be desirable was that the T values for each variable be comparable in magnitude. It, for example, one variable had ten times the T-value of another variable, it would follow that the numerical contribution of the variable having the lower T value to the estimated value of the dependent variable would be so small as to render its presence useless.

The tables of residuals provide a good comparison between different regression equations. Table 35 shows the Log:Eng equation to be a much more accurate predictor of the test data than the linear equation, whose residuals are shown in Table 32.

Elimination of Outliers

Tables of residuals are often used to reject data points as outliers. Data points having the largest percent deviations are rejected and the regression analysis is repeated. This invariably results in a more "accurate" equation. However, this is a more effective procedure when dealing with data about which little or nothing is known quantitatively, such as public opinion type surveys. In this program, however, a great deal is known about the data. In such cases, apparent regression outliers must be evaluated against the actual test data. An illustration of the



importance of this is given in Figure 60. The four points a, b, c and d represent response strain values for four different skin thicknesses. The line drawn (1) --- (1) represents a computed regression relationship showing strain increasing with skin thickness. Based on a table of residuals, data point "d" appeared to be an outlier. Elimination of point "d" resulted in a new regression line (2) ---- (2), which had greater statistical accuracy than the first line. Since it is known that strain decreases with increasing thickness, it can be seen that the regression analysis resulted in an illogical relationship. In addition, by removing an outlier on the basis of statistical accuracy, the incorrect trend of the regression was worsened. By plotting the data prior to regression, and knowing that strains decrease with increasing skin thickness, it is obvious that data point "a' is the main outlier and not point "d". When point a was removed, the new regression line was (3) --- (3), which shows a more reasonable relationship. This example illustrates the importance of checking data for technical inconsistencies prior to regression analysis, preferably by graphical means; and also demonstrates the danger in allowing statistical decisions to replace technical ones.

Figures 61, 62 and 63 show graphical representations of measured rms strains versus stringer spacing, skin thickness and radius of curvature for each test sound pressure level. The only imposition made on the data prior to regression was that response strain must increase with increasing sound pressure level, stringer spacing and radius of curvature; and must decrease with increasing skin thickness. No prior limitation was placed on the rate of change. This is a sensible and practical approach when dealing with sonic fatigue test data, where isolated illogical data points are not unusual. Referring to Figure 61, there were no inconsistencies in the data presented. On Figure 62, however, both panels a (6 ply) and n (4 ply) had lower strains than panel b (8 ply). In order to determine whether panel b response was too high or that for panels a and n were too low, Figures 61 and 63 were referred to. From these graphs, it does not appear as if the response for panel b was too high. In fact, Figure 63

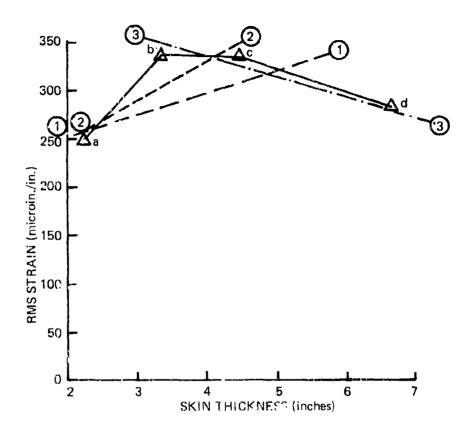


Figure 60. Graphic Illustration of Regression Error

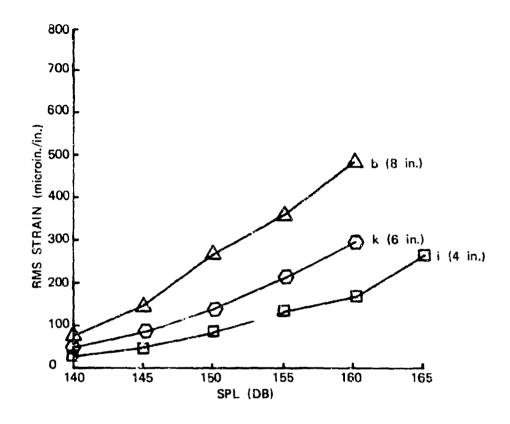


Figure 61. Response Comparisons for Different Stringer Spacings

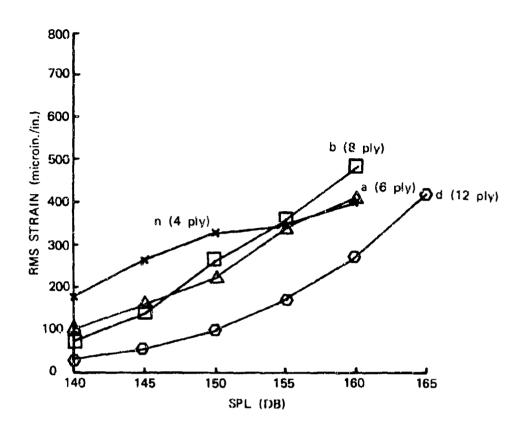


Figure 62. Response Comparisons for Different Skin Thicknesses

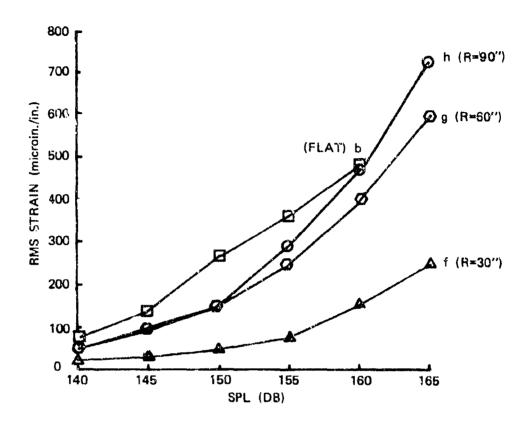


Figure 63. Response Comparisons for Different Radii of Curvature

indicates that at 160 dB, the response for panel b was too low. Based on this observation, referring back to Figure 62, the following data points were rejected: panel a at 150, 155 and 160 dB; and panel n at 155 and 160 dB. Referring now to Figure 63; panel b at 160 dB was rejected, as was panel h at 145 and 150. Sine other data points were similarly rejected, based on comparisons that did not lend themselves to graphical representation. They were:

panel g @ 160 dB
panel i @ 165 dB
panel j @ 140 dB through 165 dB
panel p @ 155 dB
panel r @ 140 dB
panel s @ 140 dB

There was a tendency for data at 140 dB to be generally inconsistent due to the low response levels. With the possible exception of panel n, the data points rejected did not interfere with observations regarding the nonlinearity of the panel responses.

In developing a design method for both flat and curved panels, using regression analysis, it was necessary to determine a numerical value for the radius of curvature of a flat panel. Since regression analysis deals entirely with numerical values, using a very high value to represent an infinite radius of curvature must be avoided. Orginally, a value of R = 10,000 inches was used, resulting in a very small regression coefficient for this variable. Since the response differences between the flat and the R = 90-inch curved panels was much less than between the R = 30-inch and the R = 60-inch panels, it seemed likely that a much lower number than 10,000 inches would be appropriate. Various numbers were tried, and also a graphical review of the data was performed. It was determined that R = 150 inches was a satisfactory number to represent the flat panel radius.



NOTE: The following important observation was made during these regression analyses. The signs (+ or -) of the regression coefficients of the independent variables were determined within the computer program, based on the sign of the cross-correlation coefficient between the independent variables and the dependent variable. When using a Log function to represent an independent variable having values of less than unity, the program fails to take account of the logarithm of the value changing sign. To overcome this, the values of independent variables were adjusted to be always greater than unity. In this program, the skin thicknesses were entered x 10³.

Durbin-Watson Statistic

It will be noticed that the tables of residuals quote the Durbin-Watson statistic. In regression analysis it is assumed that the residual errors are an independent random variable. If the error terms are not independent, but show serial correlation, this indicates that the best possible curve fit may not have been obtained. It also means that the F and T tests may not accurately reflect the true confidence levels of the regression results. The Durbin-Watson statistic is used to check for serial correlation in the error terms. In the regression analyses performed here, the Durbin-Watson statistic indicated that there was some serial correlation in the error terms. However, this is not critical for the regression analysis performed in this section. As mentioned earlier, the emphasis here was more on uncovering patterns in the data than on formal tests. The best possible curve fit was sacrificed partially in order to ensure a technically acceptable result. Also, the F and T values obtained here were considerably in excess of those values required to assure good statistical accuracy, and therefore, the validity of these regression results is not affected by small changes in their values.

Many regression analyses were performed prior to selecting one for the final design method. Some resulted in unacceptable equations, others yielded results that may be used as alternatives to the one chosen here.

A major effort was made to use nondimensional independent variables, of the form used in AGARD nomographs. Regression equations do not usually balance dimensionally, and therefore, care must be taken if using units other than those used in developing the equations. Nondimensional parameters overcome this objection. However, by imposing certain fixed relationships between variables, the accuracy of the equation usually suffers.

Other regression analyses performed included using as an independent variable rms strains calculated from Miles' equation, with the frequency component estimated from the AGARD nomograph and the static strain component computed from the finite-element models. These estimated strain values are given in Table 29. The following equation was obtained:

$$log c_{rms} = 0.33 + 0.47 log c_{rms} calculated$$
 (21)

The calculated and measured rms strains had a cross-correlation coefficient of 0.73 and satisfied the F and T tests. However, the average error was 50 percent with maximum errors exceeding 2:1. Table 36 shows the residuals.

Since the above regression yielded unacceptable results, the next step was to regress directly on the frequency and static strain components used in the preceding regression. The calculated frequency had a cross-correlation coefficient of -0.64 with the measured strains. The computed static strains had a corresponding correlation coefficient of 0.83. The average error was 32 percent. Table 37 shows the residuals for the following regression equation:

$$\varepsilon_{\rm rms} = \frac{(1.825.3) \ 1.193^{\varepsilon_0}}{1.001^{\rm f}}$$
(22)

TABLE 36

TABLE OF RESIDUALS FOR REGRESSION OF MILES' EQUATION

TABL	- n	L 10	£ 4 7	na.	4 6	•
IADI	r H	- x			-	`

N12345678961234567896123456789678967896789678967896789678967896789	Y VALUE 101-70000 77-30000 147-10000 265-80000 357-70000 357-70000 358-90000 101-00000 174-20000 425-10000 48-50000 77-60000 153-60000 48-7-40000 250-70000 48-30000 48-30000 133-10000 141-20000 153-300000 153-300000000000000000000000000000000000	Y 100-100-100-100-100-100-100-100-100-100	AL TRUMPTR MARKET MARKE	144
59 60 61 62	90 - 70000 149 - 00600 261 - 80006 444 - 40000	50 -5 4669 60-13364 86-51272 113-39993 AVERAGE	40.12331 82.86636 175.28728 331.00007 4 DEVIATION	44 - 23 7 38 55 - 615 01 36 - 954 65 74 - 45246
		OURB IN-WAT SO		15 (.89991
		AGM WEAR	ANN'S RATIO	15 0.91+66

TABLE 37

TABLE OF RESIDUALS FOR REGRESSION USING CALCULATED FREQUENCIES AND STATIC STRAINS

TABLE OF RESIDUALS

NO 123456789001234567890100000000000000000000000000000000000	Y VA LUE 3506-99300 2665-50060 2825-80000 2194-50000 1195-20000 1094-20000 1097-50000 525-30000 823-388000 768-90000 576-90000 576-90000 1758-60000 1758-60000 1758-60000 1758-60000 1758-60000 1758-60000 1758-60000 1758-70000 1758-70000 1758-70000 1758-70000 1758-70000 1758-80000 1758-700000 1758-700000 1758-700000 1758-700000 1758-700000 1758-700000 1758-700000	Y 900-164599 22165-164599 22165-164599 22165-164599 22165-1645772 2165-1857772 2165-1857772 2165-1857772 21586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-857772 1586-85772 1586-85772 1586-85772 1588-85778 1588-8773 1688-8773 16978-17839 1697	RLS.170391 598.35412 598.35412 598.355772 598.355772 734.8557772 657772 657772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 641.35772 642.9269 642.9277772 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 642.929 643.399 644.399 643.399	TION 1.59
59 60 61 62	1744 -20000 1619 -50000 1606 -10000 1532 -40000	807-20336 607-20336 607-20336 807-20336	936 -99664 612 -29664 798 -59664 725 -19664	33:13973 47:32424
		aver ag Lairt in-Wat	E & DEVIATION SUM STATISTIC	15 31.81944 15 1.31602

WUN NEUMANN'S RATIO IS

1.33760

This equation also results in major differences from many of the test data points, and is not recommended for design use. It is, however, significantly better than using Miles' equation. It may be used as a design guide for irregularly shaped structures for which there are no simple dimensions such as b, t and R; but for which computed static strains and frequencies are available.

A regression analysis was performed, combining ϵ and f with b, t and R as independent variables. However, the results were no better than using only b, t and R.

Effects of Nonlinear Structural Response The regression analyses described thus far have all used $\binom{\epsilon_{rms}}{SP}$ dependent variable. This imposes the assumption of linear response. However, although some panels show linear response, there was a general tendency for strains to not quite increase linearly with sound pressure level. This does not necessarily mean that the structural reponse is truly nonlinear. Several test panels had back-to-back strain gauges installed, and none detected any in-plane (membrane) strains. There are, however, appears of somic fatigue testing that can give the appearance of nonlinearity, such as "clipping" at high sound pressure levels, overall gained and fixture motion which may not be fully responsive to changing sound pressure levels. For these reasons, and because the degree of runlinearity was not excessive, the design method proposed in Section IV.5 is based on linear response. However, in order to provide quantitative information on the degree of nonlinearity, and thereby make an alternative design equation for those who may wish to use it, a regression analysis was performed with overall sound pressure level as an independent variable. It should be remembered that some of the less stiff panels were not tested at the high sound prescure levels that the stiffer panels were subjected to, and as a result, there will be a slight bias in the regression equation. The blas, however, will be small. The following equation was obtained:

Log ε = 0.3528 + 1.0458 Log b-1.1241 Log t (23) + 0.4994 Log R + 0.873 Log (SPL x 10³)

(SPL was entered times 10³ in order to keep its value above unity and prevent the logarithm from changing sign)

This equation had an average accuracy of 22 percent, slightly better than the equation selected for the design nomograph. The residuals are shown in Table 38. Table 39 shows the corresponding correlation matrix and statistics for the above equation. A comparison between Tables 35 and 38 show the nonlinear regression to have significantly lower residuals. Comparing the cross-correlation matrices for the linear and nonlinear regressions (Tables 33 and 39) shows much lower correlation between $\epsilon_{
m rms}$ and the panel dimensions (b, t and R) than between $\left(\frac{\varepsilon_{rms}}{SPL}\right)$ panel dimensions. This would indicate that there was significant correlation between SPL and the panel dimensions. The correlation matrix in Table 39 hows significant correlation between t, R and SPL. In fact, t and R show higher correlation with SPL than with ϵ_{rms} . This lack of independence between the "independent" variables is called multicollinearity, and is a condition of deficient data. The presence of multicollinearity does not necessarily invalidate the regression, but it is a signal for caution. Performing comparative calculations using the linear and nonlinear equations indicated that the degree of multicollinearity was not excessive. In order to illustrate the degree of nonlinearity, the change in strain due to 6 dB increase in sound pressure level was found to be times 1.83. The linear equation would produce a ratio of times 2.

It should be pointed out that the nonlinear equation is the most accurate representation of the test data in this program, and may be quite acceptable for design use. However, since the degree of nonlinearity was not high, and in the interests of some conservatism, the linear equation was used to develop the design nomograph in Section IV.5.

TABLE 38

TABLE OF RESIDUALS FOR NONLINEAR REGRESSION

Yanif	OF RESIDUALS		
CASE No. 1077-30000 1777-30000 1777-30000 1777-30000 1777-30000 1777-30000 1777-30000 1777-30000 1777-30000 1777-30000 1777-3000000 1777-3000000 1777-30000000000000000000000000000000000	T	### ##################################	N T84542911868237392090545293749320201308103337679419668237396425457811552951886081033376945786167737768682376696553926 T847199118927768214356425405169178324115570373845789718308394676853926 T6471997777668441433222066967564061474660564473118377670863946668353926 T64719977766848767226683544061474666831487671870914477668314876696668314876976683148769766831487697668314876976837301679611477668314668314676966837666837666837666837666837666837666837666837666837666837668686686686686686686686686686686686686
59 99.7000 60 149.0000 61 761.8000 67 444.4000	0 12x./45h7 6 212.04409	12.47626 20.27433 49.70591 93.67014	13.75565 13.60021 17.96021 21.67789
	AVEDAG	BE & DEVIATION	
	DUILD IN-WAT	SON STATESTE	TC 0.86877

VOI NEUMANNIS PATTO IS

0.88301

TABLE 39

REGRESSION ANALYSIS RESULTS FOR NONLINEAR REGRESSION

CORRELATION MA	X T H T &			
b	t	R	SPL.	€ rms
1.0000	n.2399a	-0.14990	-6.03749	0.14109
59975°U	1.00000	0.15846	0.18721	-0.18026
-0.14000	0.15846	1.00000	-n.20nja	n.n2567
170¥ 4 -0.03749	0.18721	-0,20010	1.00000	n.~9074
ዋለ₩ ጜ ሳ•ነፋ¦ስዓ	70.1H02K	0.02567	0.79075	1,0000
VARIABLE ENTERET.	٦			
SUM OF SOUAKES HE PROPORTION REDUCE	NUCEO IN THIS O IN THIS ST	S STEP	0_870 0_108	
CHMOLATIVE SUM OF CHMULATIVE PROPUR	TION HEDUCHI TION HEDUCHI	(JUEN	7,373 0.914	OF 8.065
FOR A VARIABLES MULTIPLE CORREL	ATION CUEFFI	CIENT	n.956 0.954	
STANDARD ERROR	FOR D.F.) LYSIS OF VAR OF FSTIMATE.	1 WIACE *** I.	1.895 0.110	
(ADJUCTE)	FOR (1.F.)		0.113	
NUMBER CO	GPFSSTAN FFFILTENT .8730418H	SID. ENROR REG. COEFF 0.0370	- T-VAL	HF.
7 -1	1240K212 0457KG83	0.0946 0.1228	5 -11. 5 8.	97A 513
ች በሚተከር። 1	40935087	0.0589	7 P.	447

Regression analyses were also performed on the test frequencies and the static strains computed from the finite-element models; against the panel dimensions b, t and R. It was originally hoped that simplified regression equations could be developed for frequencies and static strains, which in turn could be used as inputs to a regression equation for rms strain. However, the regression equation for rms strain which utilized frequencies and static strains as inputs was not particularly accurate. In addition, it was not possible to obtain a satisfactory regression equation for static strains on the curved panels. For the flat panels only, however, a regression equation between the computed static strains and the panel dimensions produced an equation with an average accuracy of 5 percent:

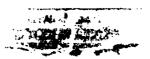
$$t_0 = \frac{(921)(1.4105^{b})}{(1018)^{t}}$$
 (24)

Regression analysis on the test frequencies against the panel dimensions gave satisfactory results, but since the existing AGARD nomograph also gave satisfactory results, there was no point in using a regression equation in the design method.

4. DESIGN EQUATIONS

Before proceeding with the final design method, it seems useful to fully describe the regression equation used, and to present those alternatives that are /iable.

The basic design method utilizes overall sound pressure levels rather than spectrum levels as applied loads. Consequently, it is not necessary to determine the natural frequency in order to determine rms strain. Response frequency estimates, however, are required in order to estimate fatigue lives.



- a. Calculation of RMS Strains Acceptable equations developed in Section IV.3 follow:
 - (i) Equation for rms strain, used to develop the design nomograph in Section IV.5 is:

$$Log \frac{\varepsilon_{rms}}{SPL} = 3.080614 + 1.104533 Log b$$

$$-1.206903 Log (103.t) + 0.551923 Log R$$
(20)

where $\varepsilon_{\mbox{\scriptsize rms}}$ is in microinches/inch

SPL is in 1b/in²

b is in inches

t is in inches

R is in inches

and where R = 150 inches for a flat panel, i.e., for $150 < R < \infty$, use 150.

- NOTE: (1) Because the equation is in Log:Log form, six significant figures are required in order to maintain reasonable accuracy.
 - (2) This equation assumes linear response, i.e.,6 dB represents a doubling of strain.
 - (3) Strain levels were quoted rather than stress levels in order to allow elastic modulus values for alternative skin laminates to be used in determining stress levels.
 - (4) All logarithms are to the base 10.

This equation may be written in the form:

$$\epsilon_{\text{rms}} = \frac{(8.3234 \times 10^{-10}) \ 10^{(\text{SPL/20})} \ b^{1.1045} \ R^{0.5519}}{t^{1.2069}}$$
 (25)

where SPL is in decibels (dB).

(ii) Nonlinear Response Equation (from equation 23):

$$\varepsilon_{\text{rms}} = \frac{(1.394 \times 10^{-8}) \, b^{1.0458} \, i.0.4994 \, 10^{0.04365.\text{SPL}}}{t^{1.1241}}$$
(26)

where the variables are defined as in (i) above.

NOTE: This equation is slightly more accurate than (i), but may be slightly unconservative at very high sound pressure levels

Effects of Aspect Ratio

In this program, the long side of the individual bays was kept constant at =12 inches. The short side varied from 4-inches to 8-inches, thus the aspect ratio varied from 1.5 to 3. In order to include the effects of varying aspect ratio, the stress nomograph in Reference 5 was used. RMS stresses for various aspect ratios were calculated, and the ratio effects applied to the strains calculated in this program. Within the levels of accuracy of the AGARD stress nomograph, and also considering the accuracies of the regression equations; there were no significant changes in strain response at aspect ratios above 1.5. Based on the combined effects of aspect ratio on static strains and frequencies, the dynamic strains at a/b = 1.5 and $a/b = \omega$ are within approximately 5 percent of each other. Consequently, the design nomograph was constructed assuming a common response for all aspect ratios above 1.5. Aspect ratio lines for

a/b = 1.2 and 1.0 were then superimposed based on stress ratios determined from the AGARD rms stress nomograph.

Effects of J Stiffeners

The static analysis showed that J stiffeners resulted in significantly lower edge strains, compared to using Z stiffeners. The ratio of J to Z being 0.71. The measured data gave a corresponding ratio of 0.7 to 0.8 for configuration b. Configuration c did not show any strain reduction due to the J stiffeners, but it did show a major increase in fatigue life. Based on these observations, it is recommended that the calculated strains in this design method be factored by 0.8 when using J stiffeners. This is believed to be a slightly conservative factor.

b. Calculation of Natural Frequencies - Reference 5 was used to calculate the fundamental fully-fixed panel frequencies. The equations and nomograph are included in Section IV.5.

This method was derived for typical metals, and assumes typical values for elastic modulus (E) and material density (ρ). It is necessary to modify these values when using composite materials. Graphite/expoxy laminates have a density of 0.055 lb/in³. The elastic modulus varies with ply orientation. In this program, elastic modulus values are given in Tables 2 through 6.

Reference 8 is recommended for use if stiffener properties are to be used, rather than assuming fully-fixed edges. For flat panels only, Reference 5 contains a simplified method based on Reference 8. However, both the flat and curved panel equations in Reference 8 lend themselves to programming on modern desk top computers.

5. DESIGN METHOD

This section contains a semi-empirical method for estimating rms strains and natural frequencies for curved and flat graphite-epoxy skin-stringer panels, in order to predict their sonic fatigue lives. A random rms strain versus cycles to failure curve is presented for bonded skin-stiffener joints. A worked example is also presented.

The design equation and corresponding nomograph for rms strain was based on Z stiffeners. However, they can be readily factored to allow for the use of J stiffeners.

a. Estimation of RMS Strain - The RMS strain nomograph is shown in Figure 64. It is based on equation 25 from Paragraph IV.4.a:

$$\varepsilon_{\text{rms}} = \frac{(8.3234 \times 10^{-10}) \ 10^{(\text{SPL/20})} \ b^{1.1045} \ R^{0.5519}}{t^{1.2069}}$$
(25)

where ϵ = Maximum rms strain at panel edge due to random acoustic loading (10 in/in)

SPL = Overall sound pressure level (dB)

a = Panel length, between longerons (inches)

b = Panel width, between stringers (inches)

t = Skin laminate thickness (inches) (also given on nomograph
as number of plies)

R = Radius of curvature in "b" direction (inches). R = 150 in. is the maximum value to be used in the response equation, and is valid for flat panels and all R > 150 in.

Equation is valid for $a/b \ge 1.5$.

For a/b = 1.2, factor equation by x 0.849.

For a/b = 1.0, factor equation by x 0.744.

177

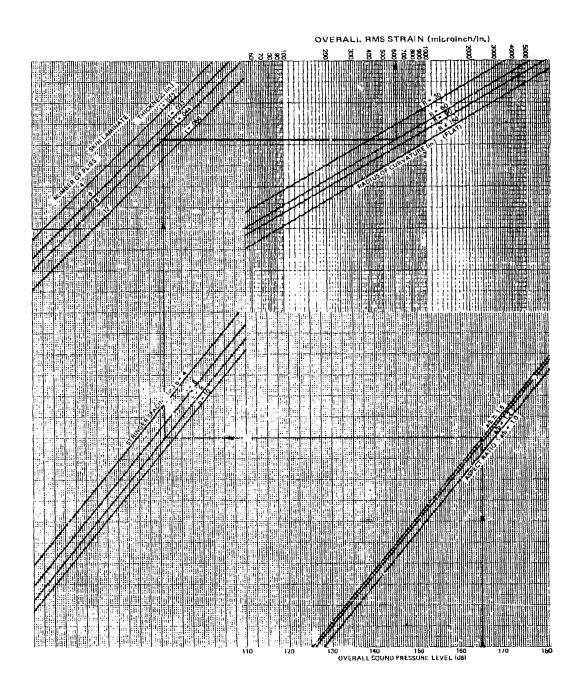


Figure 64. RMS Strain Nomograph

b. Estimation of Fully-Fixed Natural Frequency

From Reference 5,

$$f = V.K. \frac{t}{b^2}$$
 (27)

where f = frequency of fundamental fully-fixed natural frequency (Hz).

$$V = (E_y/\rho)^{1/2}/200,000$$
 (28)

where

E is the elastic modulus in the "y" direction, i.e., "y" direction (1b/in²). Obtained from Tables 2 through 6 for laminates used in this program. For other laminates, Reference 12 may be used.

 ρ = density of skin laminate. If expressed in units of lb/in , it must be divided by 386.4. For graphite-epoxy laminates,

$$\rho = \left(\frac{0.055}{386.4}\right)$$

K is obtained from Figure 65 for given b, t and R.

b,t and R are defined as in Paragraph IV.5.a, except that true values are 10 be used for all R, including ∞ for flat panels.

c. Estimation of Fatigue Life - Estimated sonic fatigue life is obtained by reading number of cycles to failure (N) from Figure 66 for rms strain ($\epsilon_{\rm rms}$) calculated in Paragraph IV.5.a. The number of cycles to failure is converted to life in hours by the relationship $\left(\frac{N}{3,600f}\right)$.

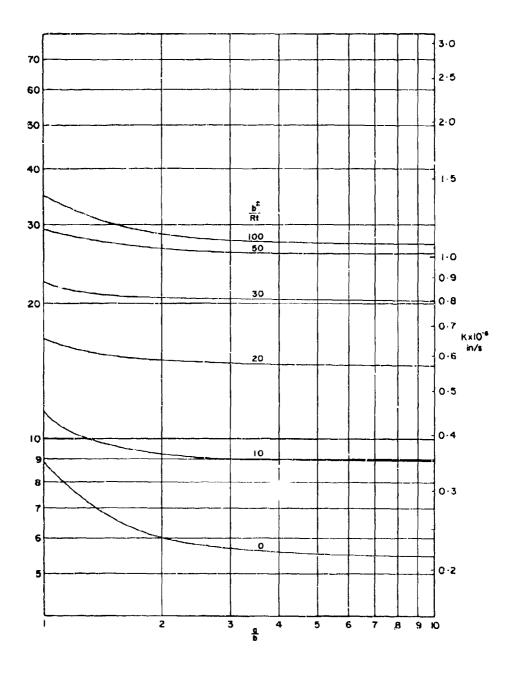


Figure 65. Natural Frequency Nomograph for Panel with Fixed Edges (Reference 5)

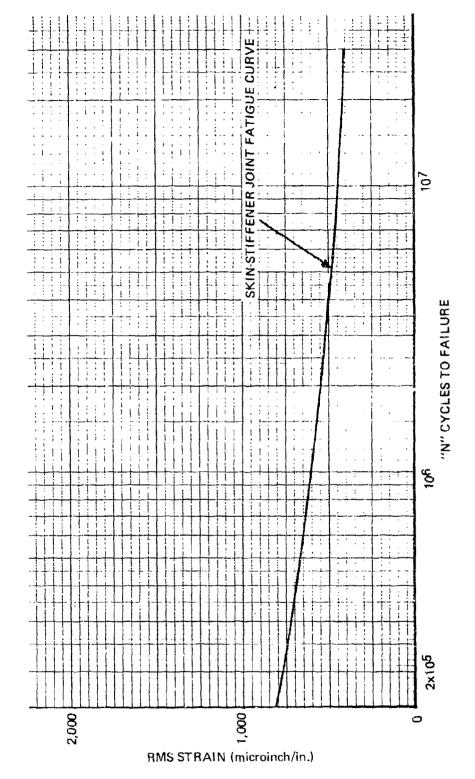


Figure 66. Random Fatigue Curve for Bonded Skin-Stiffener Joint — RMS Strain vs. Cycles to Failure

- d. Calculation Procedure
 - (1) Estimate rms strain (ϵ_{rms}) from Figure 64 or from equation 25, for given SPL (dB), b, t and R. (For flat panels and other R > 150, put R = 150-in.).

If J stiffeners are used, multiply ε_{rms} by 0.8.

- (2) Calculate V from equation 28.
- (3) Estimate K from Figure 65 for given b, t and R. Use $R = \infty$ for flat panels.
- (4) Calculate frequency (f) from equation 27.
- (5) Estimate number of cycles to failure (N) from Figure 66 for estimated $\varepsilon_{\rm rms}$ from (1).
- (6) Convert cycles to failure to fatigue life in hours, using calculated frequency from (4).
- e. Worked Example A curved panel is made up from an 8 ply skin laminate, having a ply orientation of $(0, \pm 45, 90)_s$, which corresponds to t = .044 in. and $E_y = 6.7 \times 10^6$ lb/in.². The panel has Z section stiffeners, with bay dimensions of a = 12 in. and b = 8 in. The radius of curvature is 60 in. The overall sound pressure level is 165 dB.
 - (i) From Figure 64, the corresponding rms strain $\epsilon_{\rm rms}$ = 615 microinches/inch.

(ii)
$$V = (E_y/o)^{1/2}/200,000, \rho = \frac{.055}{386.4} = .000142$$
$$= \left(\frac{6.7 \times 10^6}{.000142}\right)^{1/2}/200,000 = 1.0861$$



(iii) In order to determine K from Figure 65, first calculate:

$$a/b = \frac{12}{8} = 1.5$$

$$\frac{b^2}{Rt} = \frac{8^2}{(60)(.044)} = 24$$

From Figure 65, $K = 0.68 \times 10^6$.

(iv) From equation 27:

$$f = V.K. \frac{t}{b^2}$$

 $f = (1.0861)(0.68 \times 10^6)(\frac{.044}{s^2})$

= 508 Hz

(v) From Figure 66,

Cycles to failure $N = 8 \times 10^5$

for
$$\epsilon_{\rm rms}$$
 = 615.

(vi) Fatigue life =
$$\frac{N}{3.500 \text{ f}}$$
 = 0.44 hours

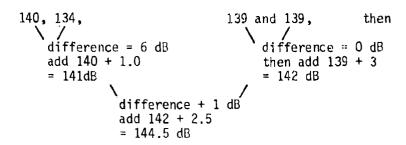
- NOTE: The estimated rms strain of 615 $\,\mu$ in./in. corresponds to a measured value of 595 $\,\mu$ in./in. The estimated frequency of 508 Hz corresponds to a measured value of 350 Hz.
- f. Fan Noise as Acoustic Load The design method presented here utilizes the overall sound pressure level as the design load. While this is adequate for the broad-band spectra that typify jet exhaust noise, it does not automatically lend itself to designing for the inlet and fan exit

acoustic spectra that occur due to fan noise on high bypass ratio engines. These spectra often have overall sound pressure levels that are dominated by very high acoustic spectrum levels occurring at the blade passage frequency and some of its harmonics. Since the blade passage frequency (typically 2-4 KHz) is usually well above the frequency range of interest for structural reponse (typically 50-1,000 Hz), including it in the overall sound pressure level to be used in this design method may result in overly conservative designs. In order to deal with this type of acoustic load it is necessary to eliminate these high frequency peaks, and develop an estimate for the overall sound pressure level from 50 Hz-1,000 Hz. This can be accomplished in one of the following ways. (1) If the actual measured acoustic data are available (e.g., on magnetic tape), reanalyze the data to measure the overall sound pressure level with a 1,000 Hz cutoff filter applied. (2) If only the acoustic spectrum plot is available, then sum together in sequence all the significant peaks between 50 Hz and 1,000 Hz in the following way:

If the difference (in dB) between two peaks is (any bandwidth):

	0	1	2	3	4	5	6	7	8	9	10	>10
then add to the larger peak (dB)	3	2.5	2.1	1.8	1.5	1.2	1.0	0.8	0.6	0.5	0.4	0

Example: If there were four peaks with the following levels (dB):



This 144.5 dB is the overall sound pressure level to be used as the design load.

6. DESIGN METHOD COMPARISONS

Graphite-epoxy skin-stringer structures, of the type evaluated in this program, are primarily in competition with similarly configured aluminum structures for application on both military and civil aircraft. Cost/weight tradeoffs between graphite and aluminum structures having comparable sonic fatique resistance are, therefore, of interest to potential users of the design method in Section IV.5. In order to provide an estimate of the sonic fatigue resistance of graphite relative to aluminum, comparisons were made between the method in Section IV.5 and those in References 2 and 5. One difficulty in making these direct comparisons is that References 2 and 5 utilize acoustic spectrum levels, whereas Section IV.5 here utilizes overall sound pressure levels. In order to overcome this, a typical broad band sonic fatigue design load spectrum was used which had an overall sound pressure level of 157 dB and a corresponding acoustic spectrum level of 132 dB/Hz in the frequency range of interest. This 25 dB difference between overall and spectrum levels is compatible with the acoustic load in this program.

The following example problem was used for comparison:

Required life = 10 cycles (using the -50% confidence level from Reference 2).

b = 8 a/b = 2 c = .02

Calculate required skin thicknesses.



The following results were obtained:

Reference 2 - Riveted Aluminum Skin-Stringer: t = .05-in. Reference 5 - Riveted Aluminum Skin-Stringer: t = .076-in. Section IV.5 - Bonded Graphite Skin-Stringer: t = .041-in. Paragraph IV.4.a. - Using the nonlinear

response equation: t = .037-in.

Comparisons of sonic fatigue resistance using References 2 and 5 yield similar results for some configurations and very different results for others. Where differences do occur, Reference 5 is the more conservative.

Since the density of graphite is approximately half that of aluminum, the potential weight saving of graphite over aluminum for equivalent sonic fatigue resistance is significantly large. Comparing values generated in this program with those in Reference 2, the weight of graphite is slightly less than half that of the equivalent aluminum structure.

SECTION V CONCLUSIONS

A satisfactory sonic fatigue design method was developed for curved and flat graphite-epoxy skin-stringer panels. The design method is presented as a self-contained section suitable for application to aircraft structural design. Design trade-offs with aluminum structures indicated that graphite offers a 2:1 weight saving over aluminum, for comparable sonic fatigue resistance.

Analytical results indicated that ply stacking order may have an effect on sonic fatigue life. However, the effects were not quantified sufficiently to facilitate the inclusion of this variable in the design method. This is an area requiring further work.

The finite-element analyses gave good static strain distributions for the test panel configurations. These computed strains displayed high statistical correlation with measured dynamic strains. Element grid size was found to be critically important at panel edges. Representing panel stiffeners as plates in three-dimensional models resulted in more accurate computed strains than when representing stiffeners as beams in two-dimensional models.

The finite-element analyses did not result in satisfactory frequency estimates for all the t.st panel configurations. On the stiffer panels, mode shapes were dominated by motion of the substructure, resulting in low frequency estimates. Test data contradicted this response behavior. The

best analytical comparisons with measured frequencies were obtained using simple frequency calculations assuming fully-fixed edges.

Adhesive bonding problems encountered during the early stages of test specimen fabrication demonstrated the importance of assuring good bond and laminate quality prior to fabricating expensive sonic fatigue test panels. Shaker testing of small coupons was found to be an excellent method of evaluating specimen quality. The modes of failure during shaker testing showed good correlation with progressive-wave tube failures.

The sonic fatigue data obtained during the progressive-wave tube tests showed good correlation with variations in panel configuration parameters. The data also displayed some inconsistencies, characteristic of sonic fatigue testing. Sonic fatigue failures were generally observed to occur over long periods of time, often over several million cycles. The first signs of fatigue damage were fractured skin laminate fibers in the stiffener-skin joint areas. Isolated fiber failures would continue to occur until the extent of the skin damage resulted in separation from the stiffeners. This type of slow progressive failure presents problems in defining time to failure. The mode of sonic fatigue failure was indicative of good quality structural panels. The fatigue lives of bonded and riveted joints were compared. Riveted joints displayed slower rates of progressive damage.

Slight variations in ply orientation did not appear to affect panel response or fatigue life. However, it is expected that major variations in ply orientation would have significant effects.

J stiffeners were observed to result in significantly longer fatigue lives than did Z stiffeners.

Panel responses showed some degree of nonlinearity, however, back-to-back strain measurement did not reveal any membrane strains.

Multiple stepwise regression analysis, relating rms strains to panel configuration parameters, provided the basis for the recommended design method. Miles' equation does not show good correlation with the test data. Linear and nonlinear equations were developed to predict panel response. Emphasis was placed on the importance of critically reviewing the test data prior to regression analysis. The potential hazards of using regression analysis were discussed in some detail. A design nomograph to predict rms strains was constructed and presented as part of a sonic fatigue design method. A worked example was also presented.

REFERENCES

- 1. Miles, J. W., "On Structural Fatigue Under Random Loading," Journal of Aeronautical Sciences, Vol. 21, November 1954.
- 2. Ballentine, J. R. et al. "Refinement of Sonic Fatigue Structural Design Criteria," AFFDL-TR-67-156, January 1968.
- 3. Holehouse, I., "Sonic Fatigue of Diffusion Bended Titanium Sandwich Structures," Paper No. 15, AGARD-CP-113, Advisory Group for Aerospace Research and Development, North Atlantic Treaty Organization, 1972.
- 4. Schneider, C. W., "Acoustic Fatigue of Aircraft Structures at Elevated Temperatures." AFFDL-TR-73-155.
- 5. Thompson, A.G.R. and Lambert, R. F., "Acoustic Fatigue Design Data," AGARD-AG-162, Advisory Group for Aerospace Research and Development, North Atlantic Treaty Organization, November 1972.
- 6. Rudder, F. F. and Plumblee, H. E., "Sonic Fatigue Design Guide for Military Aircraft," AFFDL-TR-74-112, May 1975.
- 7. Jacobson, J. J., "Acoustic Fatigue Design Information for Fiber Reinforced Structures," AFFDL-TR-68-107, October 1968.
- 8. Lin, Y. K., "Free Vibrations of Continuous Skin-Stringer Panels," Journal of Applied Mechanics, December 1960.
- 9. Powell, A., "On the Fatigue Failure of Structures Due to Vibrations Excited by Random Pressure Fields," Journal of the Acoustical Society of America, Vol. 30, No. 12, December 1958.

- 10. Roark, J. R., "Formulas for Stress and Strain," McGraw Hill.
- 11. Miner, M. A., "Cumulative Damage in Fatigue," Journal of Applied Mechanics. Vol. 12, 1954.
- 12. Lackman, L. M., et al. "Advanced Composites Data for Aircraft Structural Design, Volume IV," AFML-TR-70-58, September 1972.
- 13. Timoshenko, S. P., "Theory of Plates and Shells," McGraw Hill.
- 14. Den Hartog, J. P., "Mechanical Vibrations," McGraw Hill.
- 15. Levy, M., "Compt. rend., Vol. 129," Paris 1900.

APPENDIX A

FINITE ELEMENT MODELS AND RESULTS

Figures A-1 through A-32 are computer generated plots of the following:

- Finite element models used in the static and dynamic analyses
- ullet Static deflections and stresses for panels b, d and f
- Mode shapes for panels b and f

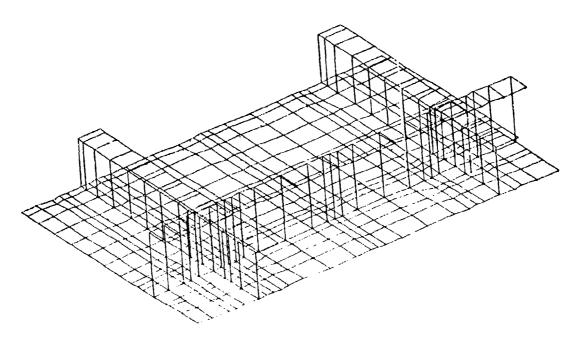


Figure A-1. Finite Element Model of 3 x 3 Center Panel - Flat

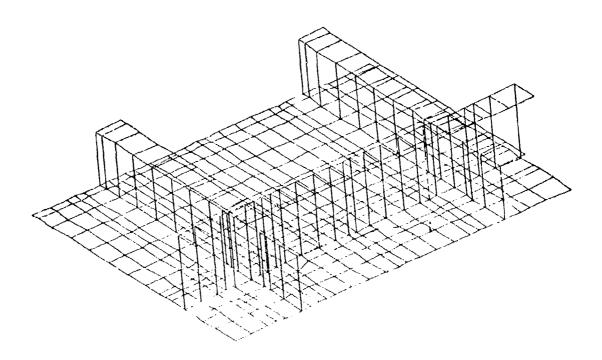


Figure A-2. Finite Element Model of 4 x 3 Center Panel - Flat

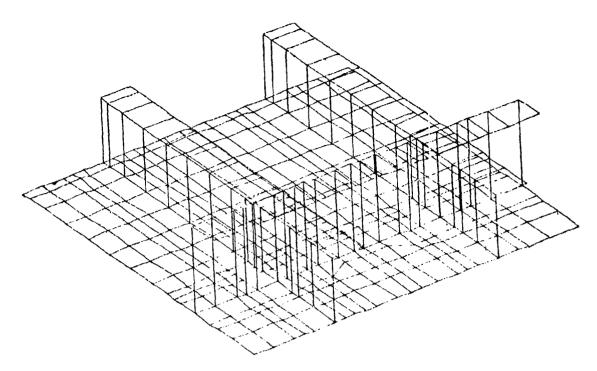


Figure A-3. Finite Element Model of 6 x 3 Center Panel - Flat

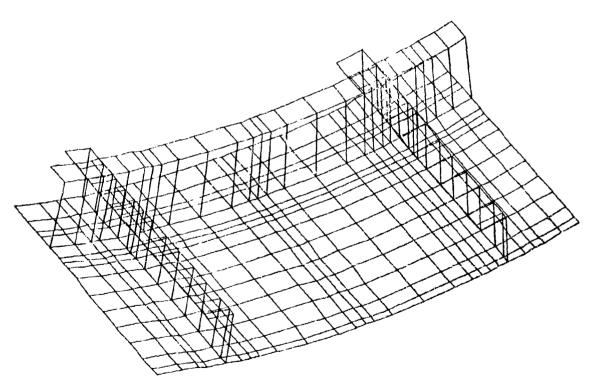


Figure A-4. Finite Element Model of 3 x 3 Center Panel (Radius of Curvature = 30 In.)

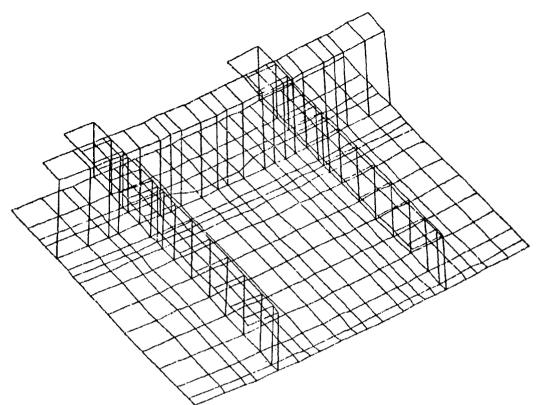
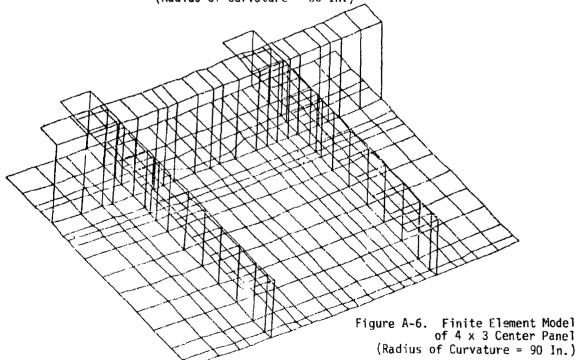


Figure A-5. Finite Element Model of 6 x 3 Center Panel (Radius of Curvature = 60 ln.)



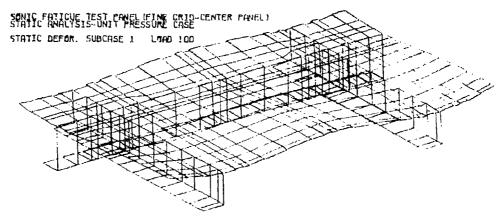


Figure A-7. Static Deformation for Configuration b

1/10/79 MAX-DEF 0.23741999 Z-DISPLACEMENT PLOT	SYMBOL 1 23 45 67 8	VALUE (IN.) 1.213720F-01 1.233218F-01 1.462715F-01 1.557213F-01 1.711711F-01 1.462707F-01 2.035204F-01 2.200702F-01 2.334200E-01
	A	

Figure A-8. Z-Displacement for Configuration b

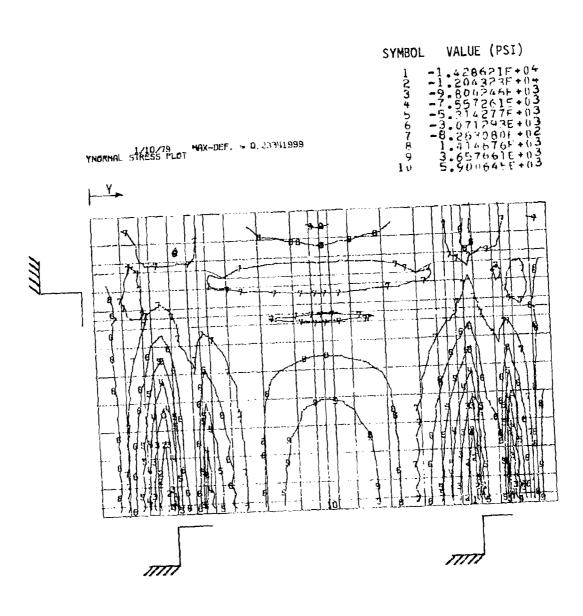


Figure A-9. Normal Stress (y) for Configuration b

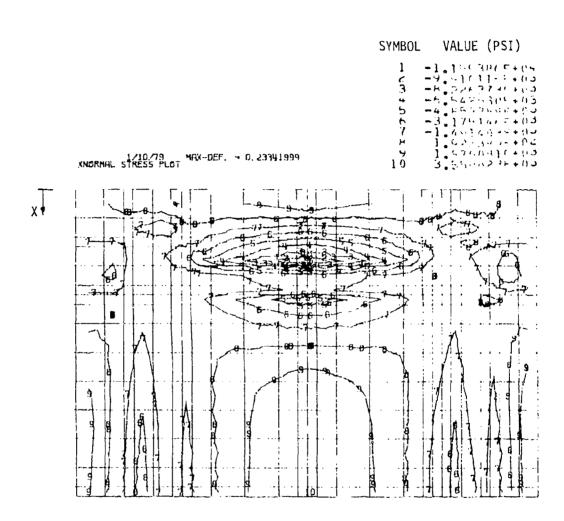


Figure A-10. Normal Stress (x) for Configuration b

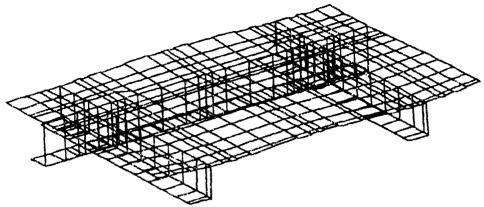


Figure A-11. Static Deformation for Configuration d

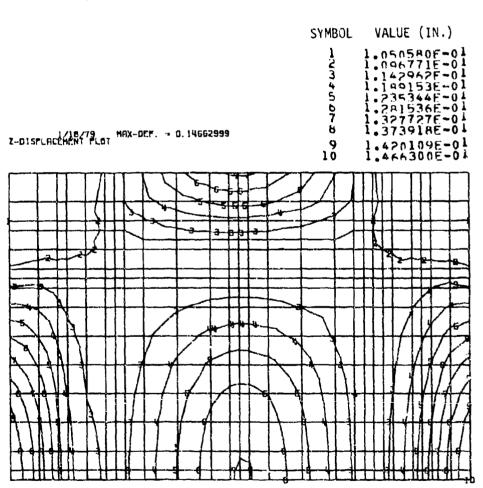


Figure A-12. Z-Displacement for Configuration d

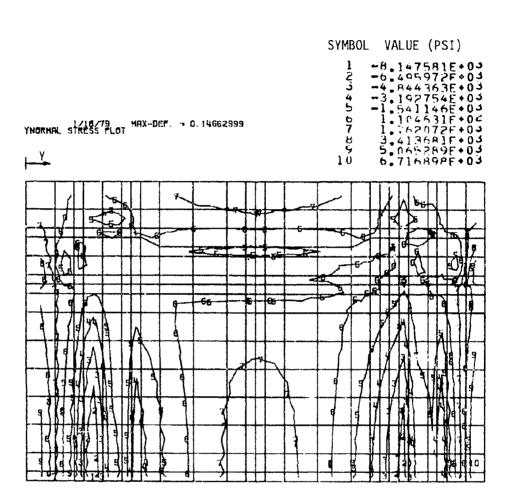


Figure A-13. Normal Stress (y) for Configuration d

	SYMBOL	VALUE (PSI)
	2 - 3 -	3.980429E+03 3.213768F+03 2.447107E+03
	5 - '	1.680446F+03 9.137846F+04 1.471235F+04 6.195376F+04
= U. 14662999	. 8	1.386199E+03 2.152860E+03 2.919521E+03



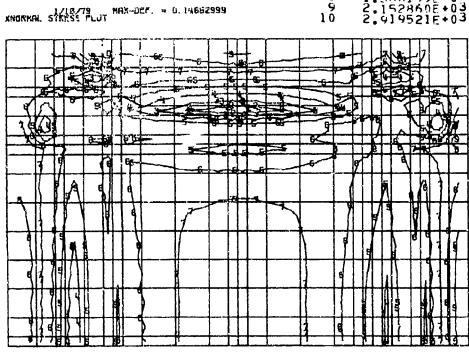


Figure A-14. Normal Stress (x) for Configuration d

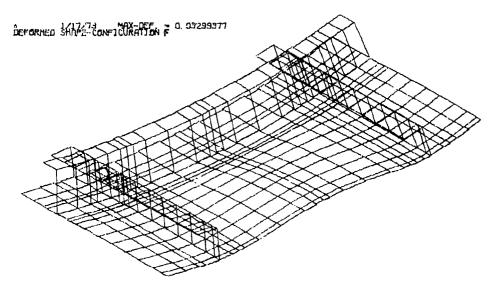


Figure A-15. Static Deformation for Configuration f

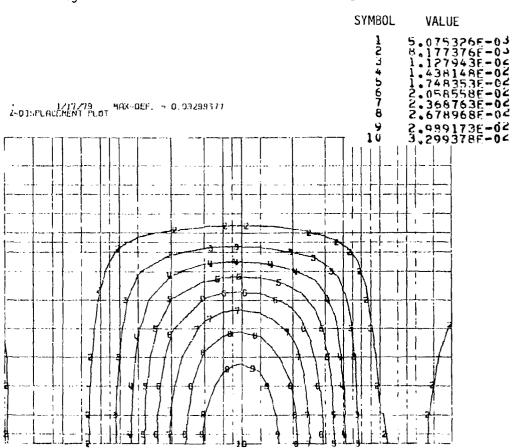
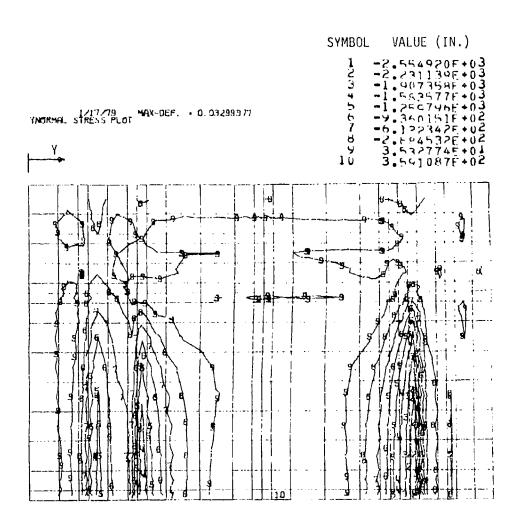


Figure A-16. Z-Displacement for Configuration f



Figur A-17. Normal Stress (y) for Configuration f

The Latest and the la

	SYMBOL	VALUE (PSI)
	1 -1 2 -1 3 -1	683883E+03 60+355696E+03 60+7509E+03
XNORMAL STRESS PLOT	5 - 5 6 - 4 7 2	3.711348F+02 2.8523 F+02 2.8523 F+02 2.134263E+02 2.416133F+03 2.269800E+03
MANUSE SUESS LOS	10 1	.269800E+03

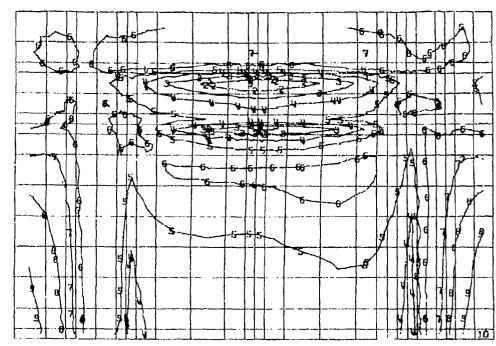


Figure A-18. Normal Stress (x) for Configuration f

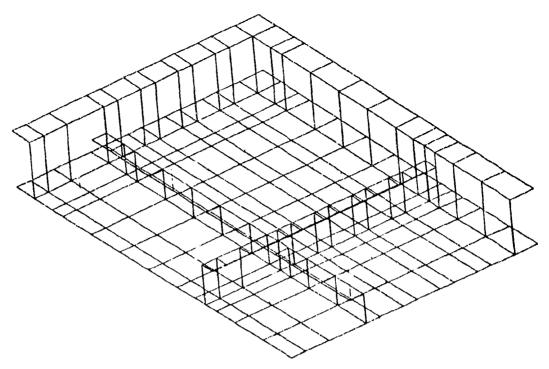


Figure A-19. Flat 3 x 3 Finite Element Model for Dynamic Analysis

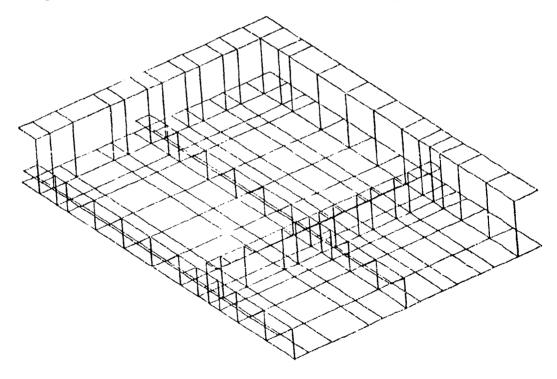


Figure A-20. Flat 4 x 3 Finite Element Model for Dynamic Analysis

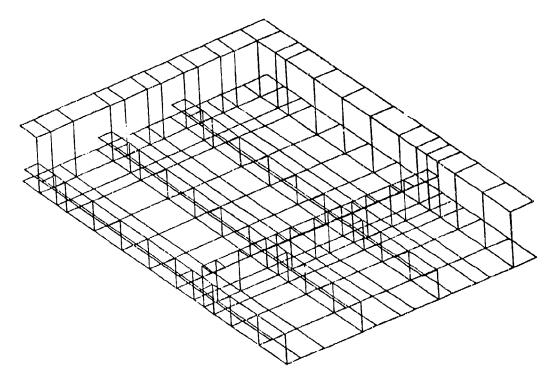


Figure A-21. Flat 6 x 3 Finite Element Model for Dynamic Analysis

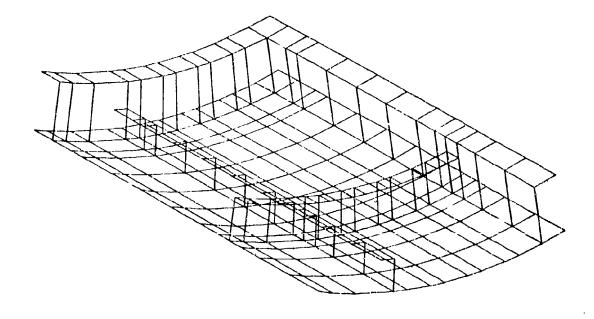


Figure A-22. Curved (R=30) 3 x 3 Finite Element Model for Dynamic Analysi

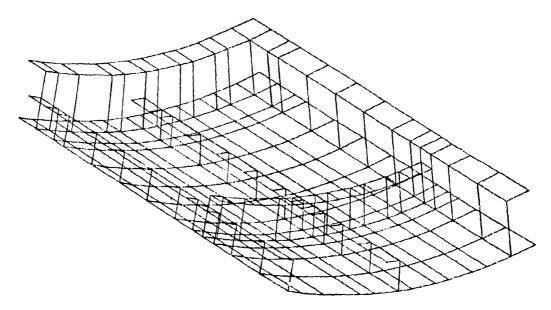


Figure A-23. Curved (R=30) 4 x 3 Finite Element Model for Dynamic Analysis

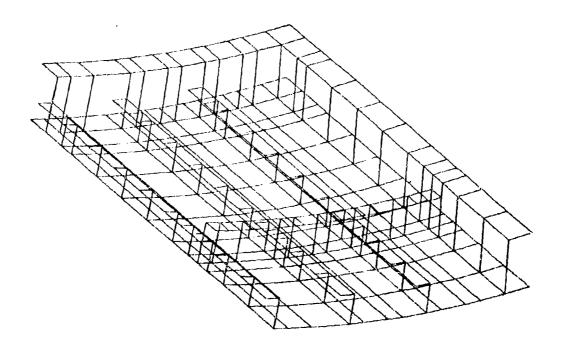


Figure A-24. Curved (R=60) 6 x 3 Finite Element Model for Dynamic Analysis

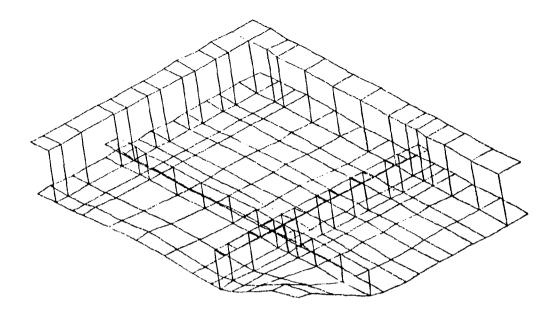


Figure A-25. First (Fundamental) Harmonic for Panel b ($f_1 = 171 \text{ Hz}$)

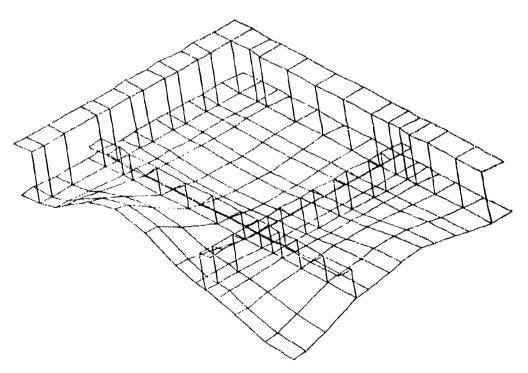


Figure A-26. Second Harmonic for Panel b ($f_2 = 177 \text{ Hz}$)

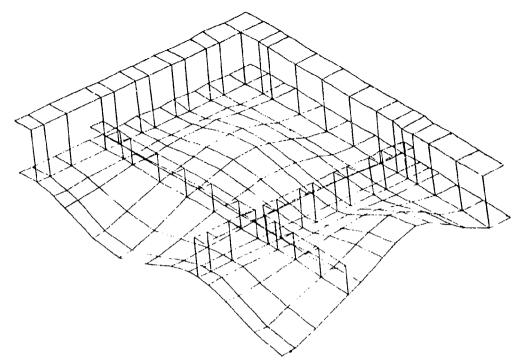


Figure A-27. Third Harmonic for Panel b ($f_3 = 189 \text{ Hz}$)

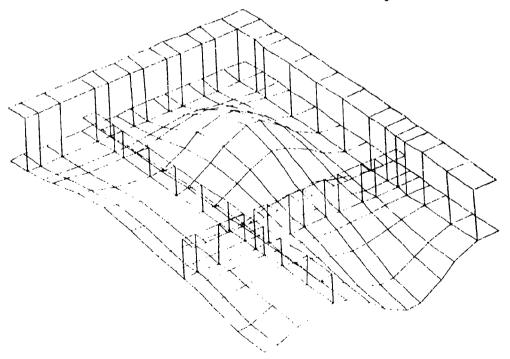


Figure A-28. Fourth Harmonic for Panel b (f_4 = 213 Hz)

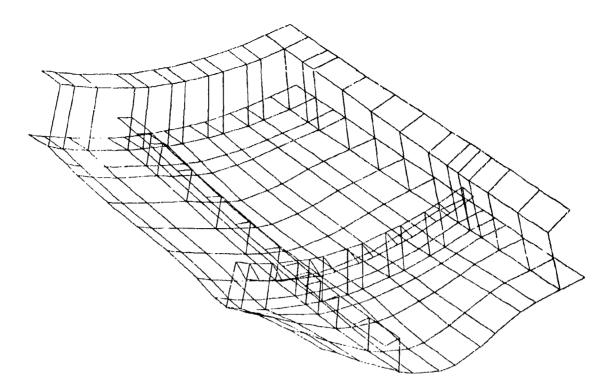


Figure A-29. First (Fundamental) Harmonic for Panel f ($f_1 = 343 \text{ Hz}$)

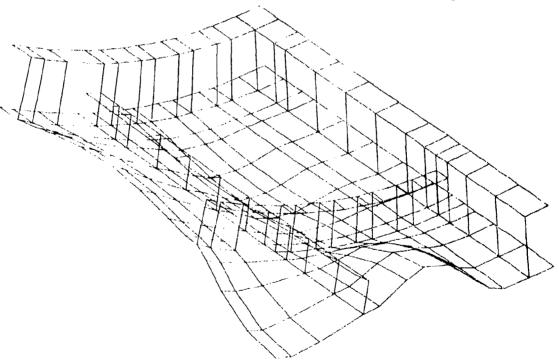


Figure A-30. Second Harmonic for Panel f ($f_2 = 463 \text{ Hz}$)

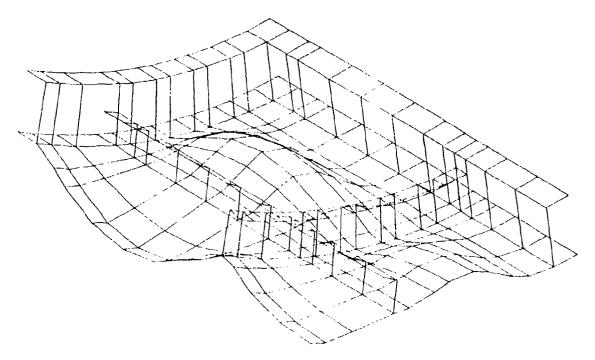
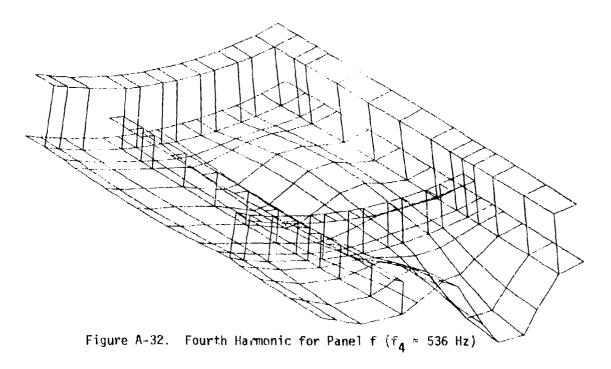


Figure A-31. Third Harmonic for Panel f ($f_3 = 483 \text{ Hz}$)



APPENDIX B

ENGINEERING DRAWINGS OF TEST STRUCTURES

Figures B-1 through B-3 are engineering drawings for the sonic fatigue test panels and the shaker test specimens. The test panel drawings show strain gauge locations and their corresponding numbers. Hercules 3501 graphite/epoxy system was used for the laminates. Stiffener-skin bonds utilized the 3M AF147 adhesive.

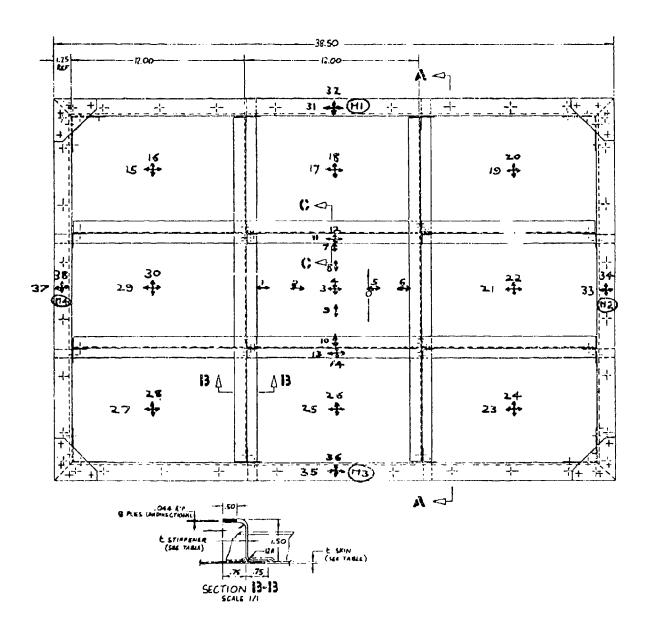
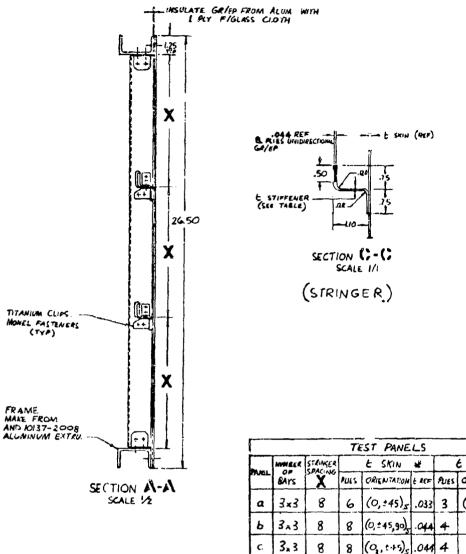


Figure B-1. Fatigue Test Panels (Sheet 1 of 3)



	HVMRER	STRINGER SPACING	E SKIN #			E STIFFENER +			
MAGL	BAYS	X	PUES	ORIENTATION	t lef	Pues	ORIENTATION ER		
а	3×3	8	6	(0,±45) _s	.033	3	(±45)eer	.039	
Ь	343	8	8	(0,±45,90) _s	-044	4		-052	
С.	3×3	8	8	(O, 145)s	.044	4		. 052	
d	3,3	8	12	(0, : 45)25	.066	6		.078	
į	6x3	4	L	(O, ± 45,90)			1	052	
k	4 x3	6	8	(0,: 45,90)	.044	4	(+ 45) REF	052	
⇒ GR/EP TAPE † GR/EP FABRIC (HERCULES 2501)									
2	3×3	8	4	(0 e)	.022	3	(245) REF	-035	
2	6×3	4	4	(0.90),	1022	3	(245)REF	.035	

Figure B-1. Fatigue Test Panels (Sheet 1 of 3) - Continued

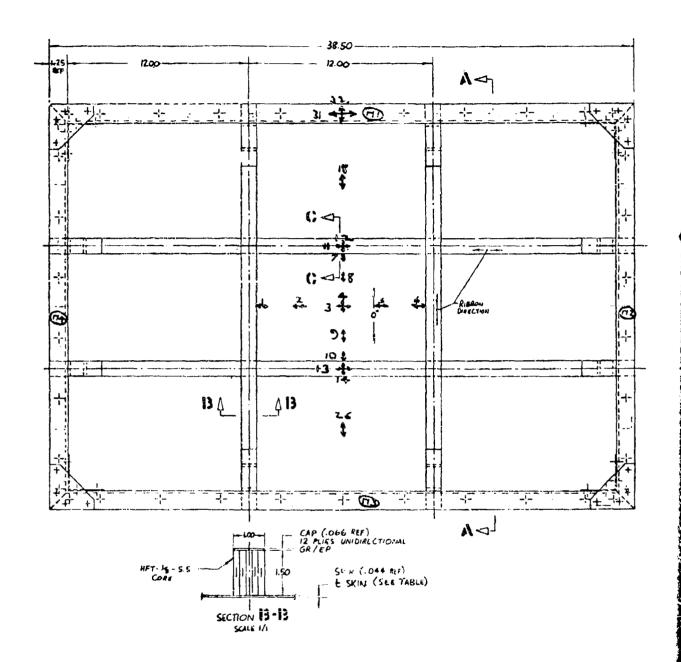


Figure B-1. Fatigue Test Panels (Sheet 2 of 3)

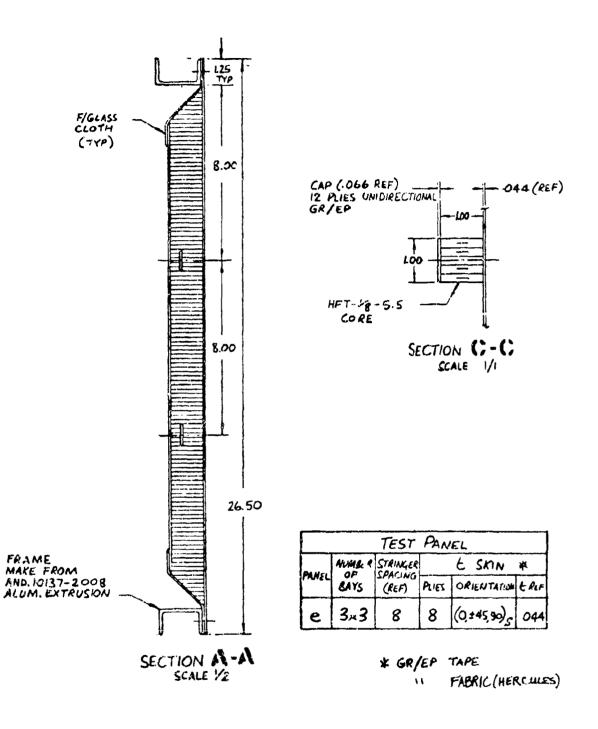


Figure B-1. Fatigue Test Panels (Sheet 2 of 3) - Continued

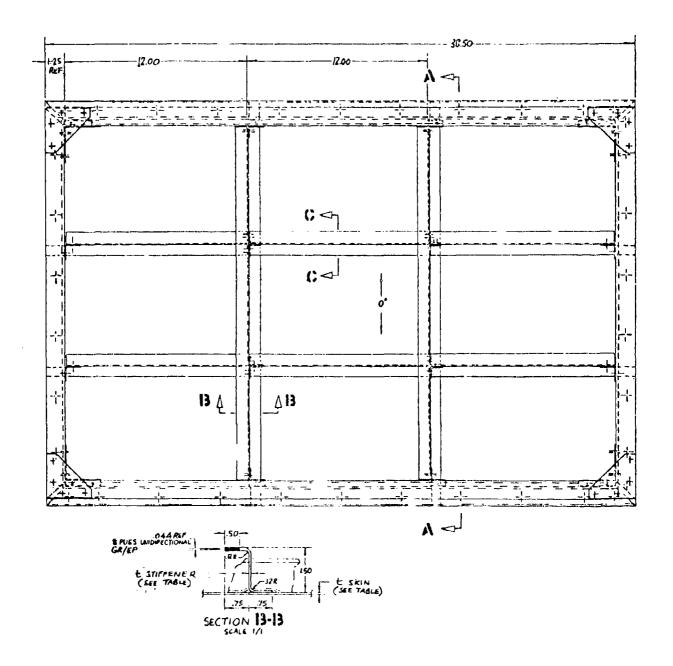


Figure B-1. Fatigue Test Panels (Sheet 3 of 3)

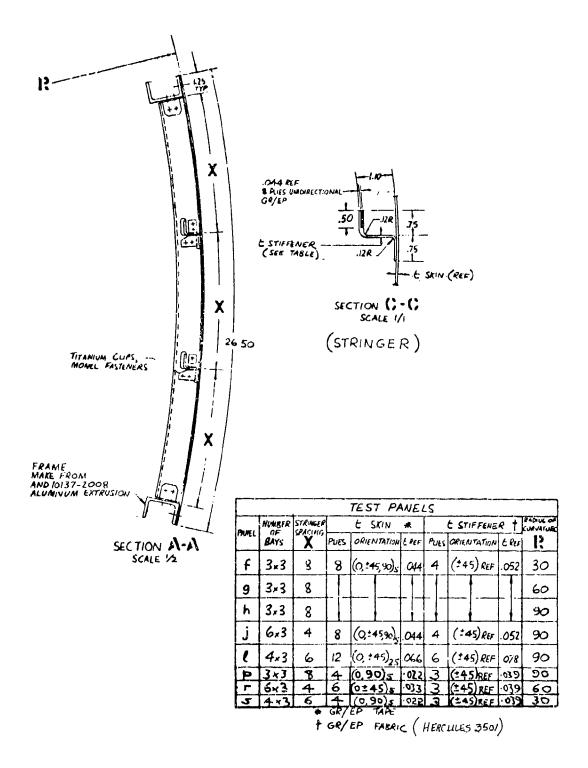


Figure B-1. Fatigue Test Panels (Sheet 3 of 3) - Concluded

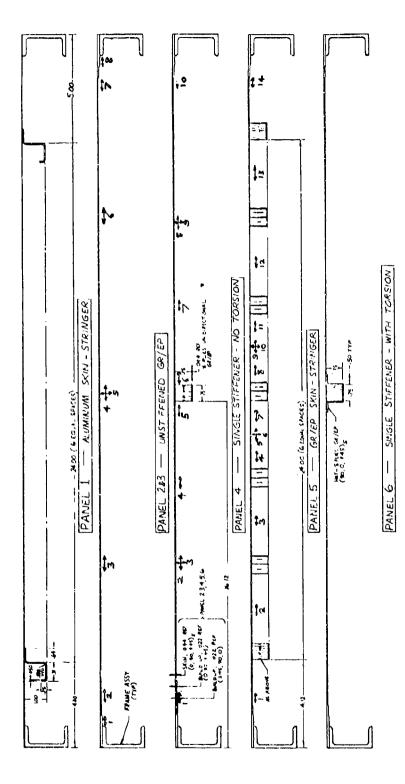
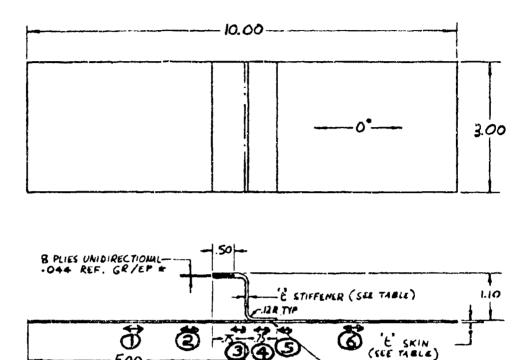


Figure B-2. Existing Rohr Test Panel Configurations

457

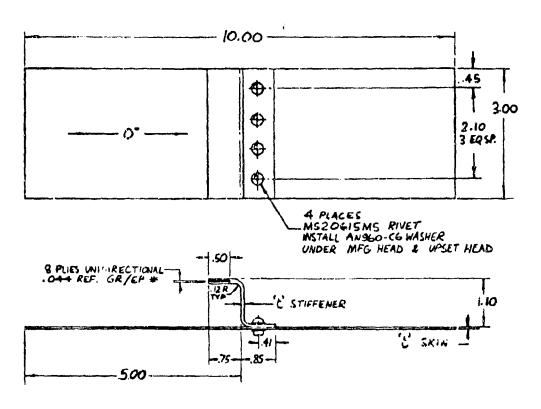


TYPE A

AF 147

STRAIN GANGE NUMBERS & LOCATIONS

Figure B-3. Shaker Test Specimens (Sheet 1 of 3)



TYPE B

SHAKER SPECIMENS								
SPECIMEN	SPECIMEN TYPE		F, ZKIN W		'E' STIFFENER T			
	TYPE	SPECIMENS	PLIES	OFICHTATION	t REF	PLIES	OCIENTATING	E REF
1	Α	15	6	(0, ± +5) ₅	.033	3	(145)10	. 03 9
2	Α	15	8	(0:45,90)S	-044	4	(±45)AF	. 052
3	Α	10	8	(0, :45)s	.044	4	(±45) REF	.052
4	Α	15	12	(0, :45)25	.066	6	(245) REF	.078
5	С	10	8	(0. 45.90) ₅	.044	NO7	APPLICA	BLE
6	В	6	8	(0, :45,90)5	.044	4	(±45)4r	.052
			# GR/EP TAPE - 3501 AS GR/EP FABRIC-					
7	Α	10	4	(0,90)5	.022	SAM	E AS	1

Figure B-3. Shaker Test Specimens (Sheet 2 of 3)

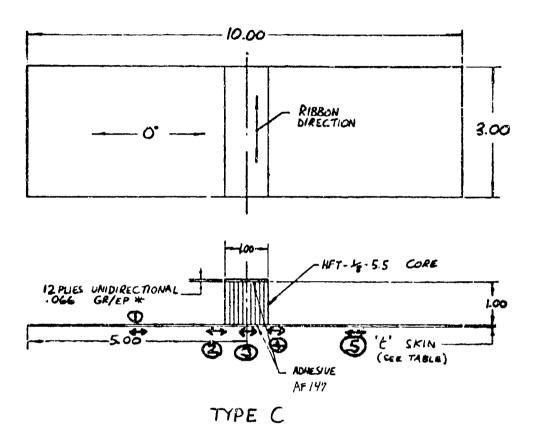


Figure B-3. Shaker Test Specimens (Sheet 3 of 3)

APPENDIX C TEST DATA USED IN THE DEVELOPMENT OF THE DESIGN METHOD

This section contains acoustic and strain spectra and associated overall rms levels that are pertinent to the development of the design method. Figures C-1 through C-7 show microphone spectra for a sine sweep and for each test acoustic load level. Figures C-8 through C-101 show strain spectra and their corresponding overall rms strain levels for strain gauge number 10 (located at the center of, and normal to, the longest side of the center bay -- see Figure B-1). Spectra are shown for sine sweeps and broadband random acoustic loading from 140 dB up to (in most cases) 165 dB in 5 dB increments for the following panel configurations: a1, b2, d, f2, g2, h, i, j, k1, l, n, o, p, q, r and s.

All spectra have an effective filter bandwidth of 2-16 Hz with an aliasing filter cutoff of 960 Hz. Twenty-second samples were used for all spectral analysis.

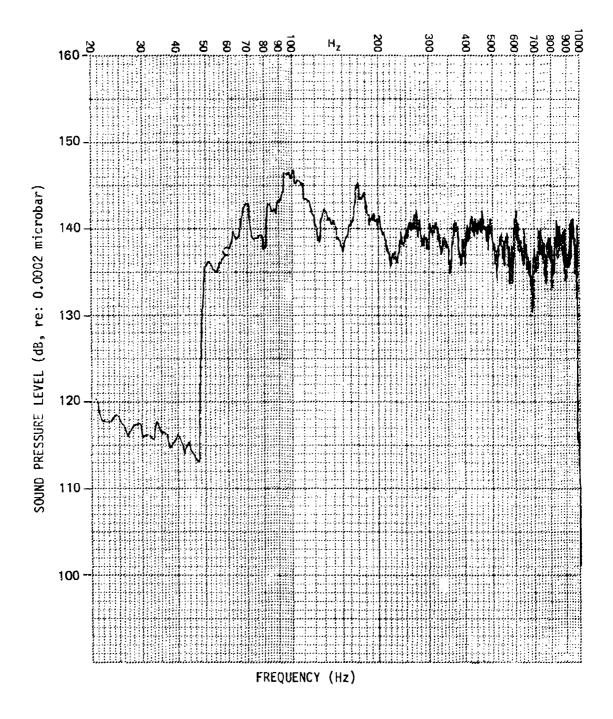


Figure C-1. Microphone Spectrum - Sine

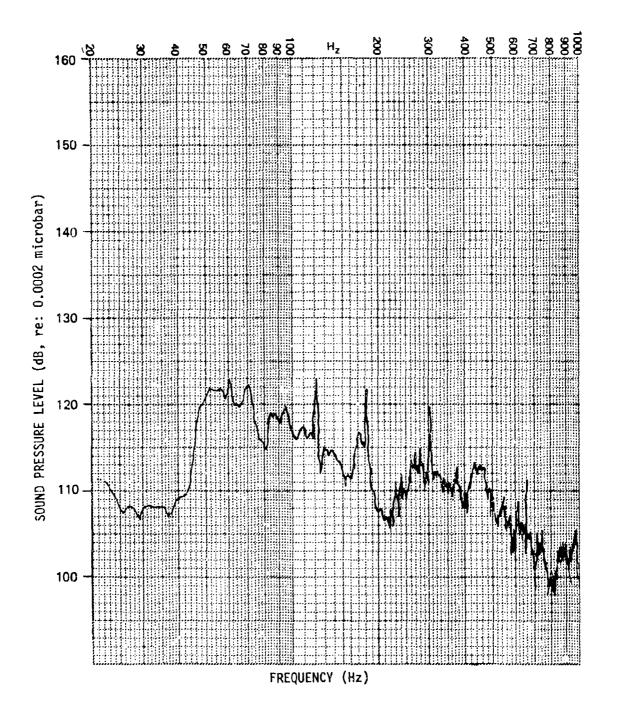


Figure C-2. Microphone Spectrum - 140 dB Random

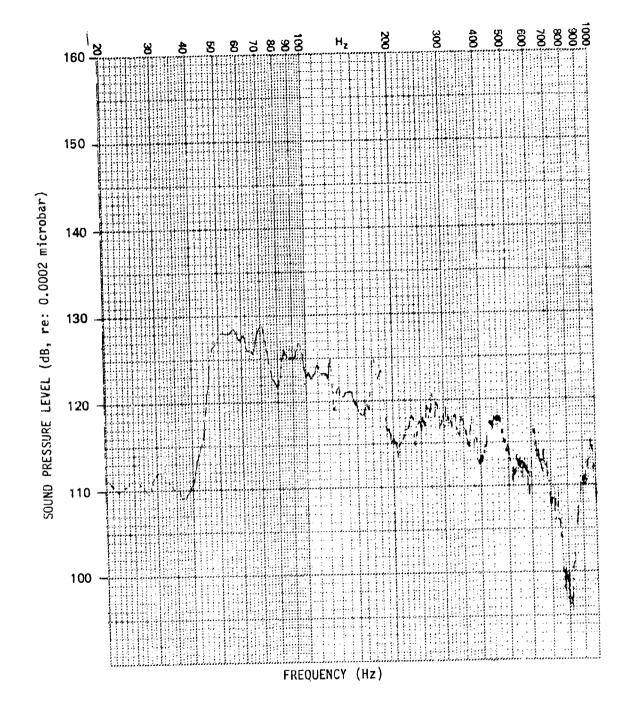


Figure C-3. Microphone Spectrum - 145 dB Random

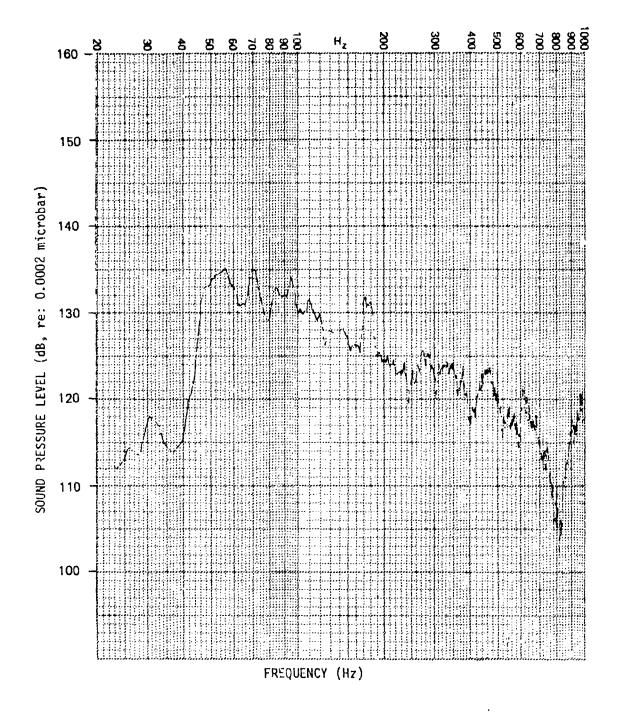


Figure C-4. Microphone Spectrum - 150 dB Random

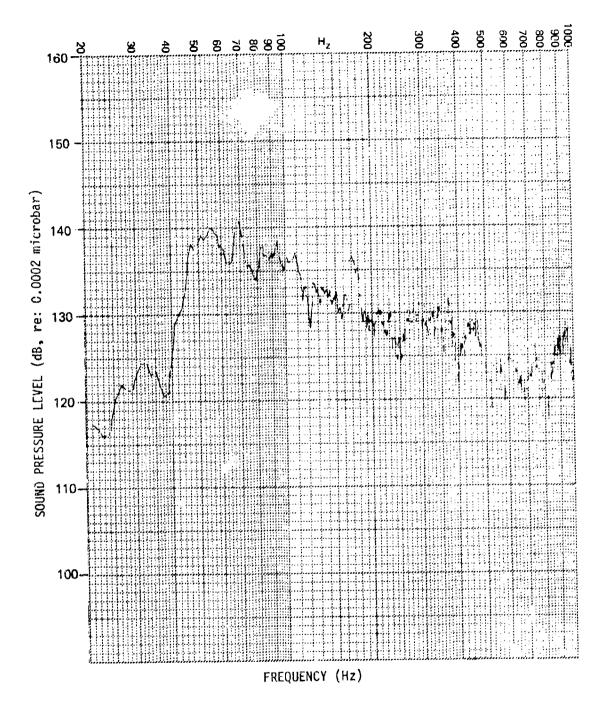


Figure C-5. Microphone Spectrum - 155 dB Random

C-6

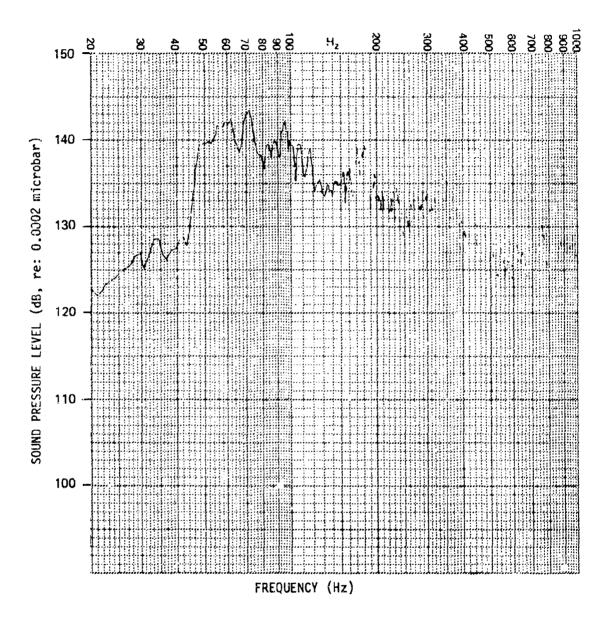


Figure C-6. Microphone Spectrum - 160 dB Random

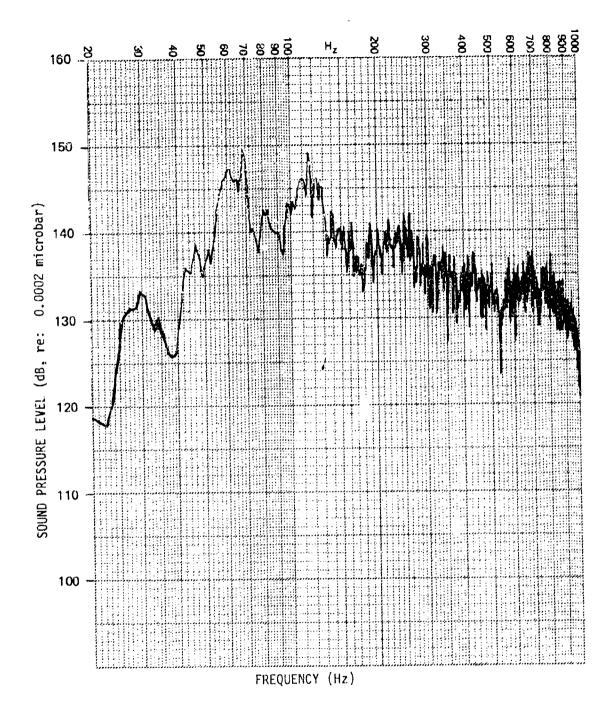


Figure C-7. Microphone Spectrum - 165 dB Random

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

a1 G10

SINE 130 dB

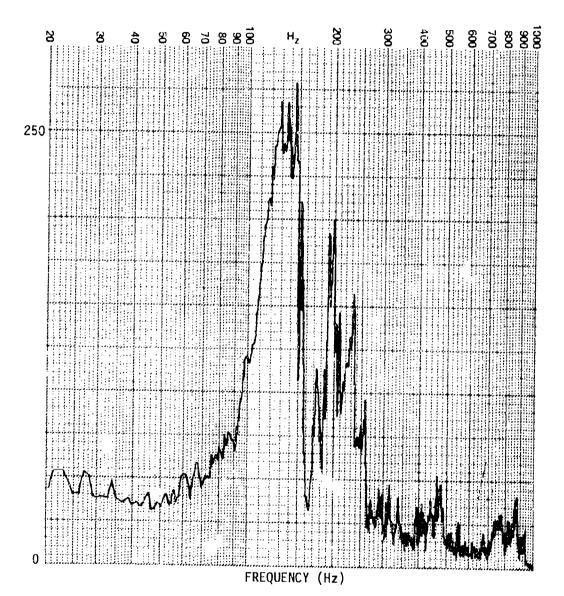


Figure C-8. Strain Spectrum for Panel al

PANEL CONFIGURATION: a1
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 101.
INPUT SPECTRUM: RAN

INPUT LEVEL:

101.7µe RANDOM 140 dB



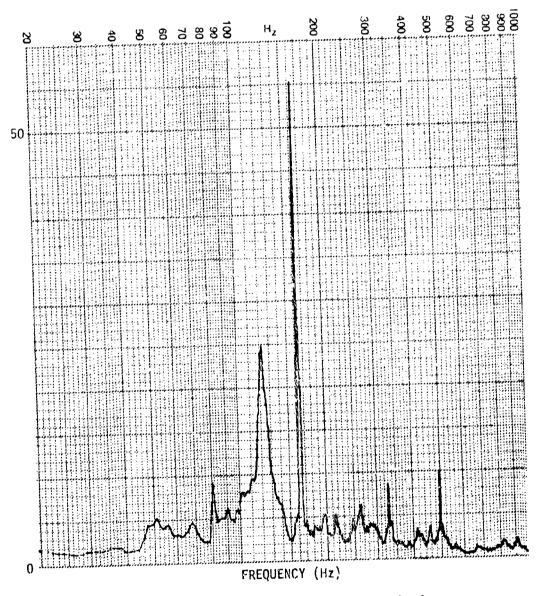


Figure C-9. Strain Spectrum for Panel al

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

161.1µe RANDOM 145 dB

a1

G10

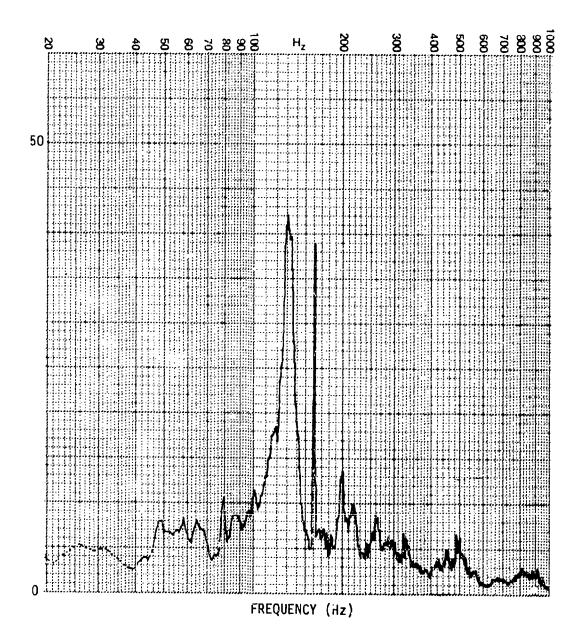


Figure C-10. Strain Spectrum for Panel a1

PANEL CONFIGURATION: a1
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 224.7µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 150 dB

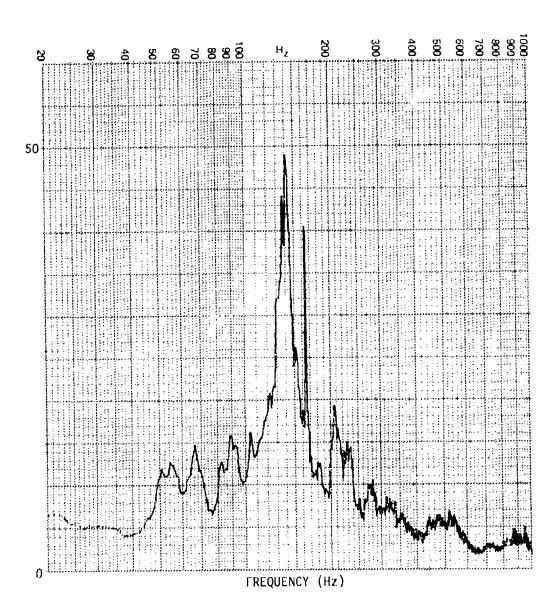


Figure C-11. Strain Spectrum for Panel al

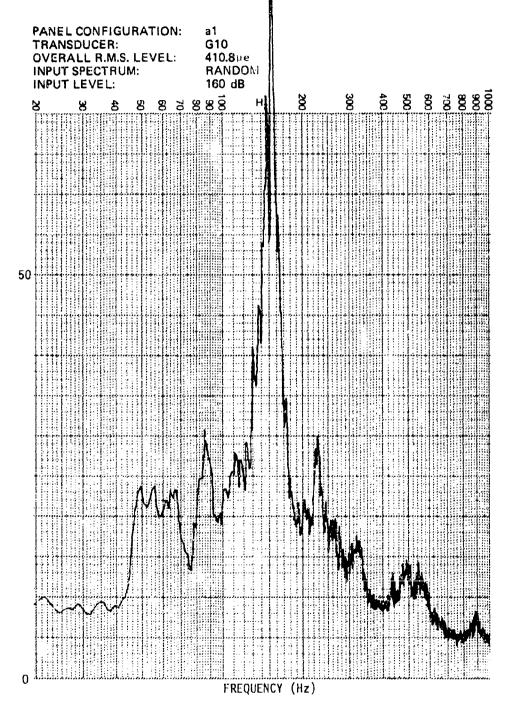


Figure C-12. Strain Spectrum for Panel al

TRANSDUCER:

b2 G10

OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT SPECTRUM: INPUT LEVEL: SINE 130 dB

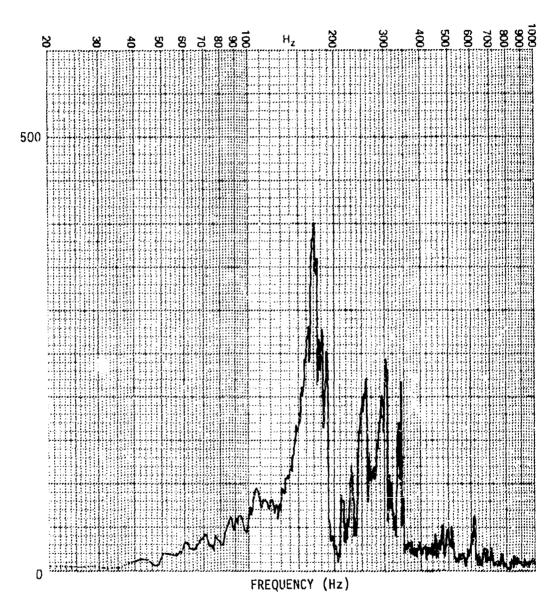
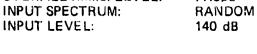


Figure C-13. Strain Spectrum for Panel b2

PANEL CONFIGURATION: b2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 77.3µe
INPUT SPECTRUM: RANDO



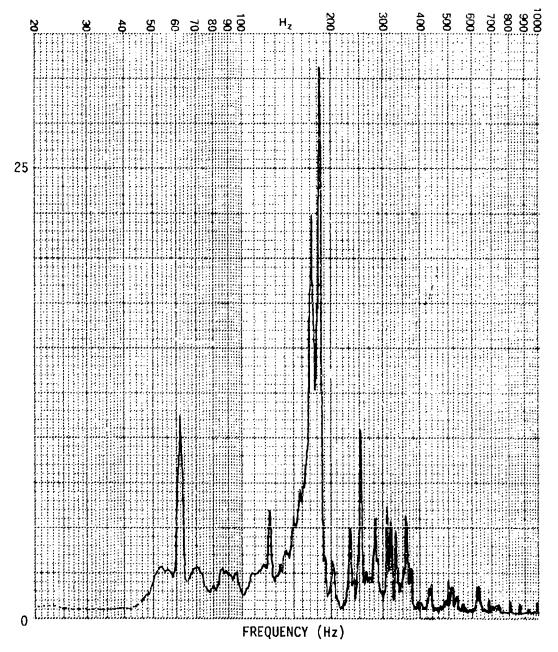


Figure C-14. Strain Spectrum for Panel b2

PANEL CONFIGURATION: b2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 147.1µe
INPUT SPECTRUM: RANDOM
INPUT LEVEI: 145 dB

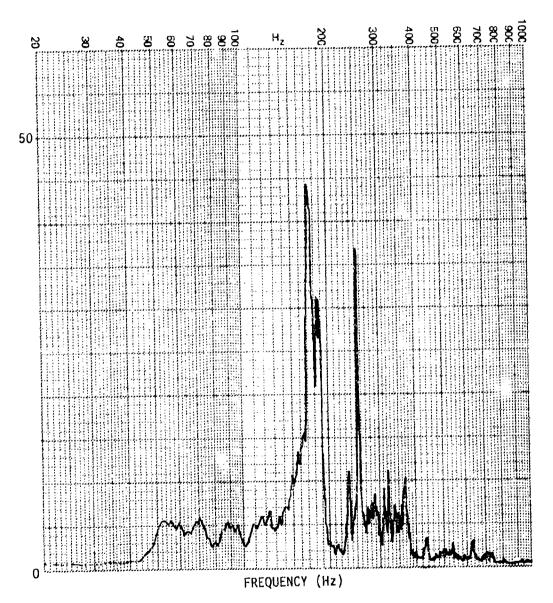


Figure C 15. Strain Spectrum for Panel b2

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

b2 G10 266.8ye RANDOM 150 dB

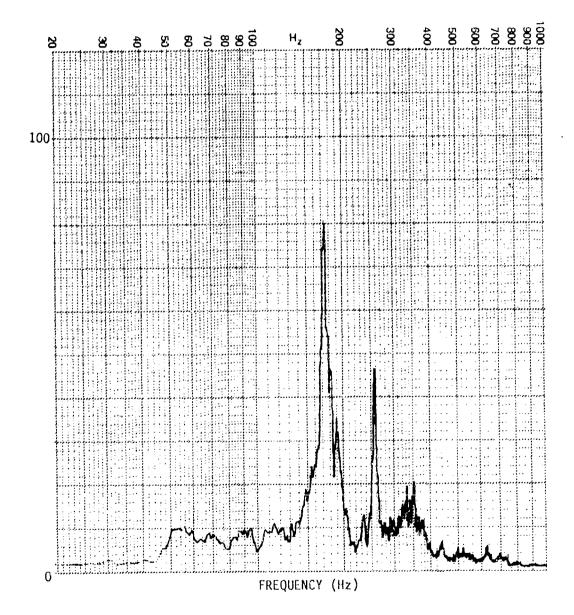


Figure C-16. Strain Spectrum for Panel b2

PANEL CONFIGURATION: b2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 357.7µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 155 dB

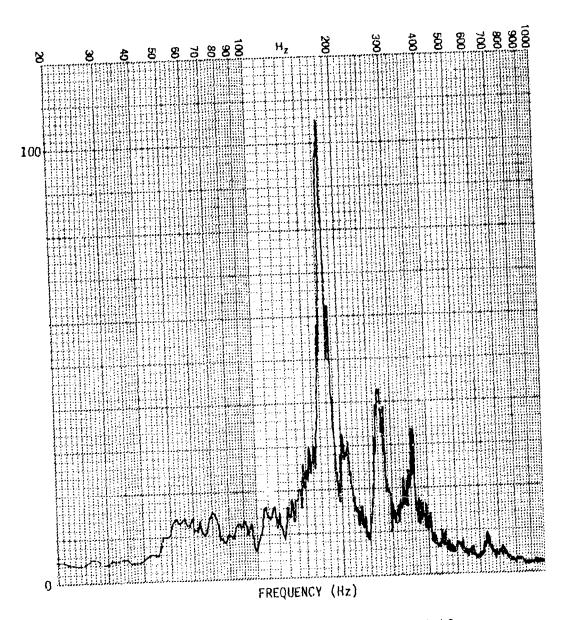


Figure C-17. Strain Spectrum for Panel b2

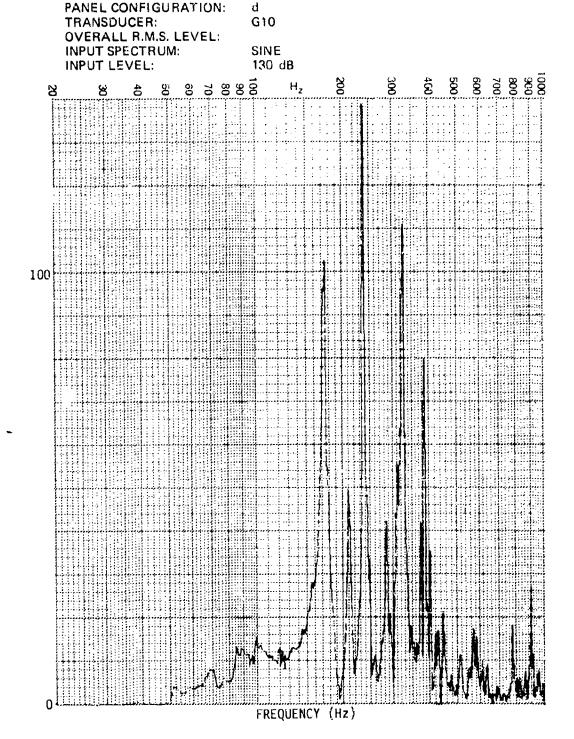


Figure C-18. Strain Spectrum for Panel d

PANEL CONFIGURATION: d
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 33.5 μe
INPUT SPECTRUM RANDOM
INPUT LEVEL: 140 dB

11

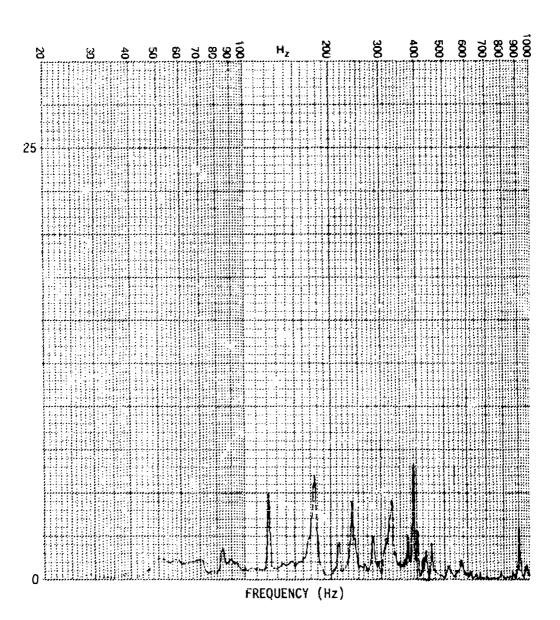


Figure C-19. Strain Spectrum for Panel d

PANEL CONFIGURATION: d
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 56.9µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 145 dB

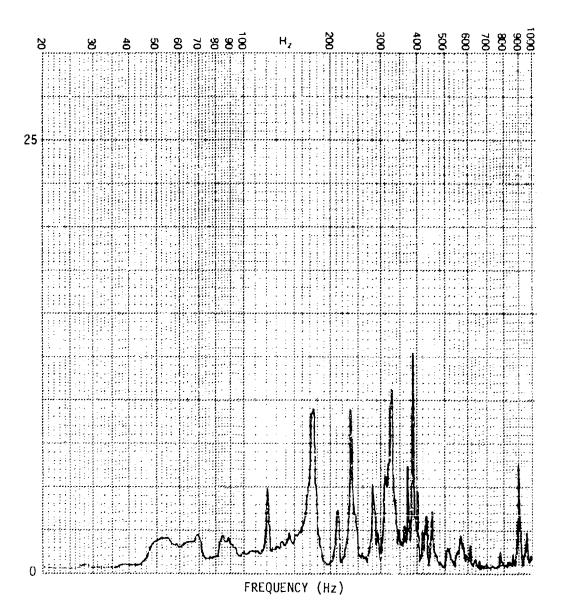


Figure C-20. Strain Spectrum for Panel d

PANEL CONFIGURATION: d TRANSDUCER: G10 OVERALL R.M.S. LEVEL: 101.0µe INPUT SPECTRUM: RANDOM INPUT LEVEL: 150 dB

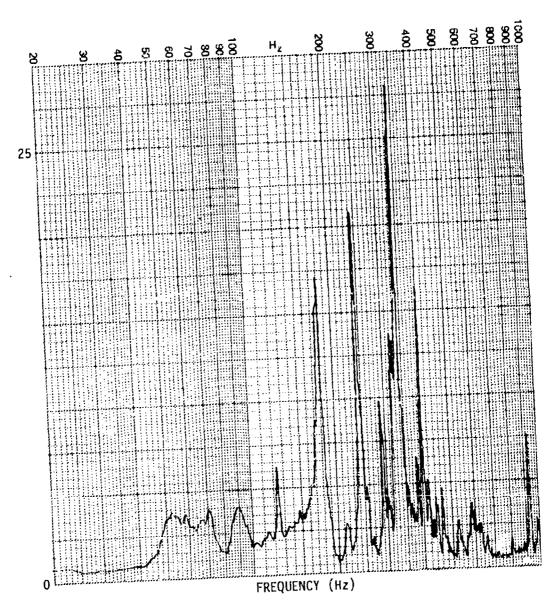


Figure C-21. Strain Spectrum for Panel d

PANEL CONFIGURATION: d
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 174.1pe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 155 dB

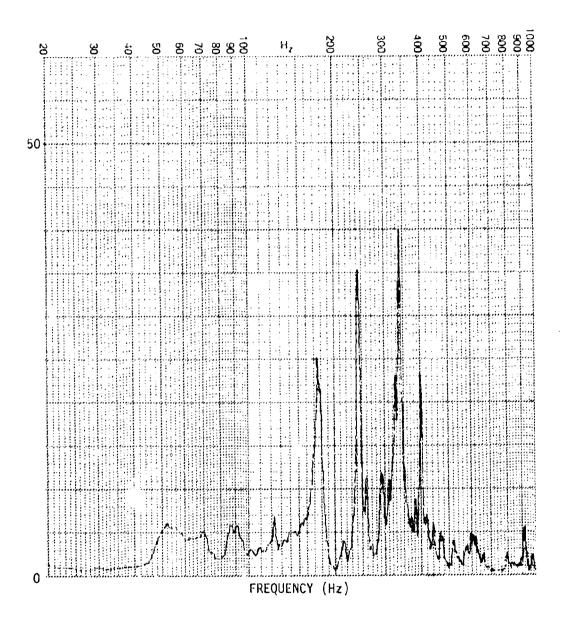


Figure C-22. Strain Spectrum for Panel d

PANEL CONFIGURATION: d
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 274.2
INPUT SPECTRUM: RAN
INPUT LEVEL: 160

274.2µe RANDOM 160 dB

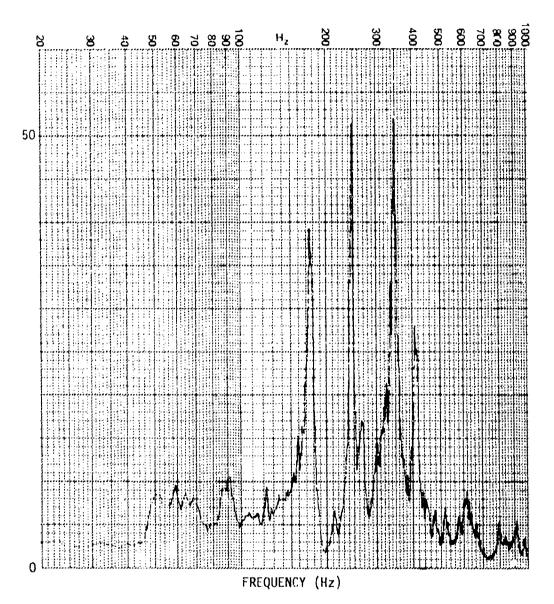


Figure C-23. Strain Spectrum for Panel d

TRANSDUCER:

f2 Gï0

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM:

SINE

INPUT LEVEL: 130 dB

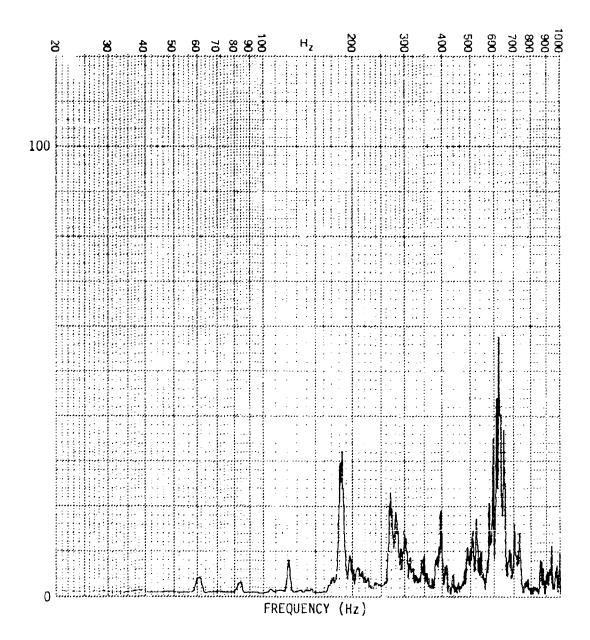


Figure C-24. Strain Spectrum for Panel f2

PANEL CONFIGURATION: f2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 22.3 µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 140 dB

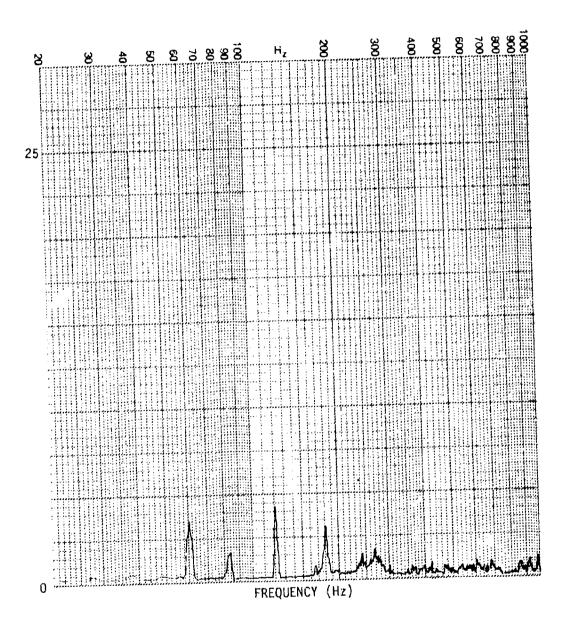


Figure C-25. Strain Spectrum for Panel f2

PANEL CONFIGURATION: f2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 30.0 µc
INPUT SPECTRUM: RANDO

INPUT SPECTRUM: RANDOM
INPUT LEVEL: 145 dB

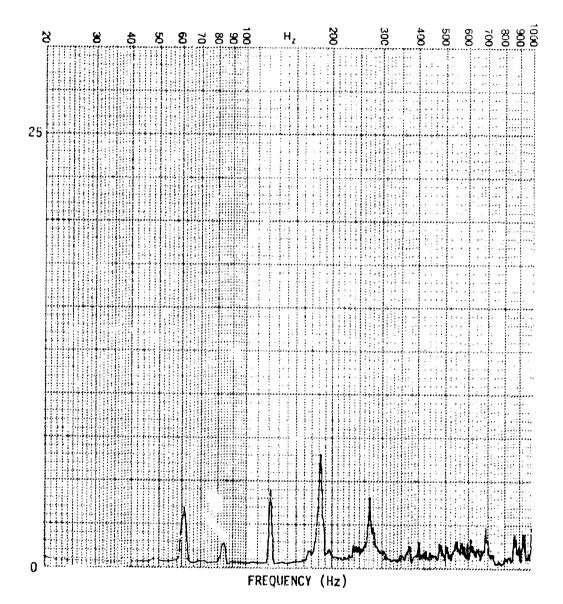


Figure C-26. Strain Spectrum for Panel f2

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL: f2 G10 48.5#e RANDOM 150 dB

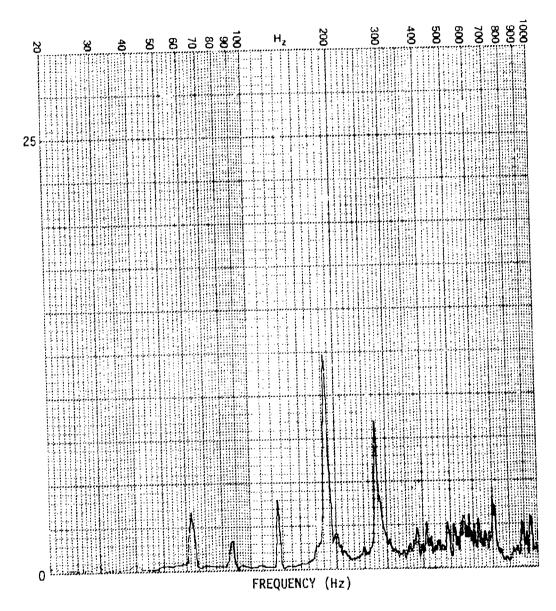


Figure C-27. Strain Spectrum for Panel f2

PANEL CONFIGURATION: f2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 77.6 µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 155 dB

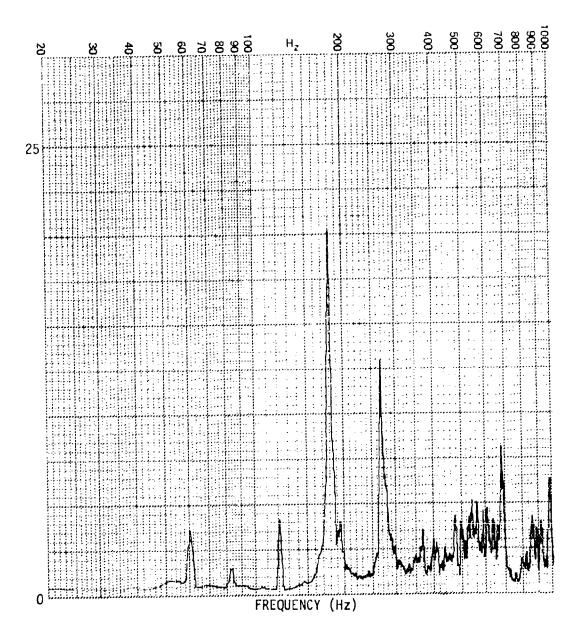


Figure C-28. Strain Spectrum for Panel f2

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

f2 G10 153.6μe RANDOM 160 dB

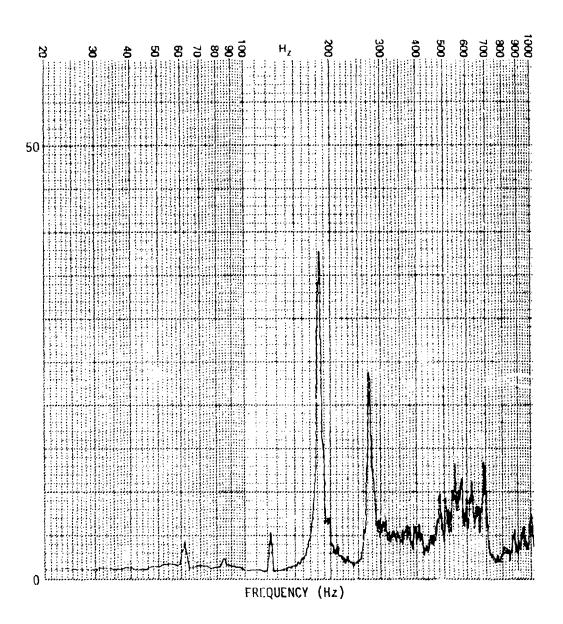


Figure C-29. Strain Spectrum for Panel f2

TRANSDUCER: OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

.4

f2 G10

247.4µe RANDOM 165 dB

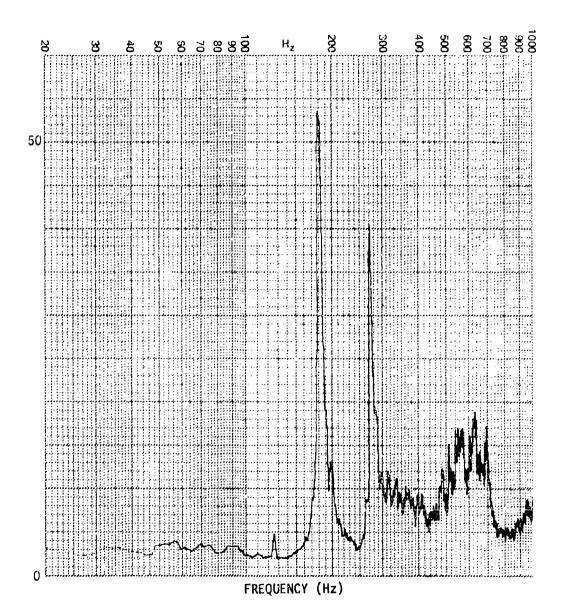


Figure C-30. Strain Spectrum for Panel f2

TRANSDUCER:

g2 G10

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM:

SINE

INPUT LEVEL:

130 dB

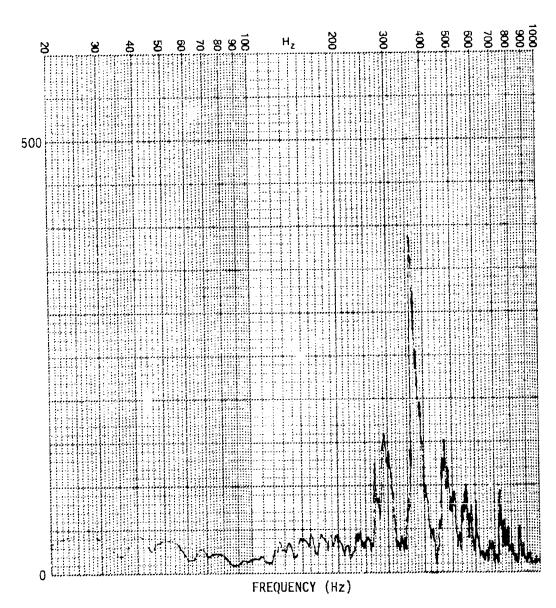


Figure C-31. Strain Spectrum for Panel g2

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

92 G10 51.0µe RANDOM 140 dB

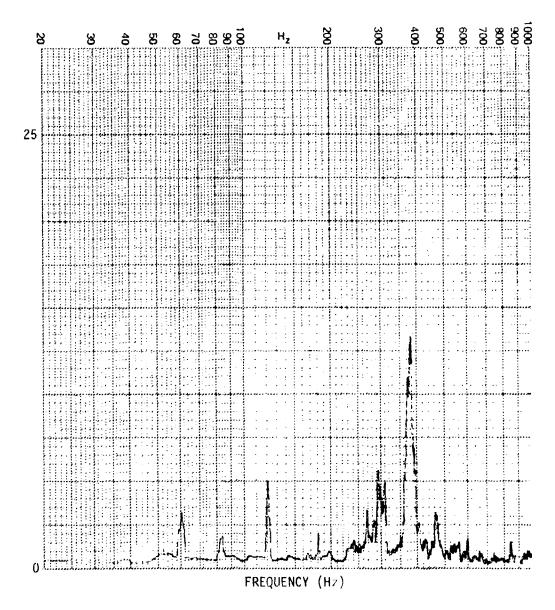


Figure C-32. Strain Spectrum for Panel g2

PANEL CONFIGURATION: 92
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 92.9 µe
INPUT SPECTRUM: RAINDOM
INPUT LEVEL: 145 dB

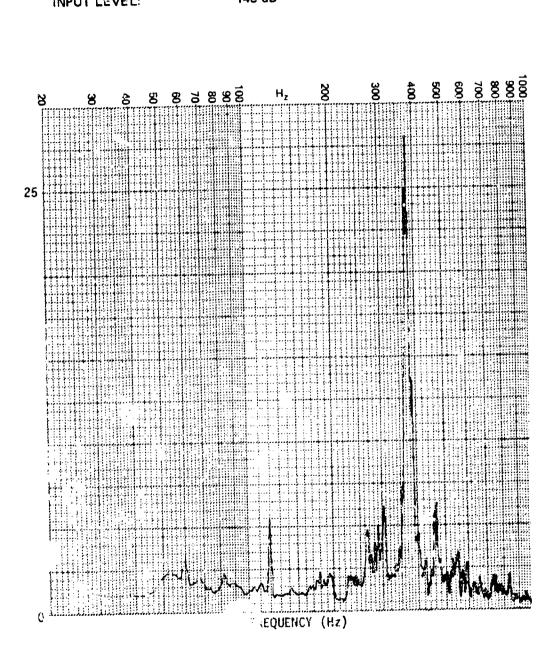


Figure 0 33. Strain Spectrum for Panel 92



PANEL CONFIGURATION: "RANSDUCER: OVERALL R.M.S. LEVEL:

Ğ10 151.4µe RANDOM INPUT SPECTRUM:

g2

INPUT LEVEL:

150 dB

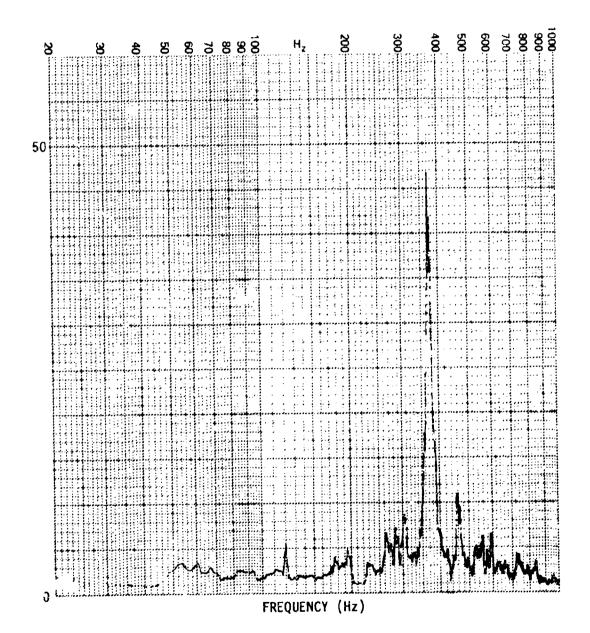


Figure C-34. Strain Spectrum for Fanel g2

PANEL CONFIGURATION: 92
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 250
INPUT SPECTRUM: RA
INPUT LEVEL: 150

G10 250.0ue RANDOM 155 dB

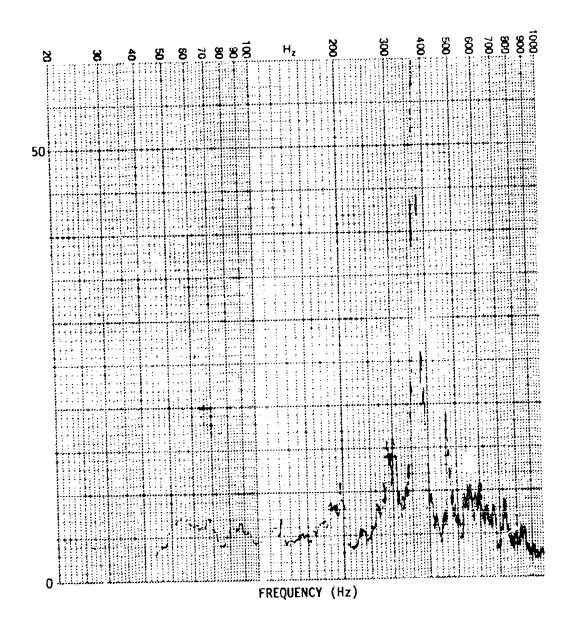


Figure C-35. Strain Spectrum for Panel g2

PANEL CONFIGURATION: m2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 400. The
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 160 dB

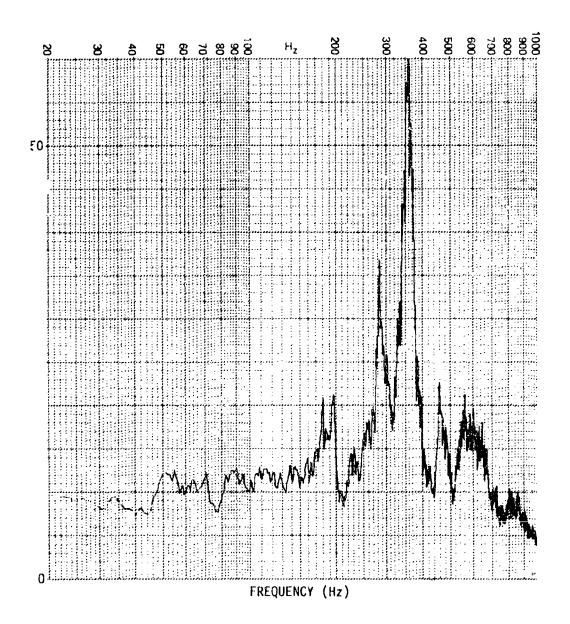


Figure C-36. Strain Spectrum for Panel g2

PANEL CONFIGURATION: g2
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 595.4µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 165 dB

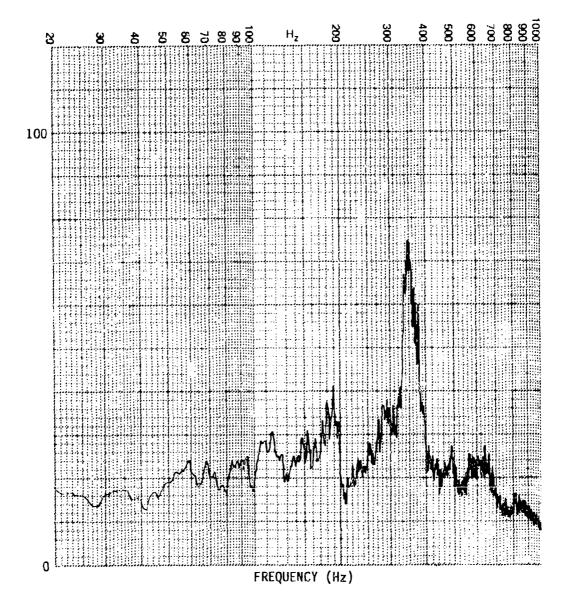


Figure C-37. Strain Spectrum for Panel g2

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

h G10

SINE 130 dB

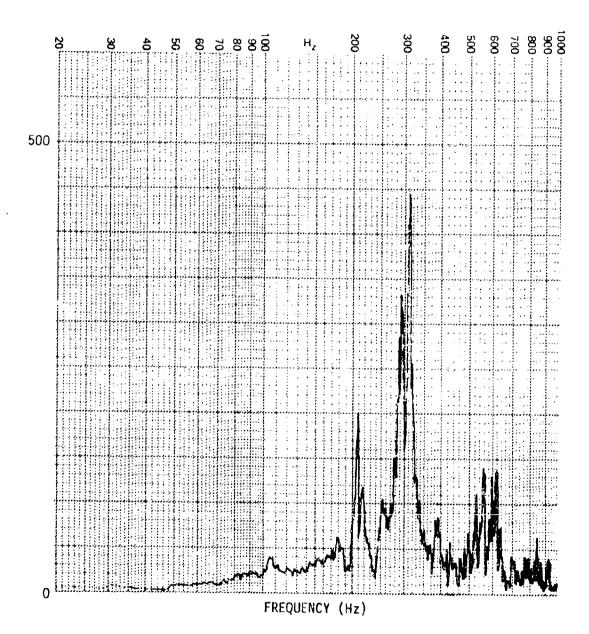


Figure C-38. Strain Spectrum for Panel h

PANEL CONFIGURATION: h
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 54.1 µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 140 dB

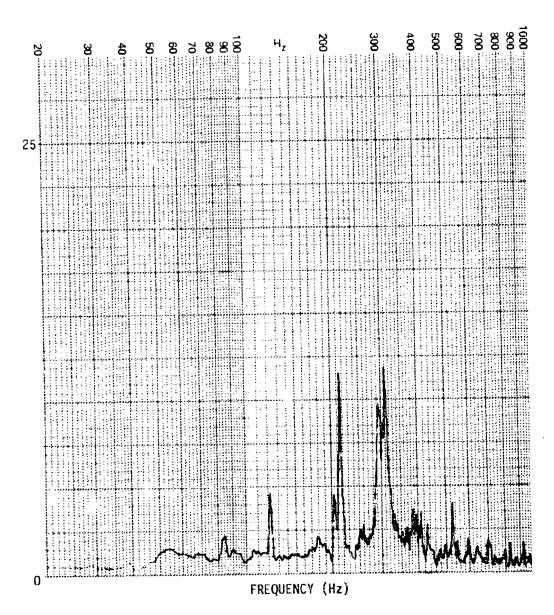


Figure C-39. Strain Spectrum for Panel h

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL: G10 101.1 µe RANDOM 145 dB

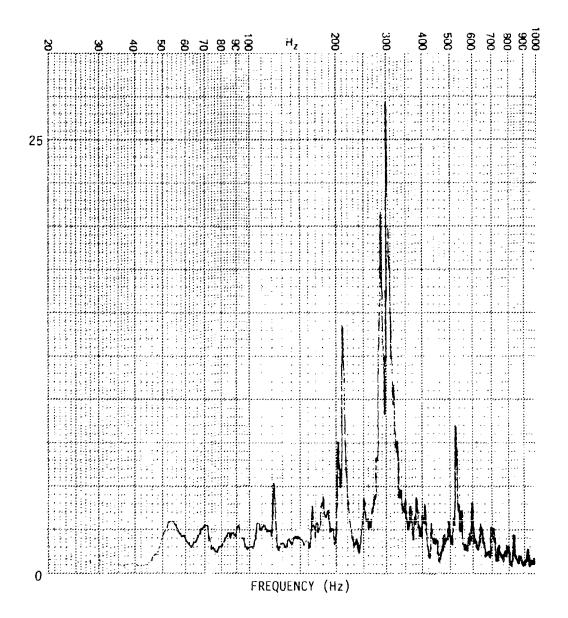


Figure C-40. Strain Spectrum for Panel h

PANEL CONFIGURATION: h
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 150.2 μe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 150 dB

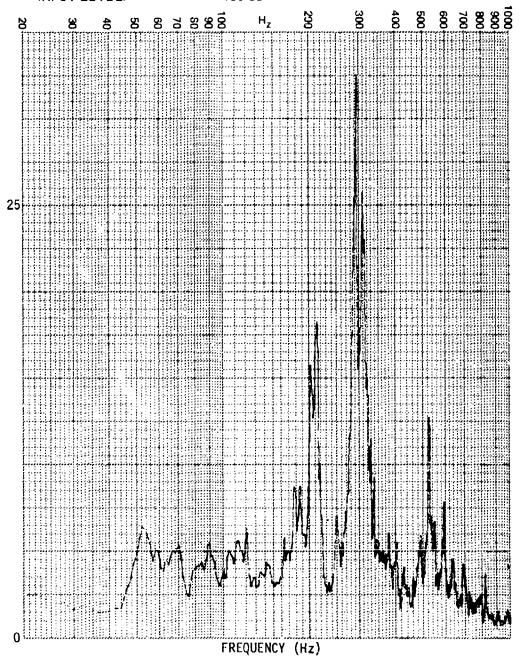


Figure C-41. Strain Spectrum for Panel h

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL: G10 285.7 ne RANDOM 155 dB

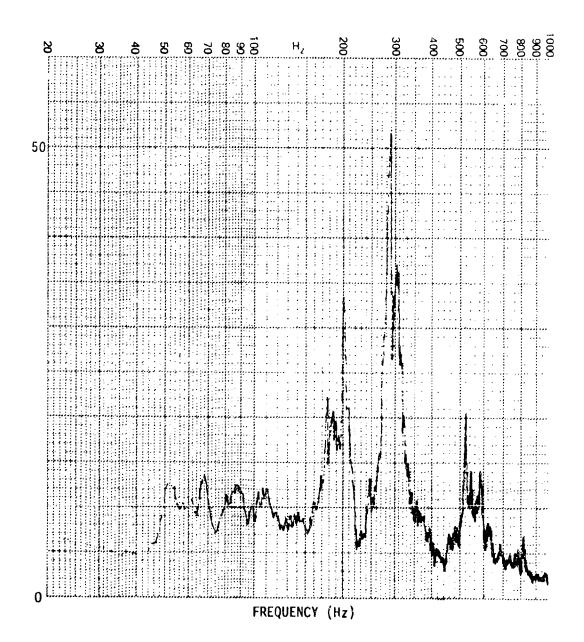


Figure C-42. Strain Spectrum for Panel h

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL: 465.5 pe RANDOM 160 dB

G10

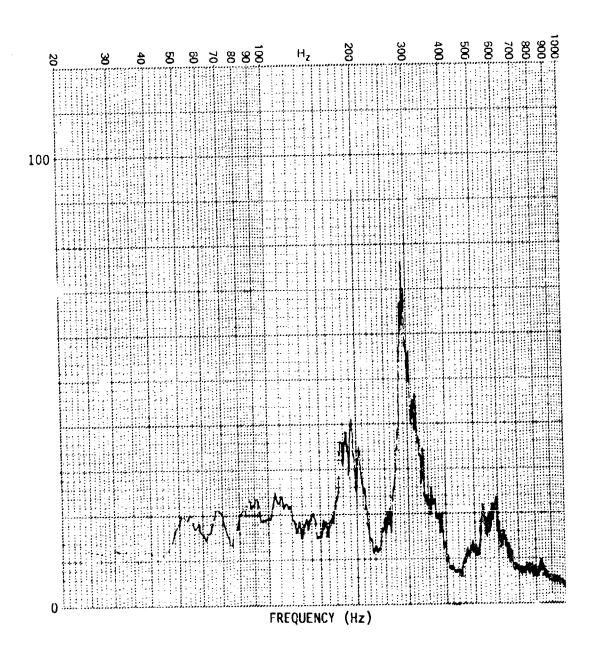


Figure C-43. Strain Spectrum for Panel h

TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

h G10 720.6 ire RANDOM

165 dB

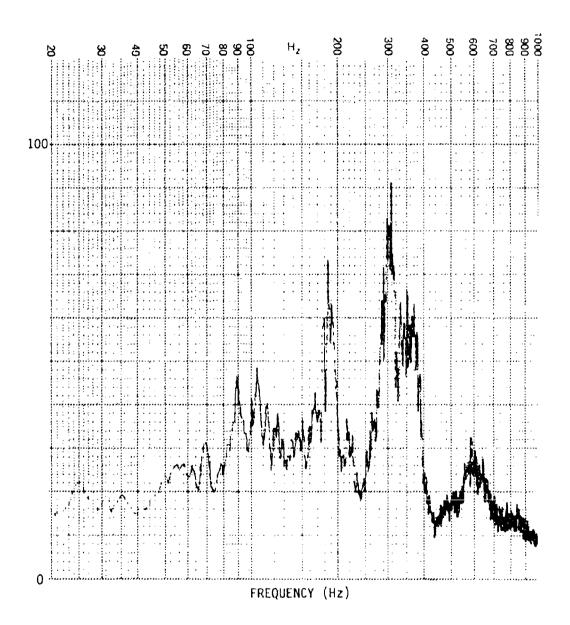


Figure C-44. Strain Spectrum for Panel h

TRANSDUCER:

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

G10

SINE 130 dB

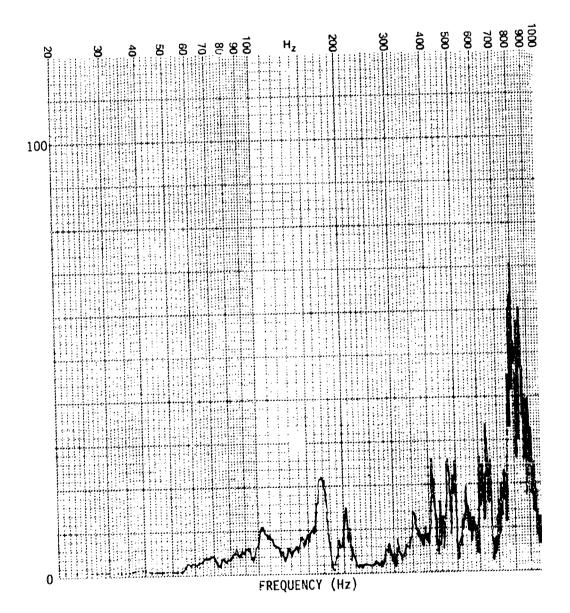


Figure C-45. Strain Spectrum for Panel i

TRANSDUCER:

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

G10 25.7µc RANDOM

140 dB

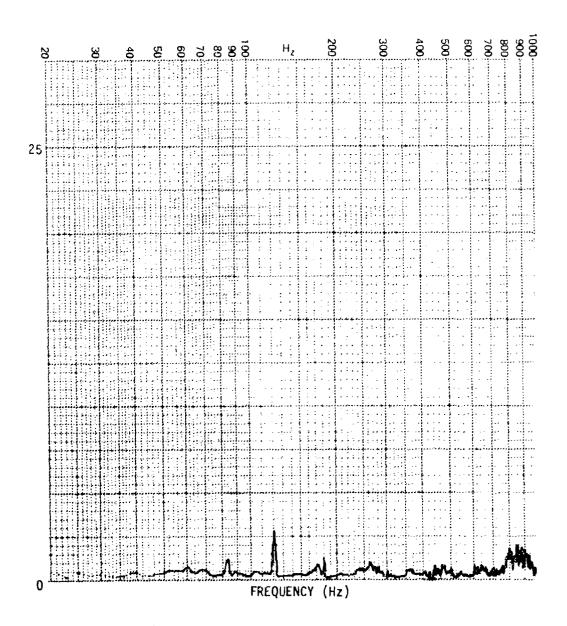


Figure C-46. Strain Spectrum for Panel i

PANEL CONFIGURATION: i
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 47.3 µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 145 dB

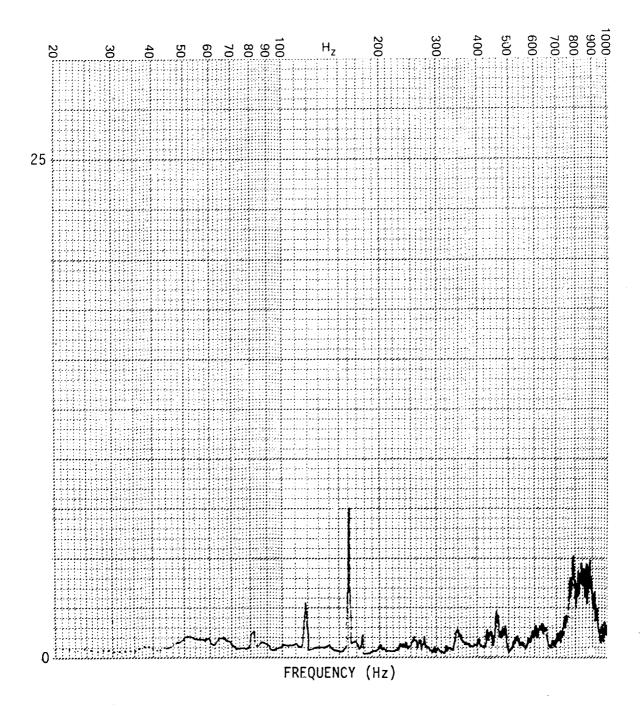


Figure C-47. Strain Spectrum for Panel i

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

84.3μe **RANDOM**

G10

INPUT LEVEL:

150 dB

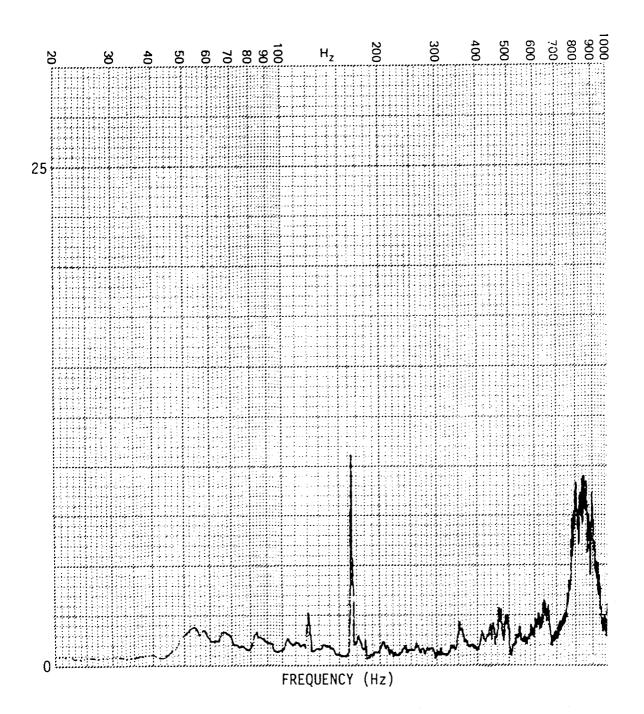


Figure C-48. Strain Spectrum for Panel i

PANEL CONFIGURATION: i
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 133.1µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 155 dB

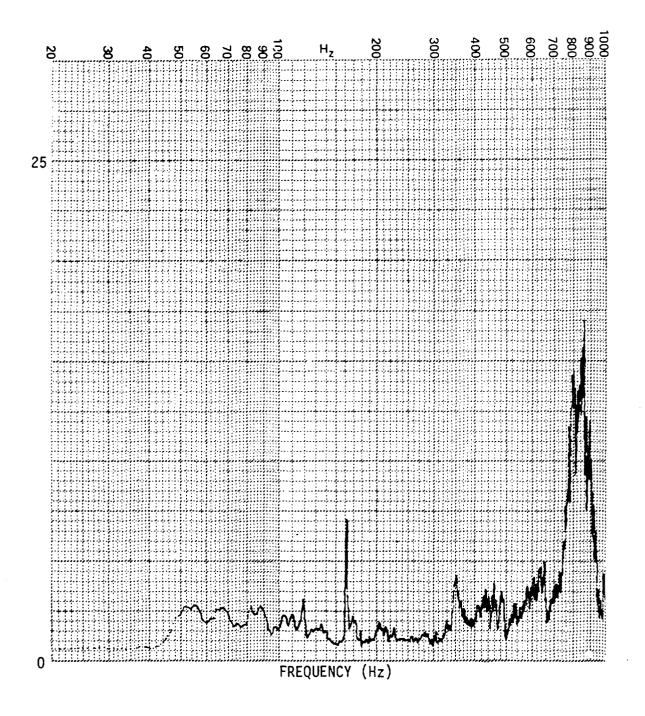


Figure C-49. Strain Spectrum for Panel i

PANEL CONFIGURATION: i
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 168.2 µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 160 dB

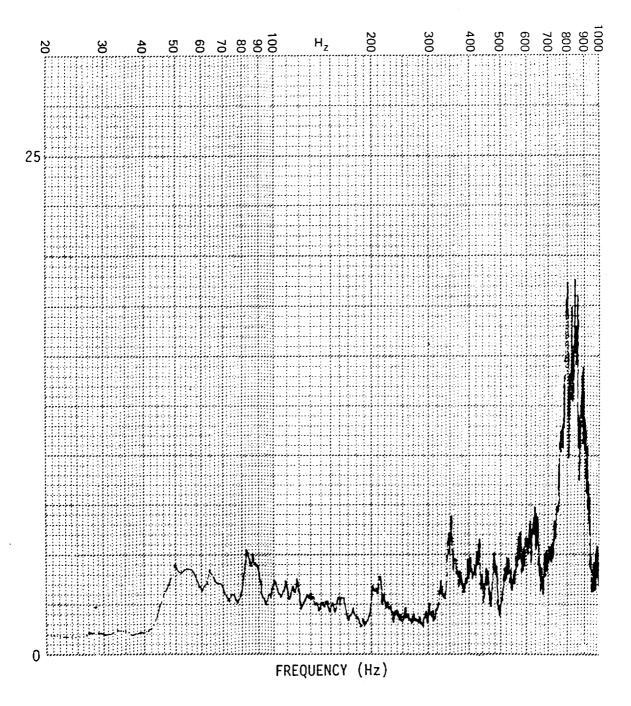


Figure C-50. Strain Spectrum for Panel i

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL:

G10 258.0 µe RANDOM 165 dB

INPUT SPECTRUM: INPUT LEVEL:

Figure C-51. Strain Spectrum for Panel i

PANEL CONFIGURATION: TRANSDUCER:

G10

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM:

SINE

:NPUT LEVEL: 130 dB

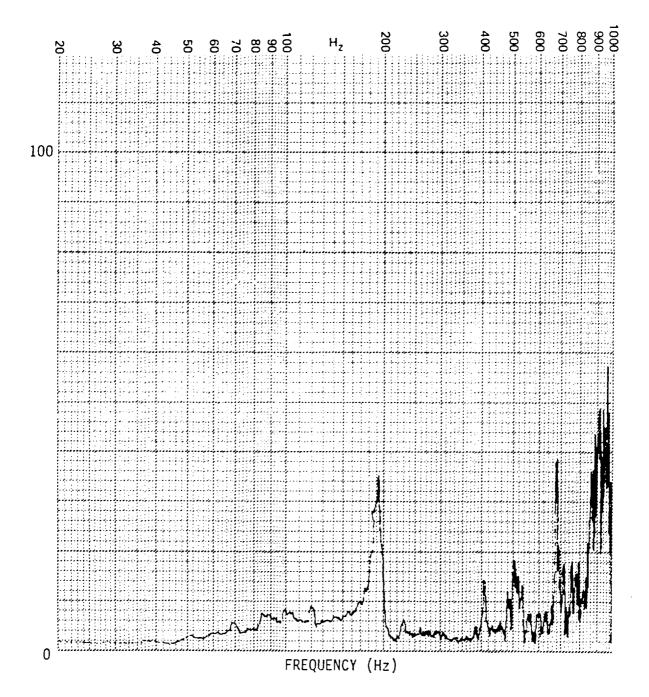


Figure C-52. Strain Spectrum for Panel j

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL: G10 41.3μe RANDOM 140 dB

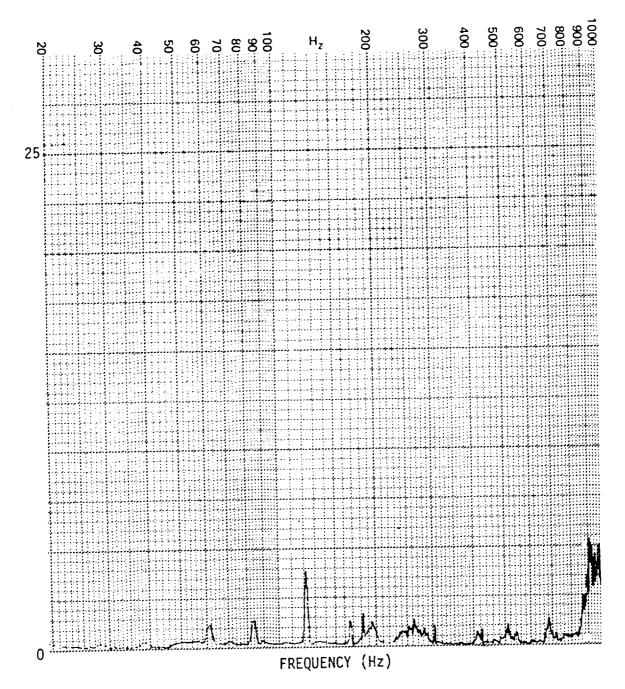


Figure C-53. Strain Spectrum for Panel j

PANEL CONFIGURATION:

TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

G10 59.0µe RANDOM 145 dB

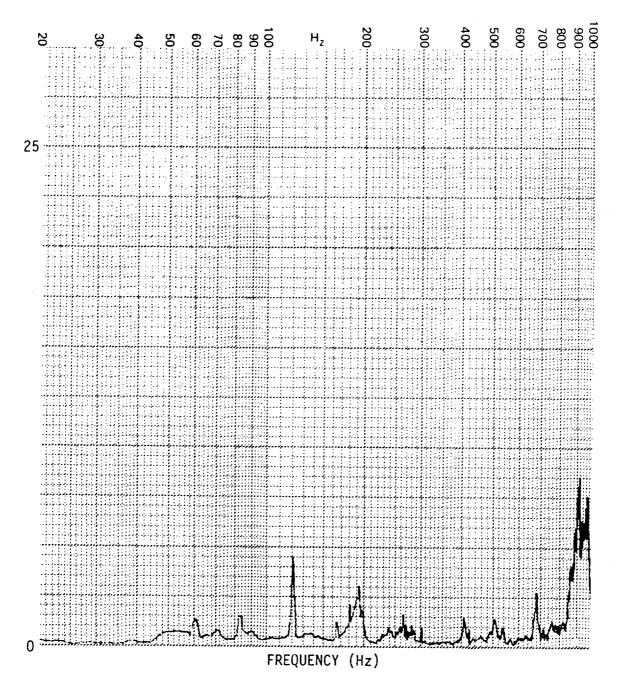


Figure C-54. Strain Spectrum for Panel j

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

G10 86.1μe RANDOM 150 dB

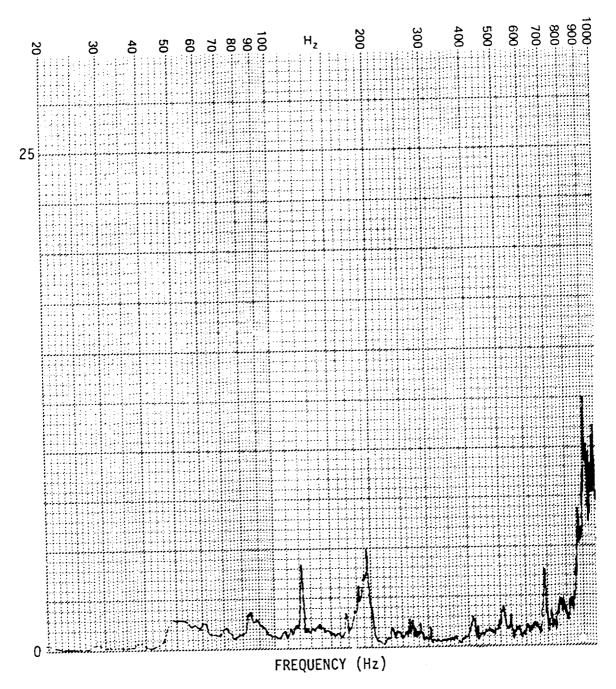


Figure C-55. Strain Spectrum for Panel j

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

137.3 RANDOM 155 dB

G10

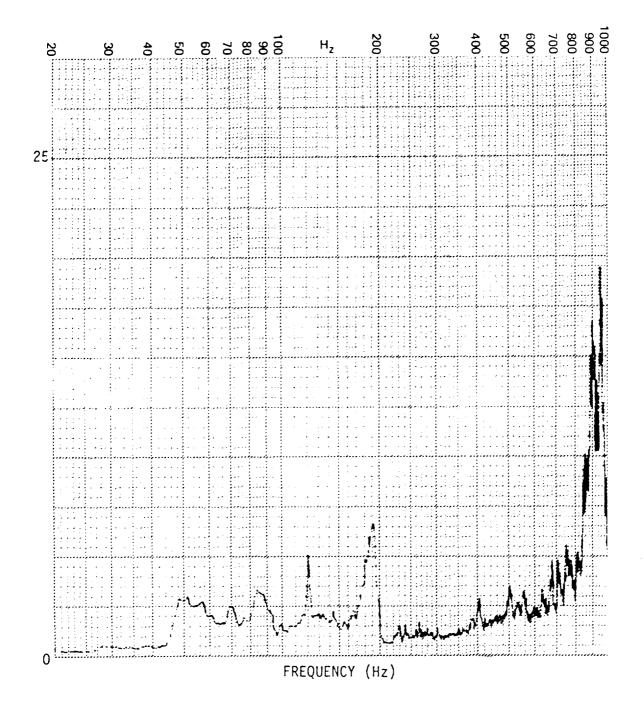


Figure C-56. Strain Spectrum for Panel j

PANEL CONFIGURATION: j TRANSDUCER: G10 OVERALL R.M.S. LEVEL: 215.8 µe INPUT SPECTRUM: RANDOM INPUT LEVEL: 160 dB

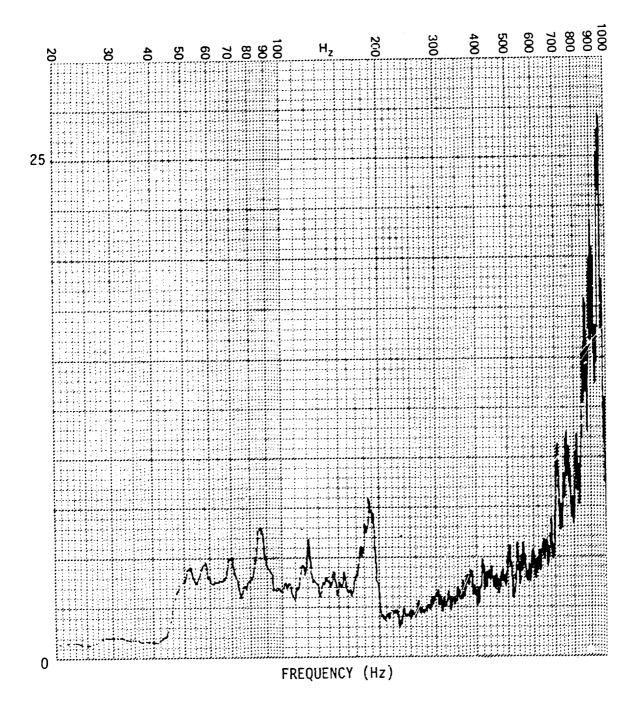


Figure C-57. Strain Spectrum for Panel j

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

j G10 311.5μe RANDOM 165 dB

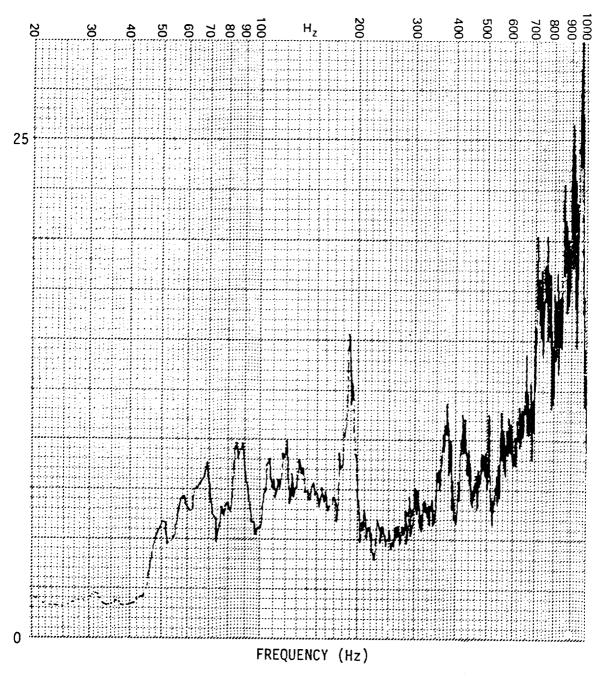


Figure C-58. Strain Spectrum for Panel j

PANEL CONFIGURATION: TRANSDUCER:

k1 G10

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM:

SINE

INPUT LEVEL:

130 dB

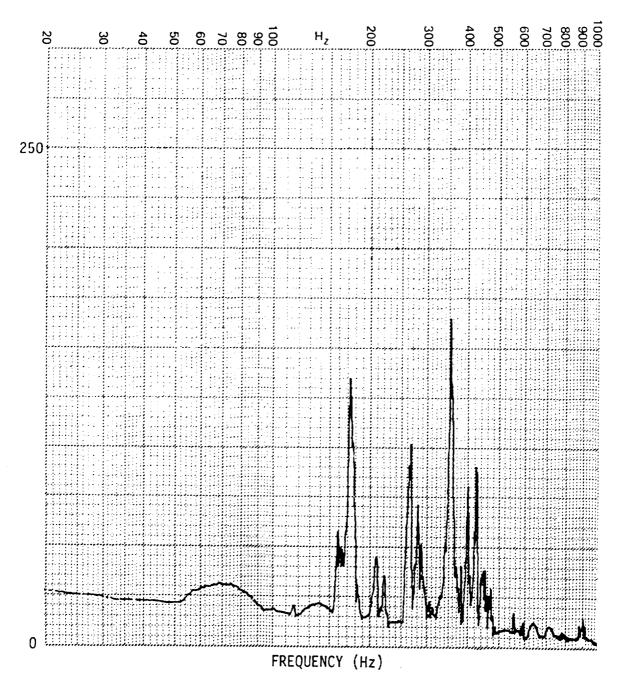


Figure C-59. Strain Spectrum for Panel k1

PANEL CONFIGURATION: k1
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 50.2µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 140 dB

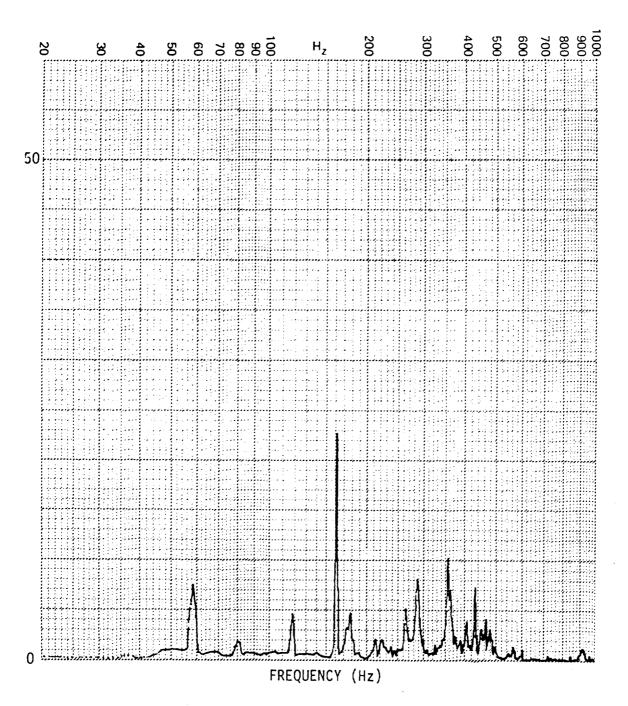


Figure C-60. Strain Spectrum for Panel kl

PANEL CONFIGURATION: k1
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 83.5μe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 145 dB

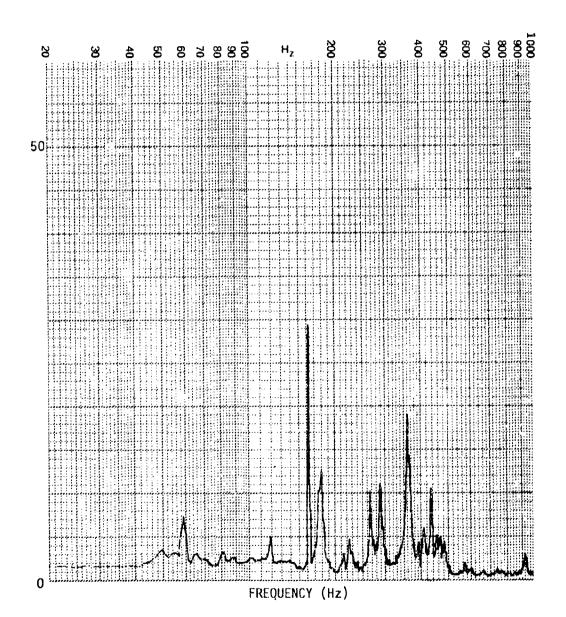


Figure C-61. Strain Spectrum for Panel k1

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

G10 142.4 μe **RANDOM**

150 dB

k1

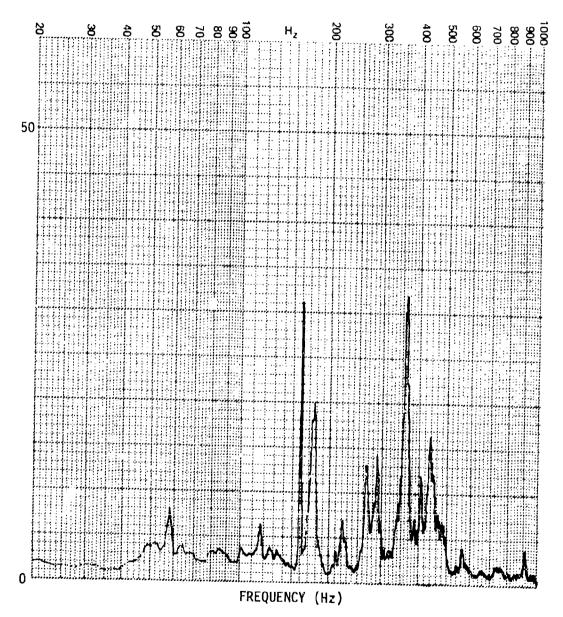


Figure C-62. Strain Spectrum for Panel kl

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

k1 G10 210.7 µe RANDOM 155 dB

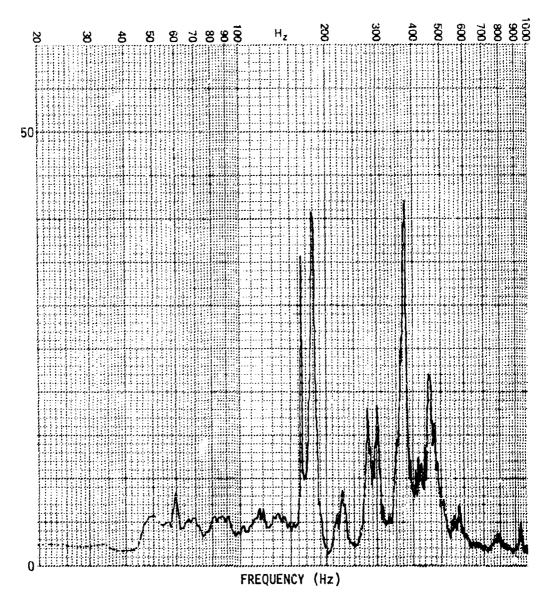


Figure C-63. Strain Spectrum for Panel k1

C-64

PANEL CONFIGURATION: k1
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 295.0µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 160 dB

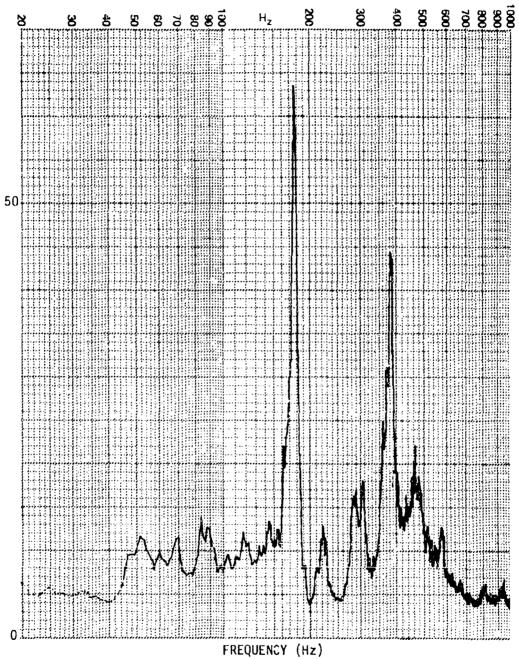


Figure C-64. Strain Spectrum for Panel k1

PANEL CONFIGURATION: 1
TRANSDUCER: G10
OVERALL R.M.S. LEVEL:
INPLIT SPECTRUM: SINE

INPUT SPECTRUM: SINE 130 dB

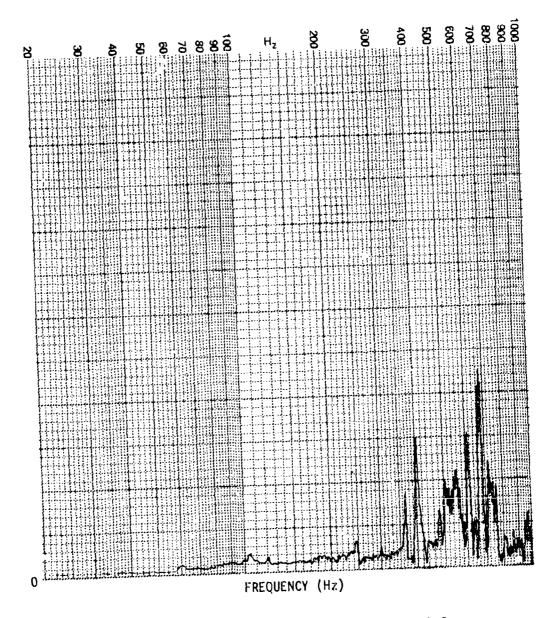


Figure C-65. Strain Spectrum for Panel 1

PANEL CONFIGURATION: I
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 28.0µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 140 dB

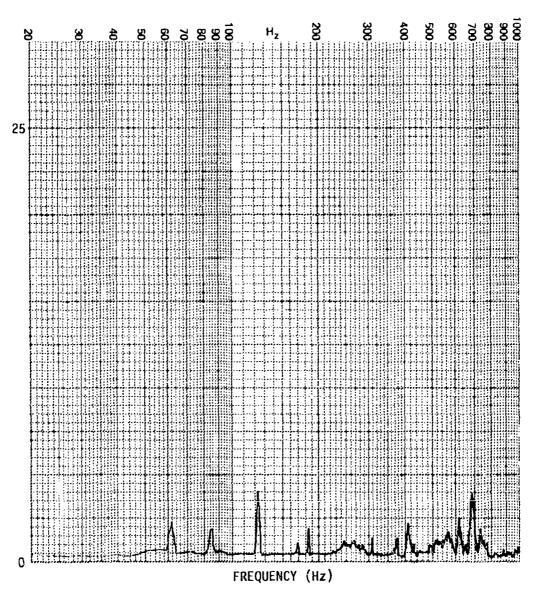


Figure C-66. Strain Spectrum for Panel 1

PANEL CONFIGURATION: TF.ANSDUCER: O'VERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

G10 43.1µe RANDOM 145 dB

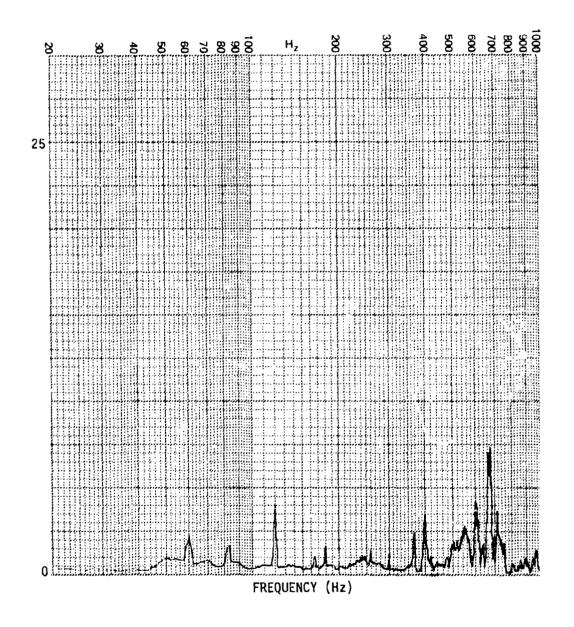


Figure C-67. Strain Spectrum for Panel 1

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL: G10 68.3µe RANDOM 150 dB

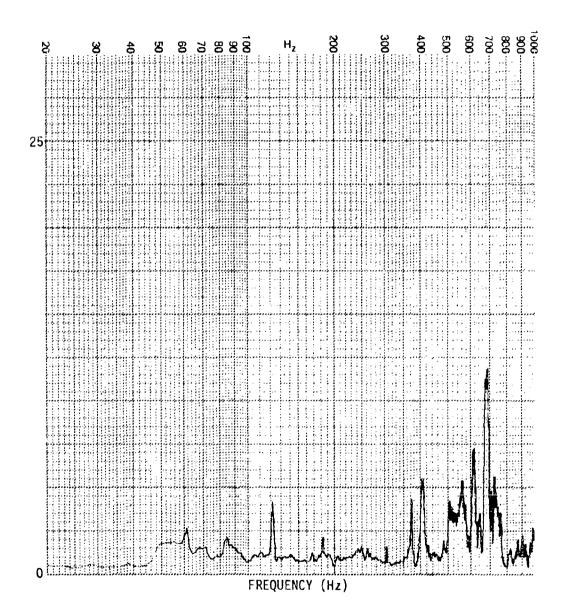


Figure C-68. Strain Spectrum for Panel 1

PANEL CONFIGURATION: I
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 108.8 μe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 155 dB

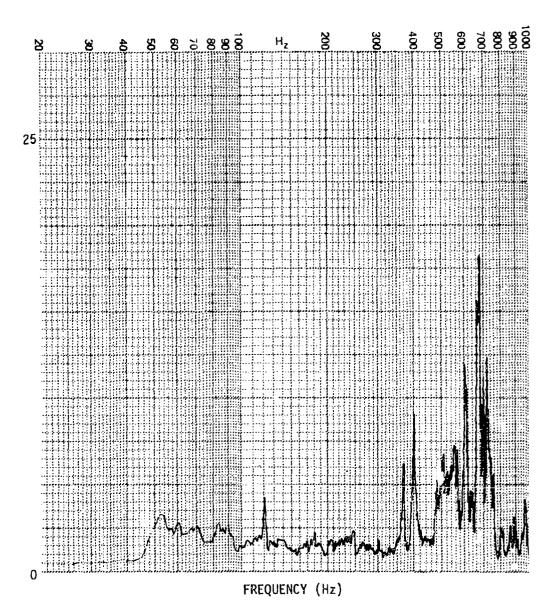


Figure C-69. Strain Spectrum for Panel 1

PANEL CONFIGURATION:

TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

. G10 179.3μe RANDOM

160 dB

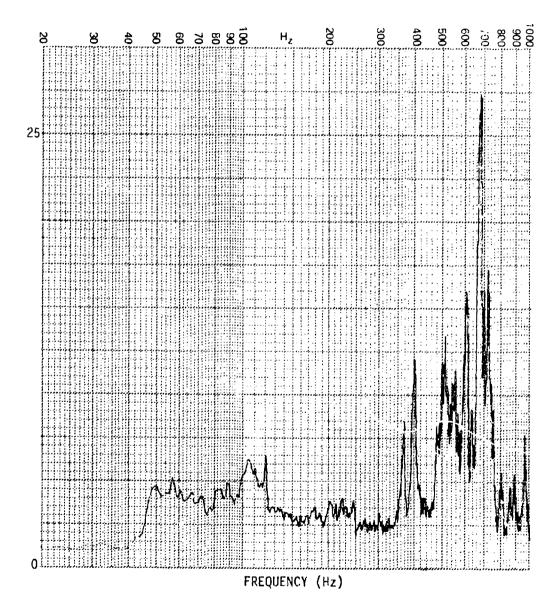


Figure C-70. Strain Spectrum for Panel 1

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

INPUT LEVEL:

G10 283.3µe RANDOM 165 dB

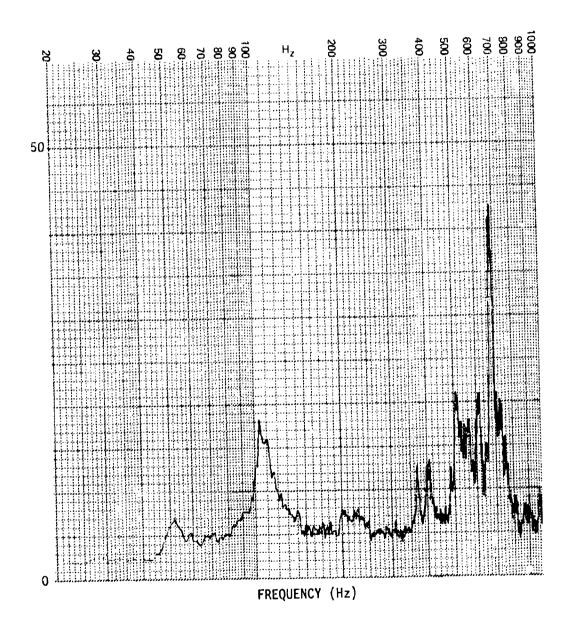


Figure C-71. Strain Spectrum for Panel 1

C-72

PANEL CONFIGURATION: n TRANSDUCER: G10 OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: SINE INPUT LEVEL: 130 dB

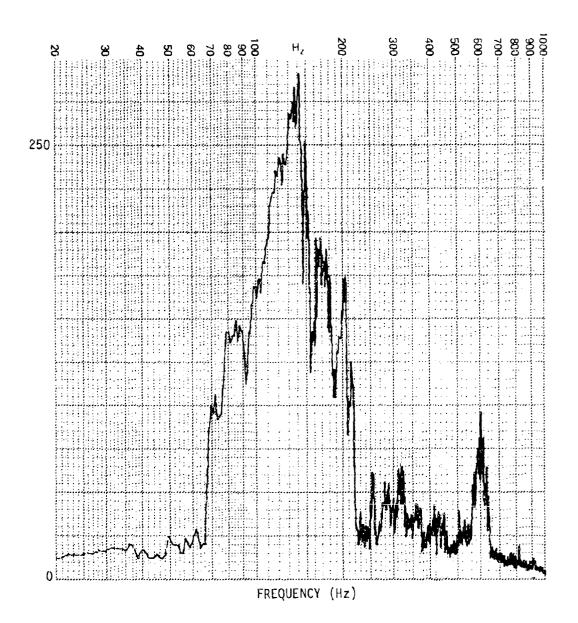
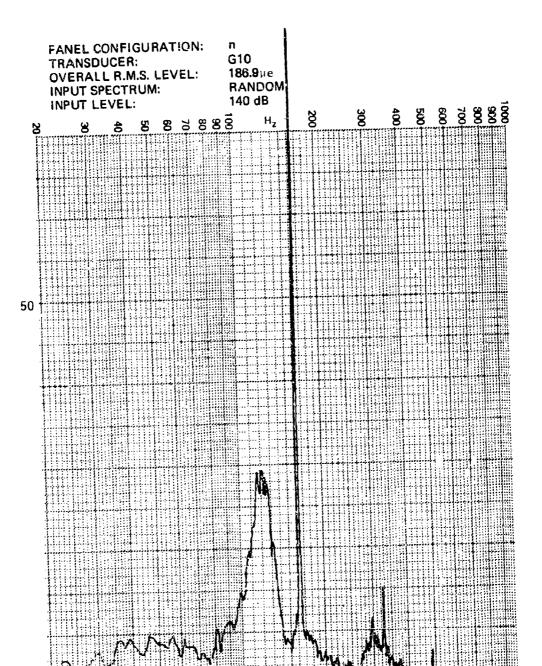


Figure C-72. Strain Spectrum for Panel n



FREQUENCY (Hz)
Figure C-73. Strain Spectrum for Panel n

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

G10 265.8µe RANDOM 145 dB

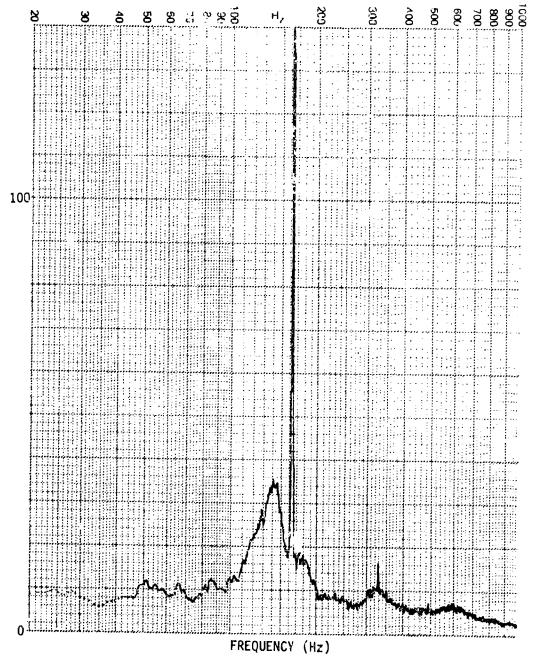


Figure C-74. Strain Spectrum for Panel n

PANEL CONFIGURATION: n
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 307.0µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 150 dB

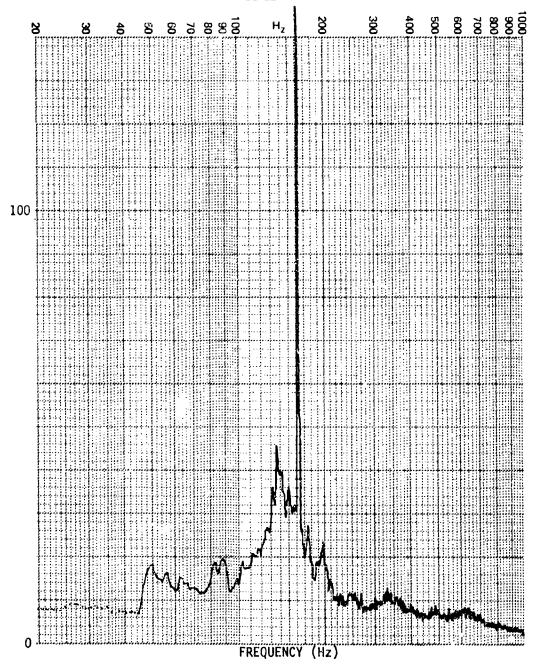


Figure C-75. Strain Spectrum for Panel n

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: !NPUT SPECTRUM:

INPUT LEVEL:

G10 355.0µe RANDOM 155 dB

n

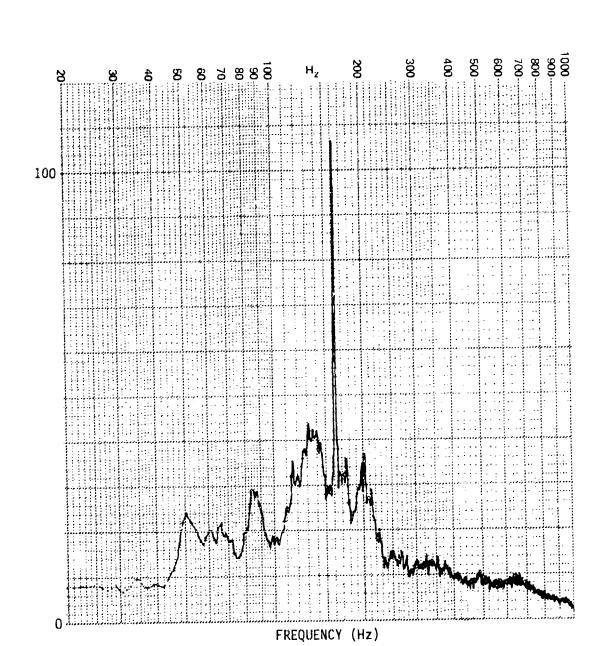


Figure C-76. Strain Spectrum for Panel n

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

G10 408.0µe RANDOM 160 dB

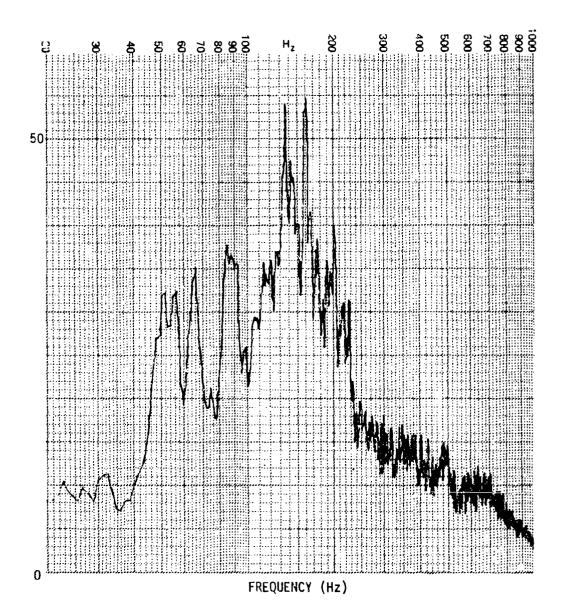


Figure C-77. Strain Spectrum for Panel n

PANEL CONFIGURATION:

TRANSDUCER:

G10

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM:

SINE

INPUT LEVEL:

130dB

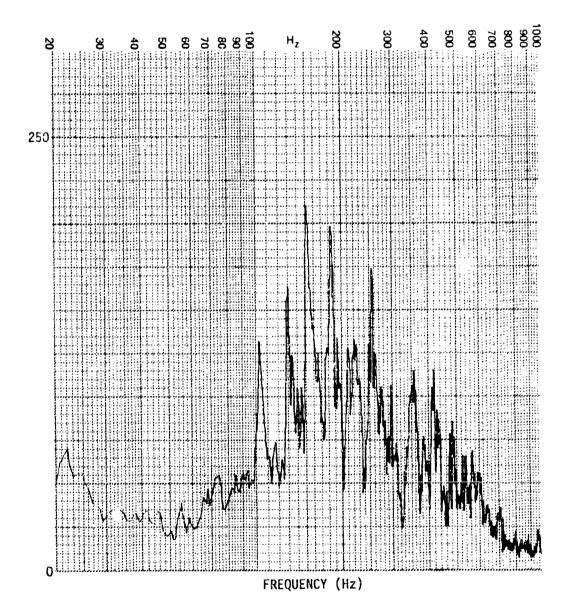


Figure C-78. Strain Spectrum for Panel p

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL: p G10μe 96.2 RANDOM

140 dB

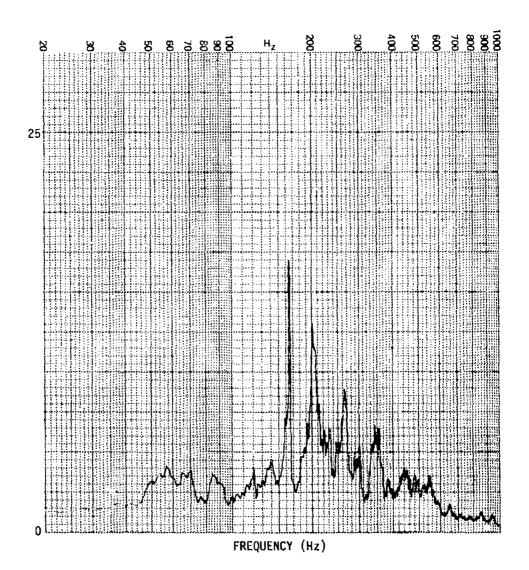


Figure C-79. Strain Spectrum for Panel p

PANEL CONFIGURATION: р G10 TRANSDUCER: **OVERALL R.M.S. LEVEL:** INPUT SPECTRUM:

115.8µe RANDOM INPUT LEVEL: 145 dB

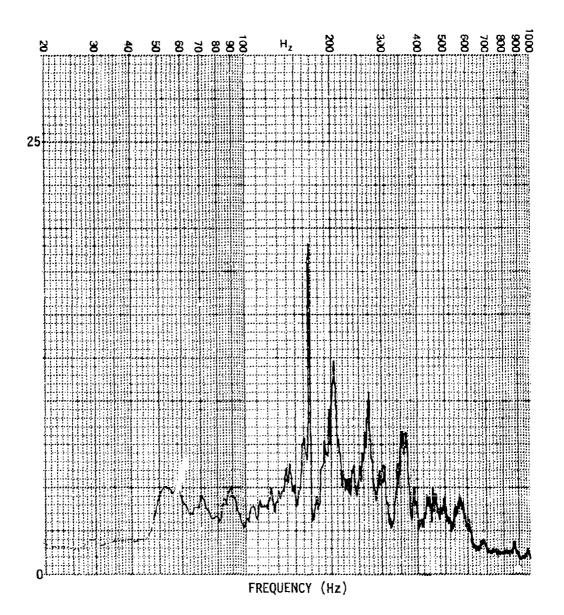


Figure C-80. Strain Spectrum for Panel p

PANEL CONFIGURATION: p
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 252.7µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 150 dB

9 1

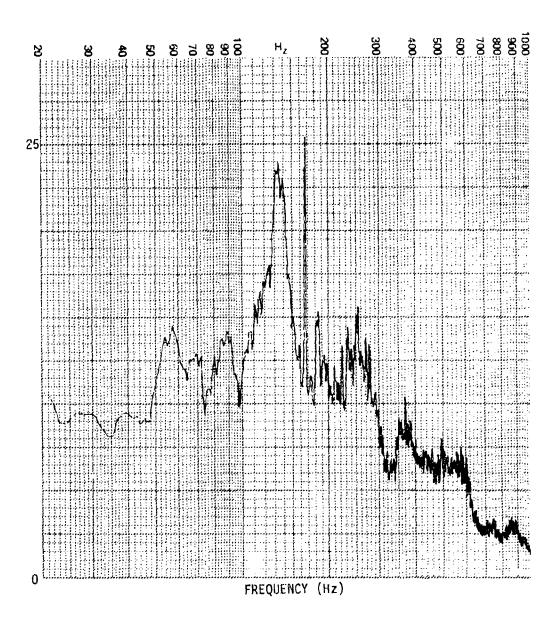


Figure C-81. Strain Spectrum for Panel p

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL: INPUT SPECTRUM: INPUT LEVEL:

p G10 455.0μe RANDOM 155 dB

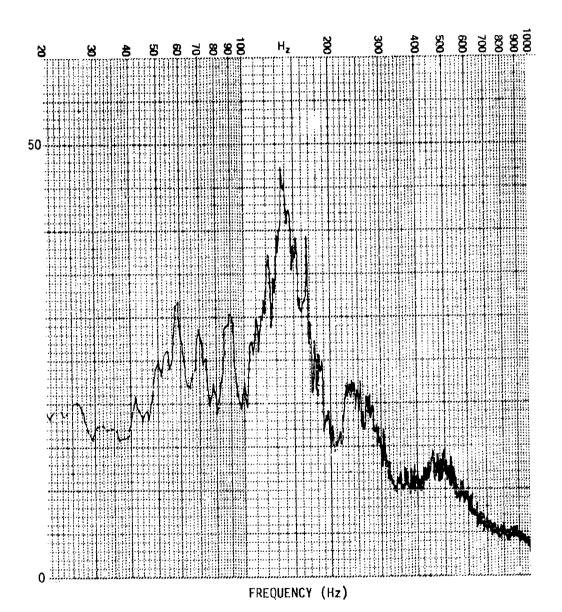


Figure C-82. Strain Spectrum for Panel p

PANEL CONFIGURATION:

TRANSDUCER:

q G10

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM:

SINE

INPUT LEVEL:

130 dB

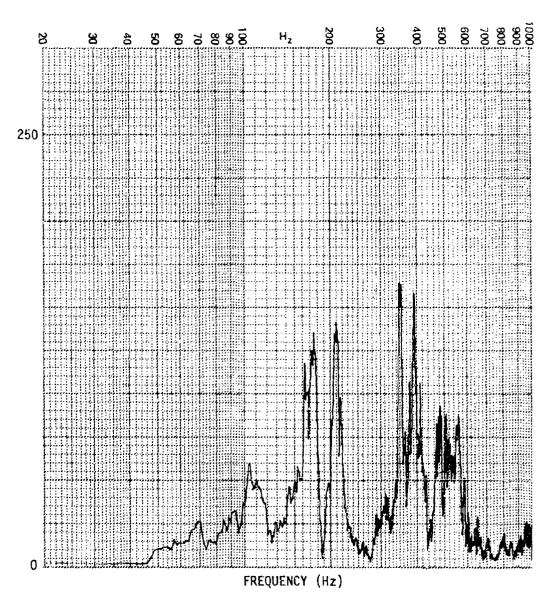


Figure C-83. Strain Spectrum for Panel ${\bf q}$

INPUT LEVEL:

G10 57.5µe RANDOM 140 dB

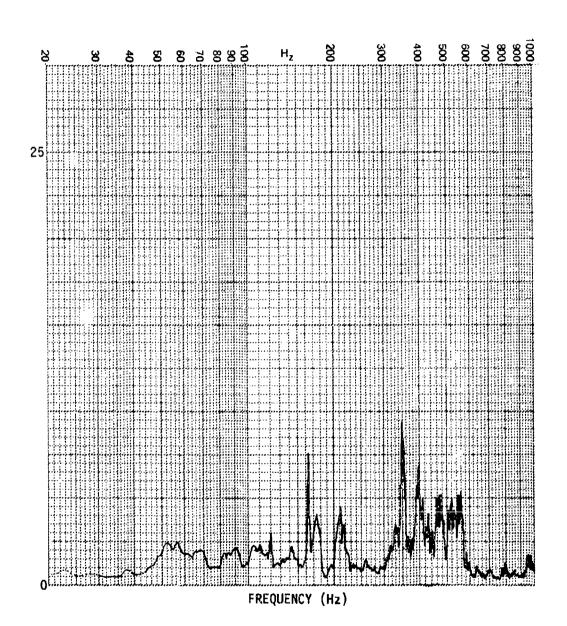


Figure C-84. Strain Spectrum for Panel q

G10 92.7µe RANDOM 145 dB

q

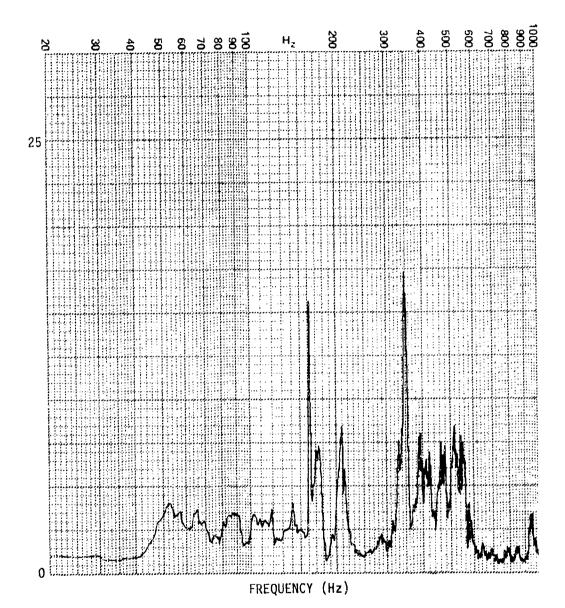


Figure C-85. Strain Spectrum for Panel q

INPUT LEVEL:

G10 141.2μe RANDOM 150 dB

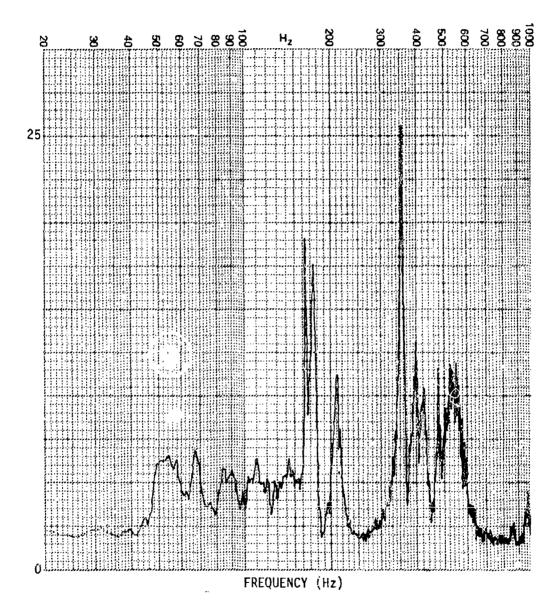


Figure C-86. Strain Spectrum for Panel q

q G10 201.5µe RANDOM 155 dB

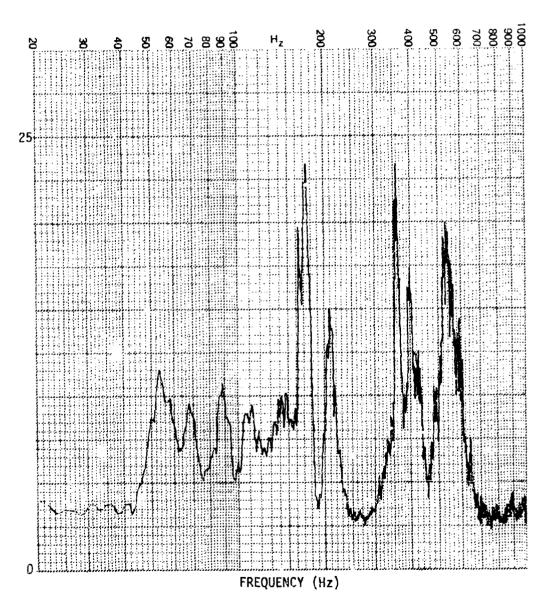


Figure C-87. Strain Spectrum for Panel q

PANEL CONFIGURATION: q
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 312.0µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 160 dB

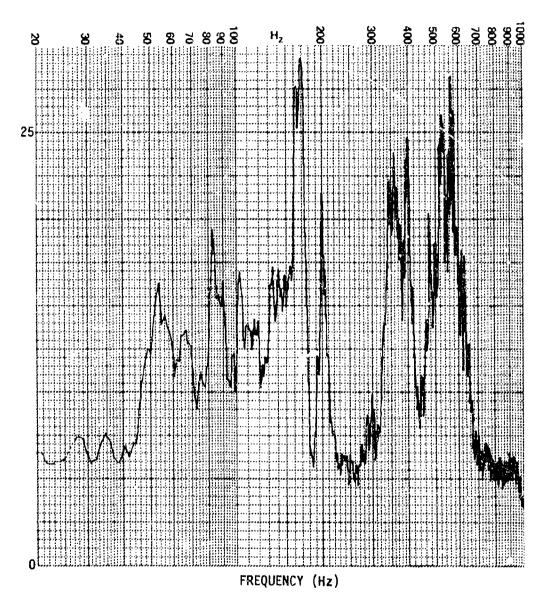


Figure C-88. Strain Spectrum for Panel q

PANEL CONFIGURATION:

TRANSDUCER:

G10

OVERALL R.M.S. LEVEL: INPUT SPECTRUM:

SINE

INPUT LEVEL:

130 dB

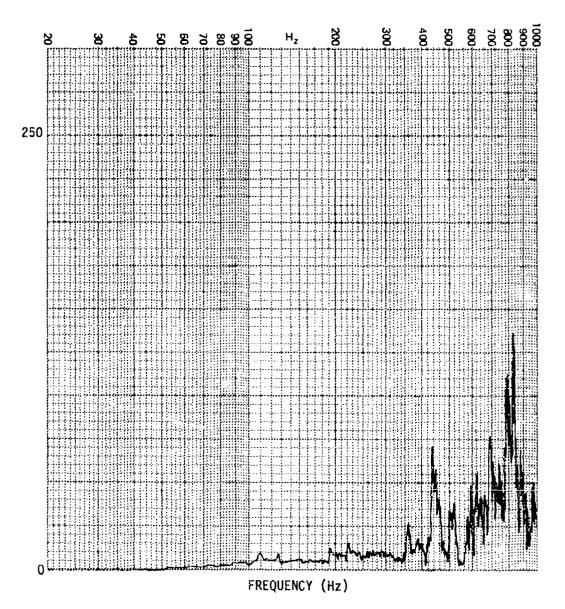


Figure C-89. Strain Spectrum for Panel r

INPUT LEVEL:

G10 43 8μe RANDOM 140 αΒ

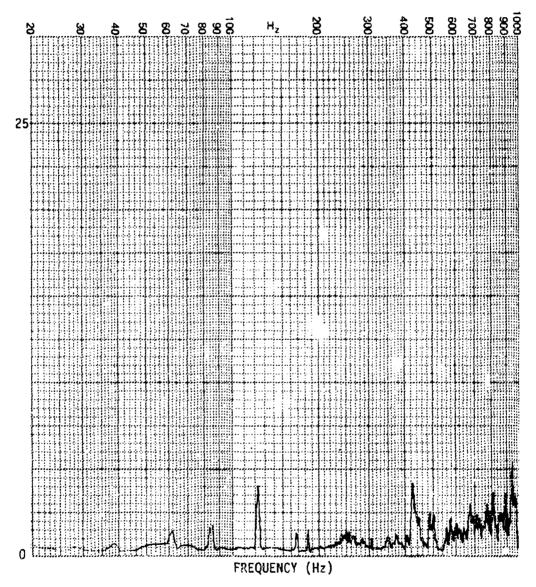


Figure C-90. Strain Spectrum for Panel r

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: INPUT LEVEL:

r G10 61.7µe RANDOM

RANDON 145 dB

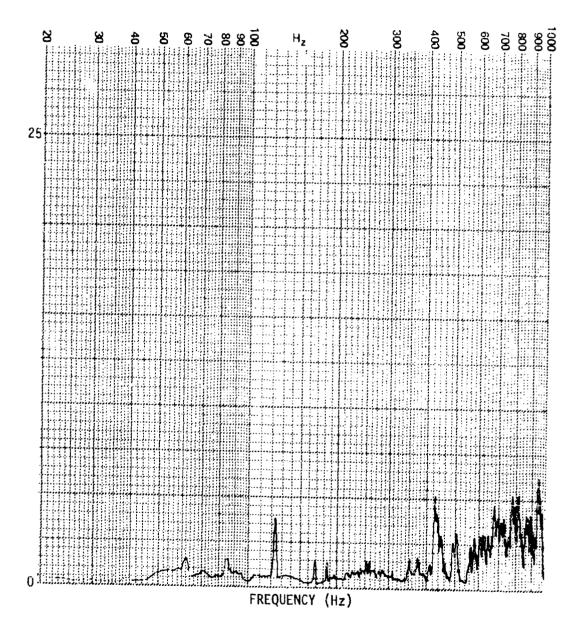


Figure C-91. Strain Spectrum for Panel r

G10 107.9µe RANDOM 150 d6

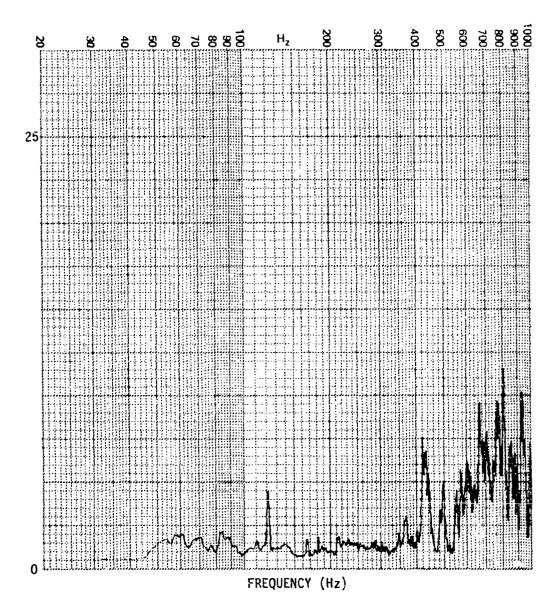


Figure C-92. Strain Spectrum for Panel r

PANEL CONFIGURATION: r
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 159.8 µe
INPUT SPECTRUM: RANDOM
INPUT LEVEL: 155 dB

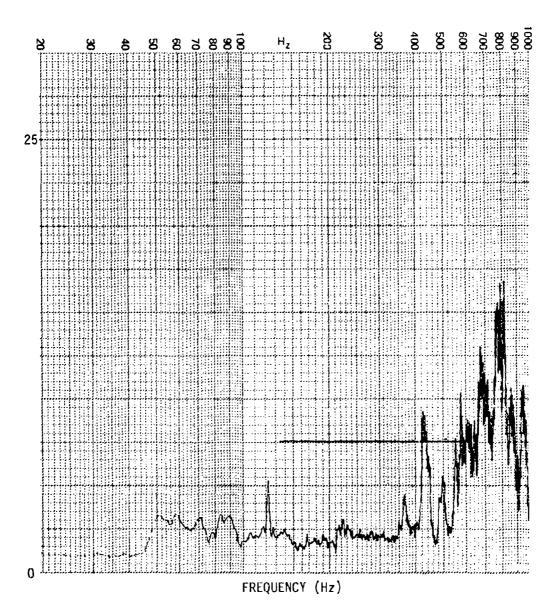


Figure C-93. Strain Spectrum for Panel r

r G10 265.4 μe RANDOM 160 dB

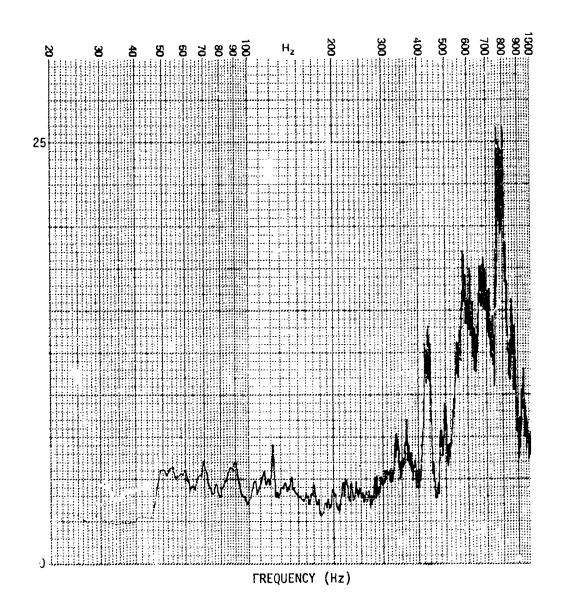


Figure C-94. Strain Spectrum for Panel r

r G10 445.6µe RANDOM 165 dB

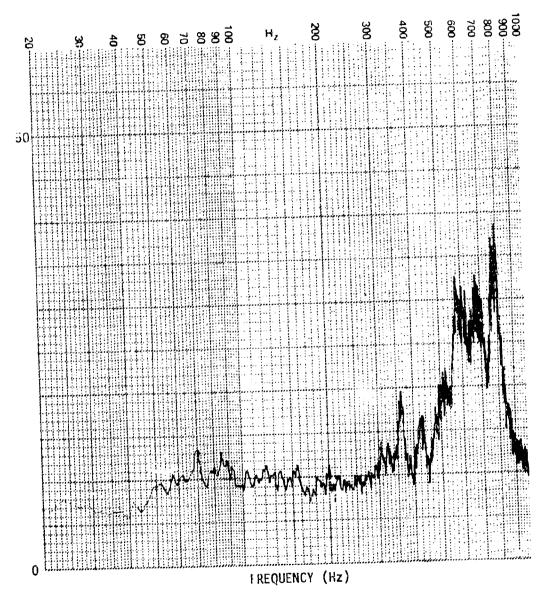


Figure C-95. Strain Spectrum for Panel r

PANEL CONFIGURATION: TRANSDUCER:

OVERALL R.M.S. LEVEL:

INPUT SPECTRUM: SINE INPUT LEVEL: 130 dB

G10

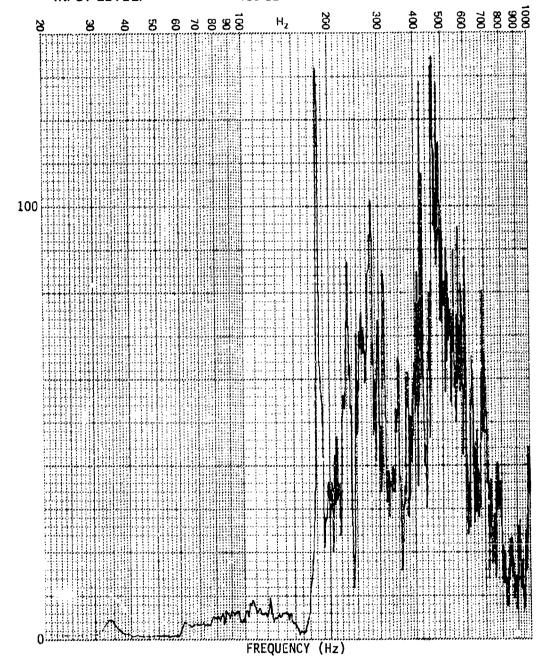


Figure C-96. Strain Spectrum for Panel s

PANEL CONFIGURATION: TRANSDUCER: OVERALL R.M.S. LEVEL:

G10 47.7µe RANDOM 140 dB

OVERALL R.M.S. LEVEL: 47.79
INPUT SPECTRUM: RAN
INPUT LEVEL: 140

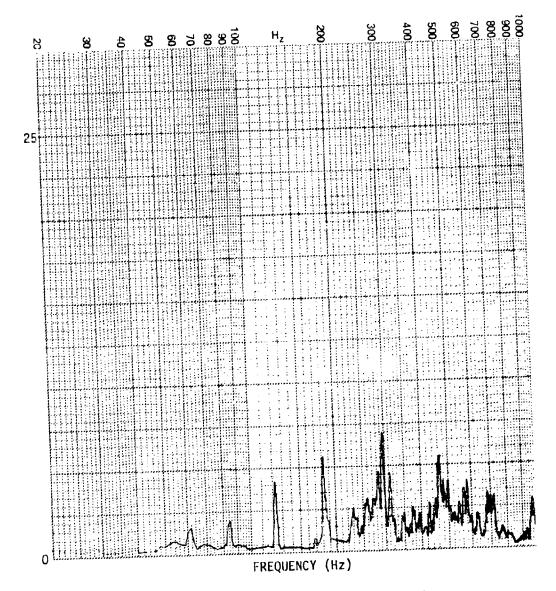


Figure C-97. Strain Spectrum for Panel s

INPUT LEVEL:

G10 90.7µe RANDOM 145 dB

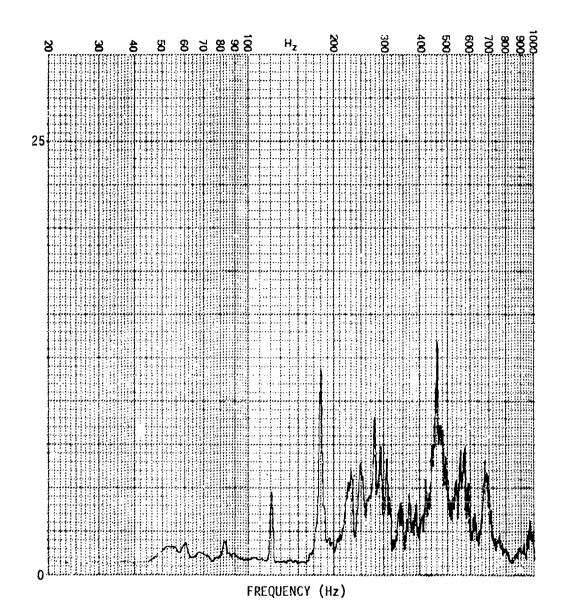


Figure C-98. Strain Spectrum for Panel s

G10 149.0µe RANDOM 150 dB

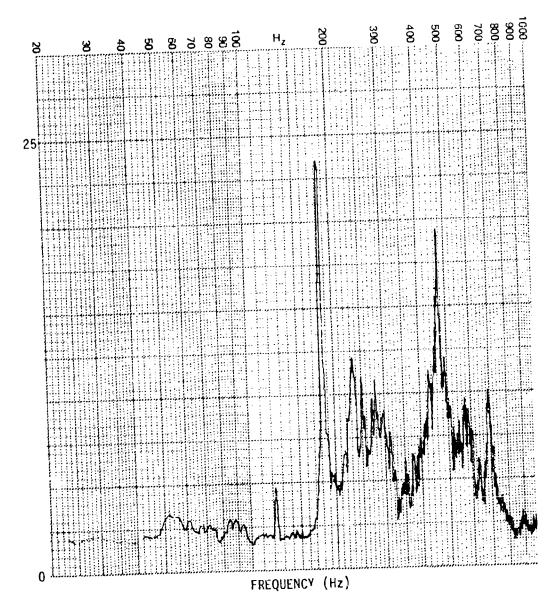


Figure C-99. Strain Spectrum for Panel s

PANEL CONFIGURATION: s
TRANSDUCER: G10
OVERALL R.M.S. LEVEL: 261.8 He
INPUT SPECTRUM: RANDOM

INPUT LEVEL: 155 dB

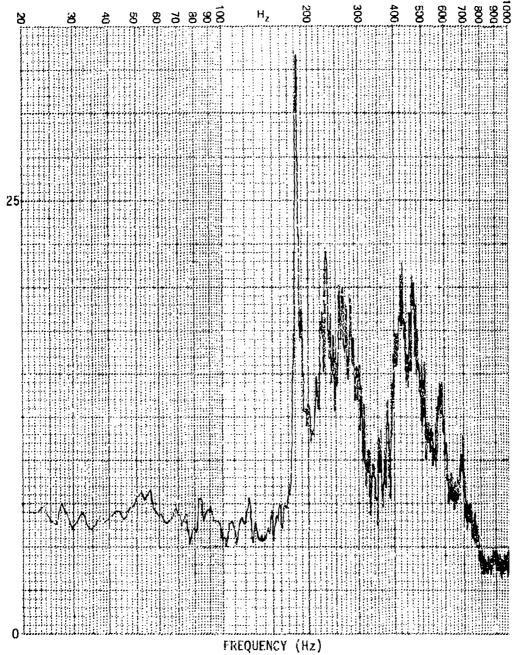


Figure C-100. Strain Spectrum for Panel's

G10 444.4μe RANDOM 160 dB

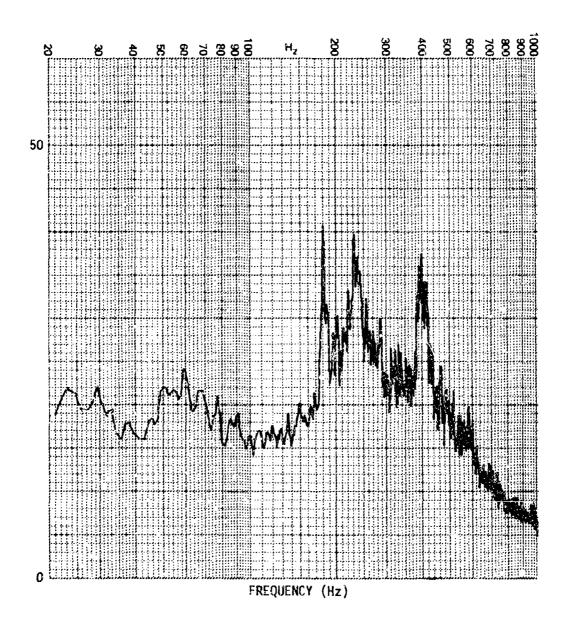


Figure C-101. Strain Spectrum for Panel

C-102

±U.S.Government Printing Office: 1980 -- 697-084/57



SUPPLEMENTARY

INFORMATION

ERRATA - March 1989

The following corrections are applicable to AFWAL-TR-80-3019, <u>Sonic Fatigue Design Techniques for Advanced Composite Aircraft Structures</u>.

Delete pages 177 through 186 (paragraphs 5 and 6) and substitute the attached pages 177 through 188.

FLIGHT DYNAMICS LABORATORY
AIR FORCE WRIGHT AERONAUTICAL LABORATORIES
_AIR FORCE SYSTEMS COMMAND
WRIGHT-PATTERSON AIR FORCE BASE, OHIO 45433-6553

DESIGN METHOD

This section contains a semiempirical design method for estimating rms strains and natural frequencies for curves and flat cfrp stiffened-skin panels, subjected to random acoustic loading. The method comprises an equation relating rms strain to panel configuration parameters and overall sound pressure levels, a procedure for estimating the natural frequencies of the fundamental fully-fixed panel mode, and a random fatigue curve for estimating sonic fatigue life.

The method can be directly applied to Z and J section stiffeners and is valid for quasi-isotropic and most orthotropic skin laminates typically used for airplane skin panels. Because the response equation uses overall sound pressure level as the applied load, a technique for utilizing fan noise spectra from high bypass ratio jet engines is also included. A worked example is presented at the end of the section.

Range of Application

The use of regression analysis techniques in developing the strain response equation limits its application to within the following range of panel configuration parameters:

Stiffener spacing: 4 to 8 inches (102 to 204 mm)

Skin laminate thickness: 0.033 to 0.066 inch (0.8 to 1.8 mm)

Stringer laminate thickness: 0.04 to 0.08 inch (1.0 to 1.0 mm)

(1.2 times the skin thickness)

Radius of curvature: flat down to 30 inches (760 mm)

Aspect ratio: 1 to 3 (assumed valid for all values above unity)

Within this parameter envelope, the estimated strains showed an average deviation of 9 percent from measured values. A progressive deterioratio of this accuracy can be expected for panel configurations outside the given range. The 90 percent confidence interval for estimated rms strains approximates a ± 22 percent variation in accuracy.

CFRP Skin Laminates -- Quasi-isotropic and orthotropic laminates were used in the development of the strain response equation and the fatigue curve. Moderate variations in skin ply orientation and stacking order do not have a significant effect on the accuracy of this design method.

The following table gives the ply orientation and elastic modulus values for the skin laminates used in this programme:

Table 40. Skin Laminate Ply Orientations and Elastic Modulus Values Laminate density c = 0.055 lb/in ³ (1,522 Kg/m ³)				
PLY ORIENTATION O° - Transverse to Stringers 90° - Parallel to Stringers	<u>Elastic Modulus</u>			
	(E _v) Transverse to stringers: b + direction		(E_) Parallèl to stringers: a - direction	
	10 ⁶ 1b/in ²	MN/m ²	10 ⁶ 1b/in ²	MN/m ²
(0, ±45) ₅	7.5	51,711	3.3	22,753
(0, ±45, 90) _s	6.7	46,195	6.7	46,195
(0 ₂ , ±45) _s	9.7	66,879	3.2	22,063
(0, ±45) _{2s}	7.5	51,711	3.3	22,753
(0, 90) _s	9.4	64,811	9.4	64,811

Stiffener Design and Method of Attachment -- The response equation is based on data from skins reinforced with z section stiffeners, adhesively bonded to the skins. However, the equation can be applied to J-stiffened panels by multiplying calculated strains by 0.75. This factor could also be applied to hat section stiffeners.

RMS strain levels are not significantly affected by the method of skin-stiffener attachment. Consequently, secondary bonding, co-curing, integral skin-stiffener layup and riveted attachments can be analyzed. The fatigue curve, however, which is based on secondarily bonded stiffeners, may not be valid for the other methods of attachment.

Stiffener cross-section properties should provide for effective panel edge restraint. The upstanding webs of stringers should be attached to intersecting frames in order to provide continuity of stiffness and to prevent the stringers from rotating.

Structural Damping -- The effects of damping have been absorbed into the empirical factors in the strain response equation. The equation is valid for damping ratios in the 0.017 to 0.03 range. The average measured value was 0.025. This range of values may be considered typical for this class of structure. If special damping factors need to be considered, such as the use of damping treatments, highly damped resin systems, discontinuous carbon fibres, etc., then the estimated rms strain should be appropriately factored down. In the absence of alternative relevant data, multiply rms strain by the square root of the ratio (0.025/Actual Damping Ratio).

Nonlinear Response Effects -- Nonlinear response effects have been taken into account to a limited extent, by deriving a lower rate of change in rms strains, with respect to overall sound pressure levels, than is associated with linear response behaviour. These effects have been averaged over the data base and do not take into account individual variations in the degree of nonlinear response characteristics. The degree of nonlinear response approximates to a 7-dB increase in sound pressure level resulting in a doubling of rms strain. Linear behaviour results in a doubling of rms strain for a 6-dB increase in sound pressure level.

<u>Units of Measurement</u> -- The equation for estimating rms strain uses panel width, panel length and skin laminate thickness in non-dimensional form. Consequently, any coherent system of units may be used to estimate rms strains for flat panels. The radius of curvature (R) is expressed in inches, with an alternate expression provided for R in millimetres.

Notation

The following notation is used in this section:

- $\epsilon_{\rm rms}$ RMS strain x 10⁶, located at the centre of, and normal to, the longer side of the skin panel
 - a length of longer side of panel (frame or longeron spacing)
 - b length (arc length) of shorter side of panel (stringer spacing)
 - t skin laminate thickness
 - R Radius of curvature in the b-direction (inches or mm)
- SPL Overall sound pressure level (dB)
 - Youngs modulus for the skin laminate material in the direction of the shorter side of the panel (lb/in² or N/m²). For laminates used in this programme, obtain values from Table 40.
- p density of skin laminate material: $(lb/in^3) \div 386.4$ or kg/m^3 .
- f fundamental natural frequency of skin panel assuming all edges to be fixed. (Hz)

v - velocity parameter for the skin laminate material. Equals $(E_y/\rho)^{1/2} \div 200,000$ when E_y and ρ are expressed in 1b and in, and $(E_y/\rho)^{1/2} \div 5,080$ when E_y and ρ are expressed in Kg and m.

Calculation of rms Strain
Equation 25 is used to estimate rms strain:

$$\varepsilon_{\text{rms}} = \left(\frac{b}{t}\right)^{4/3} \left[4 \text{ Tanh (a/b)} - 1\right] 10^{\left(\frac{\text{SPL} - 178}{24}\right)}$$

$$\text{Tanh}\left(\frac{R - 17}{40}\right) \quad (25)$$

where R is in inches.

When R is in metres, the equation is written:

$$\frac{\epsilon_{\text{rms}} = \left(\frac{b}{t}\right)^{4/3} \left[4 \text{ Tanh (a/b)} - 1\right] 10^{\left(\frac{\text{SPL} - 178}{24}\right)} \text{ Tanh } \left(\frac{R}{10^3} - 0.43\right)}{(25a)}$$

For large radii of curvature, (i.e., R greater than 150 inches or greater than 4,000 mm) the hyperbolic tangent of the radius function is unity, and the equation reduces to the flat panel response equation.

No particular physical significance is attached to the number (178) that is subtracted from the sound pressure level in the exponent of 10, and the equation is valid for both positive and negative exponents.

- NOTE 1: The equations were derived for Z stiffeners. For J stiffeners multiply ϵ_{rms} by 0.75.
- NOTE 2: The equations are valid for typical damping ratios over the range 0.017 to 0.03. For significantly different damping ratio values multiply $\epsilon_{\rm rms}$ by the square root of the ratio (0.025/actual damping ratio).
- NOTE 3: If a 90% level of confidence is required, then increase the estimated rms strain by 22%.

Calculation of Natural Frequency

$$f = VK \frac{t}{b^2}$$
 (26)

where V is defined under Notation and K is obtained from Figure 64 for given a/b, b, t and R (expressed in the form b^2 / Rt). Figure 64 is expressed in both British and S.I. units.

Estimation of Sonic Fatigue Life

The estimated sonic fatigue life is obtained by reading the number of cycles to failure (N) from Figure 65, corresponding to the estimated rms strain (ε_{rms}). The number of cycles to failure is converted to life in hours by the relationship ($\frac{N}{3,600f}$), where f is the natural frequency calculated using Equation 26.

Worked Example

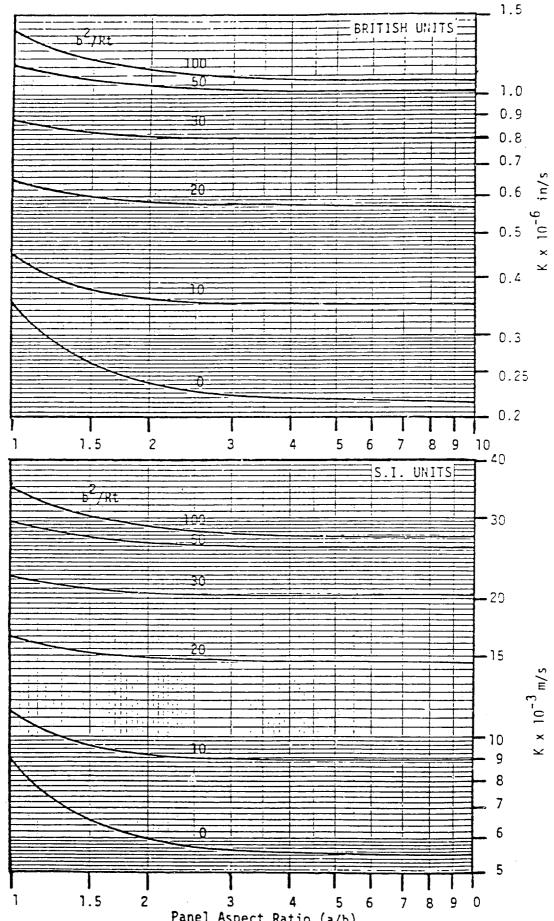
A six-ply skin laminate having a ply orientation of $(0, \pm 45)_s$ and a thickness of 0.033 inch, has an 8-inch stringer spacing, with a panel length of 12 inches and a radius of curvature of 90 inches. The overall sound pressure level is 160 dB.

(i) For a = 12 in, b = 8 in, t = 0.033 in, R = 90 in and SPL = 160, equation 25 gives

$$\epsilon_{\text{rms}} = \left(\frac{8}{0.033}\right)^{4/3} \left[4 \text{ Tanh } \frac{12}{8} -1\right] \cdot 10^{\left(\frac{160-178}{24}\right)} \text{Tanh}\left(\frac{90-17}{40}\right)$$

$$= (1,512)(2.62)(0.178)(0.949)$$

$$= 669 \text{ micro-strain}$$



Panel Aspect Ratio (a/b)
Figure 64. Natural Frequency Nomograph for Panel With Fixed Edges

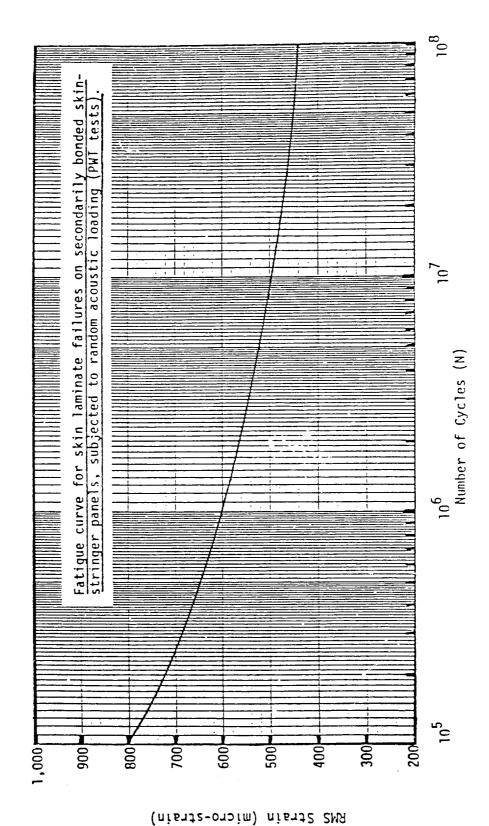


Figure 65. Random Fatigue Curve for CFRP Stiffened-Skin Panels-RMS Strain vs Cycles to Failure

(ii) Natural frequency is estimated from equation 26:

$$f = VK \frac{t}{b^2}$$

where
$$V = \frac{(E_y/\rho)}{200,000}$$
 1/2

From Table 40: $E_y = 7.5 \times 10^6 \text{ lb/in}$

$$p = \frac{0.055}{386.4}$$

$$v = 1.148$$

From Figure 64:

For
$$\frac{b^2}{Rt} = \frac{8^2}{90(0.033)} = 21.5$$

and a/b = 12/8 = 1.5, then

$$K \times 10^{-6} = 0.6$$

$$\therefore k = 0.6 \times 10^6$$

$$f = (1.148)(0.6 \times 10^6) \frac{(0.033)}{8^2}$$
$$= 355 \text{ Hz}$$

(iii) From Figure 65:

Number of cycles to failure for ε_{rms} = 669 is

$$N = 3.5 \times 10^6$$
 cycles

For a frequency of 355 Hz, the estimated sonic fatigue life is

$$\frac{3.5 \times 10^6}{(3,600)(355)}$$
= 2.74 hours

Fan Noise from High Bypass Ratio Jet Engines

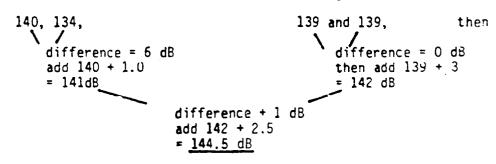
The design method presented here utilizes the overall sound pressure level as the design load. While this is adequate for the broad band spectra that typify jet exhaust noise, it does not automatically lend itself to designing for the inlet and fan exit acoustic spectra the occur due to fan noise on high bypass ratio engines. These spectra ofte have overall sound pressure levels that are dominated by high acoustic spectrum levels occurring at the fan blade passage frequency and its next harmonic (typically in the frequency range of 2 to 2.5 KHz and 4 to 5 KHz respectively). These frequencies are above the usual frequency range of panel resonant response. This, including their corresponding acoustic spectrum peaks in the overall sound pressure leve to be used for design purposes, may result in overly conservative design. To deal with this type of acoustic load, the applied overall sound pressure level should not include these two acoustic spectrum peaks.

Since design acoustic loads are usually given from 0 to 10,000 Hz in one-third octave or one-octave band levels, the applied overall sound pressure level can be obtained by summing these levels up to 10,000 Hz. The blade passage tone and its next harmonic can be eliminated (if predominant) by reducing the one-third or one-octave band levels containing these peaks to those levels contained in adjacent frequency bands. The one-third octave or one-octave levels can then be summed in the following way:

If the difference (in dB) between two band levels is: 0 1 2 3 4 5 6 7 8 9 10 >10

Then add to the larger level (dB): 3 2.5 2.1 1.8 1.5 1.2 1.0 0.8 0.6 0.5 0.4 0

Example: If there were four bands with the following levels (dB):



This 144.5 dB is the overall sound pressure level to be used as the design load.

6. COMPARISONS WITH DESIGN METHODS FOR ALUMINUM PANELS
CFRP skin-stringer structures, of the type evaluated in this
programme, are primarily in competition with similarly configured
aluminum structures for application on both military and civil
airplanes. Cost/weight tradeoffs between cfrp and aluminum
structures, having comparable sonic fatigue resistance, are therefore of interest to potential users of the design method in Section 5.
A typical broadband sonic fatigue design load spectrum was used
which had an overall sound pressure level of 157 dB and a corresponding acoustic spectrum level of 132 dB/Hz in the frequency range of
interest. This 25 dB difference between overall and spectrum levels
is compatible with the acoustic load in this programme.

The following example problem was used for comparison:

Required life = 10^7 cycles (using a 50% confidence level)

b = 8

a/b = 2

 $\zeta = 0.02$

Calculate required skin thickness.

The following results were obtained:

Riveted Aluminium Skin-Stringer: t = 0.05-in.

Riveted Aluminium Skin-Stringer: t = 0.076-in.

Bonded cfrp Skin-Stringer: t = 0.037-in.

An 8-ply skin laminate having a thickness of 0.044 inch would fall within the 90-percent confidence interval for equation 25.

Since the material density of cfrp is approximately half that of aluminum, the difference in weight between cfrp panels and aluminum panels having comparable sonic fatigue resistance, approaches 2-1/2 to 1.